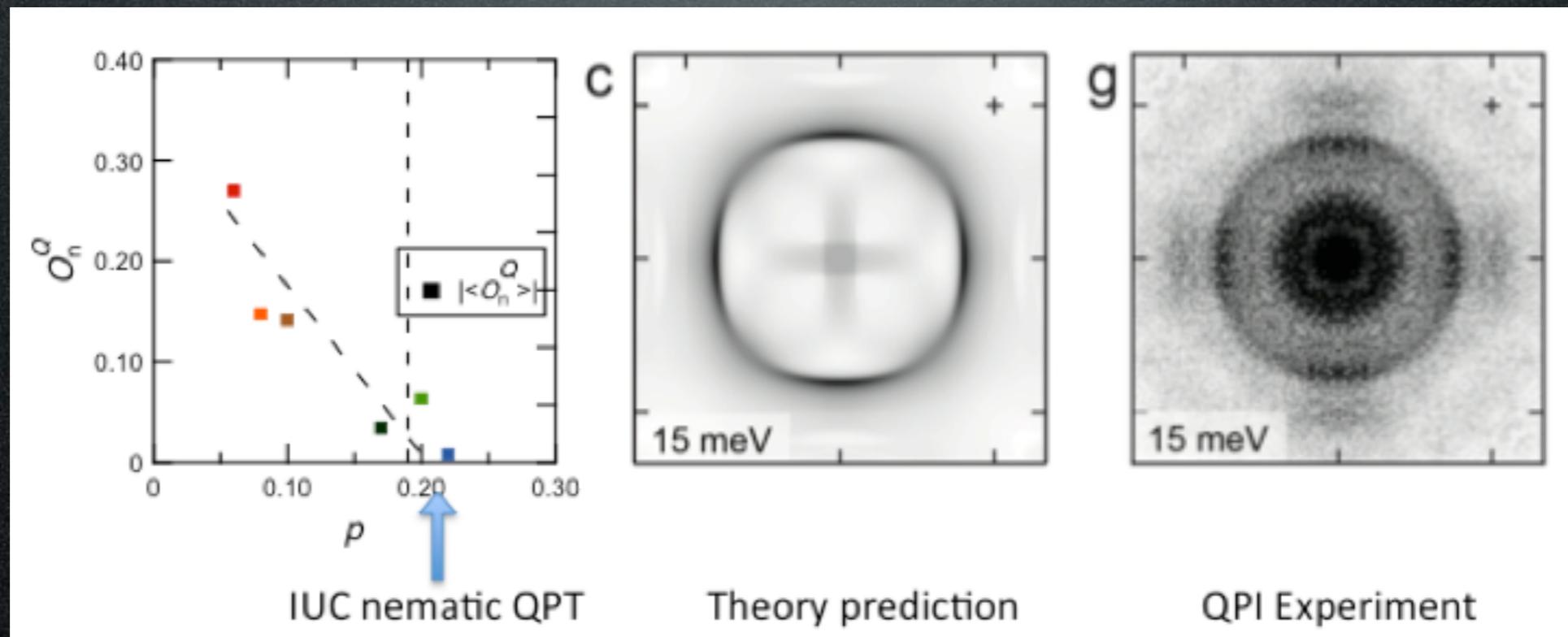
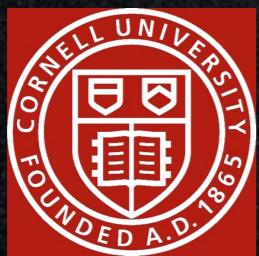


Recent Theoretical Advances in the Study of High-T_c Superconductivity using a 'Middle-top/down' Approach

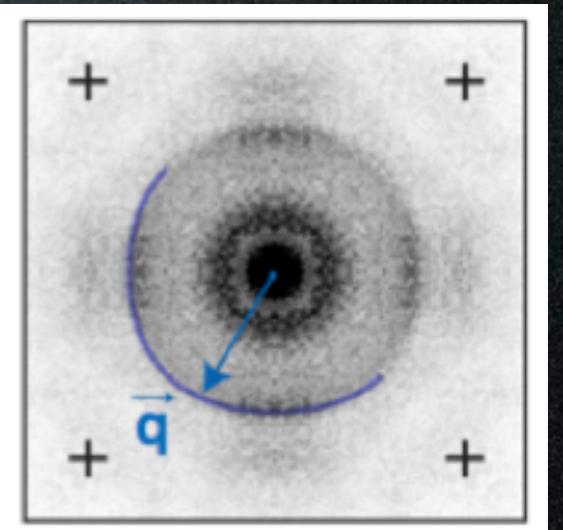
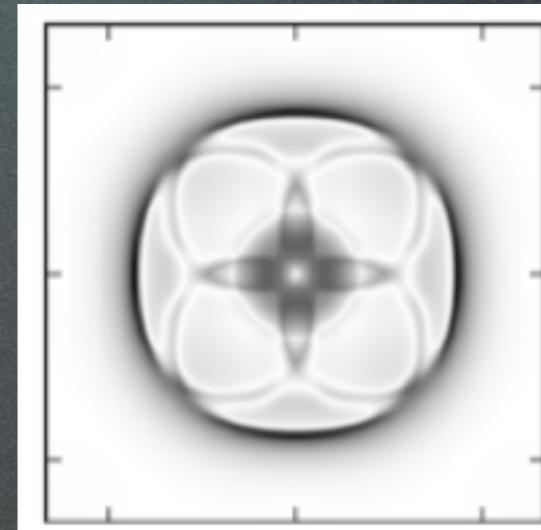
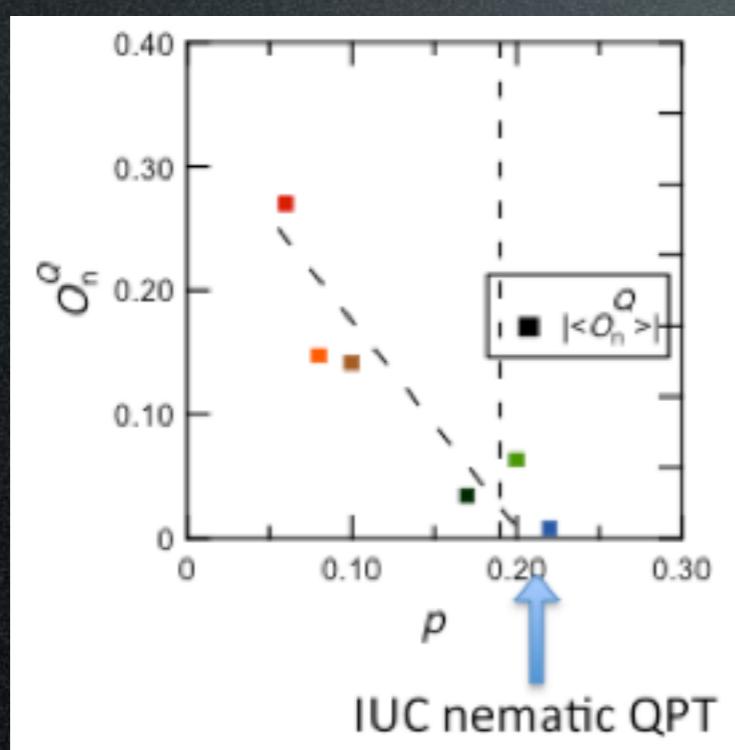
Eun-Ah Kim



Penn State, Oct 2, 2014

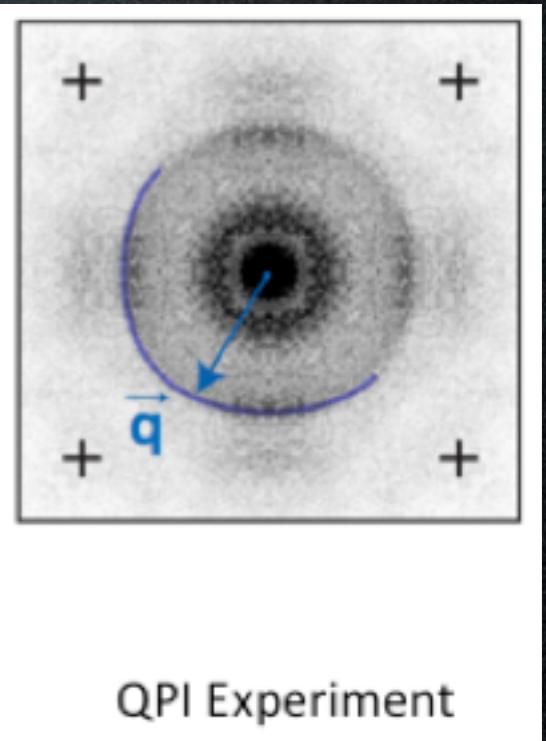
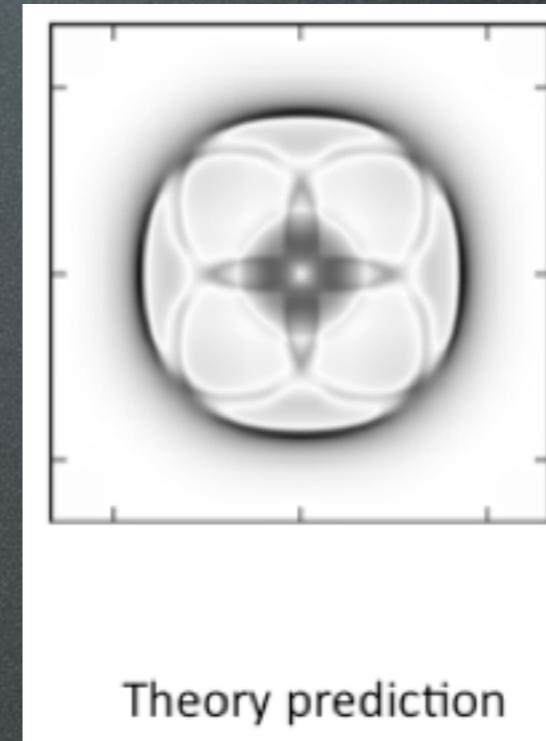
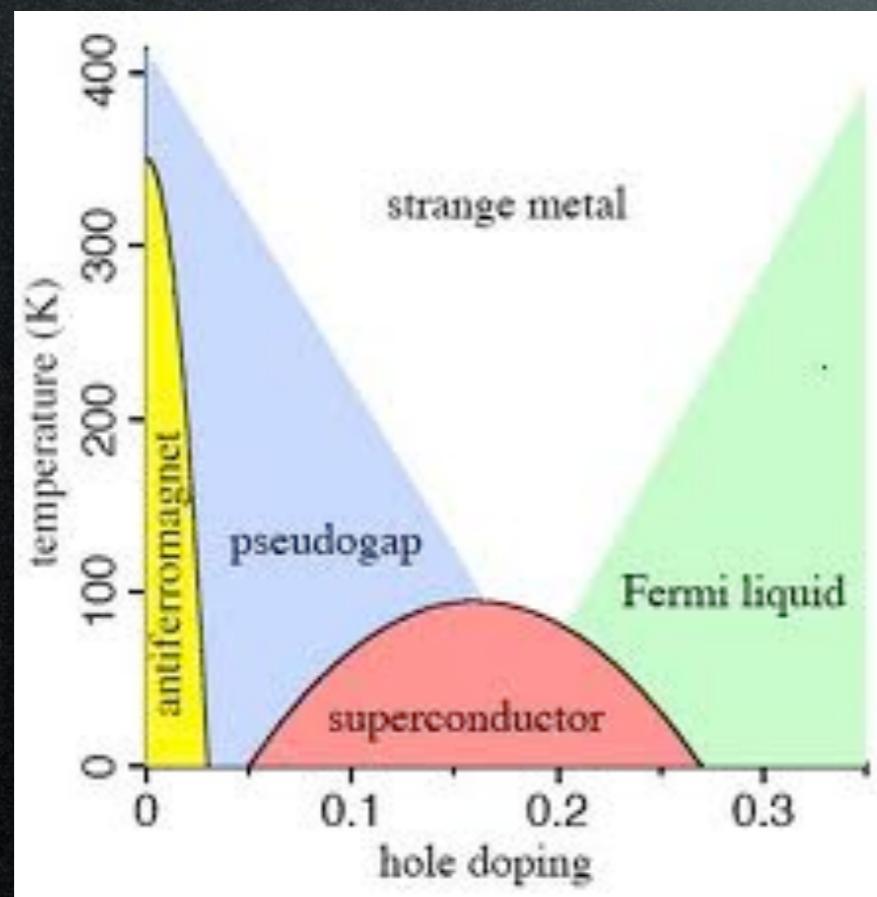


Recent Theoretical Advances in the Study of High-T_c Superconductivity using a 'Middle-top/down' Approach



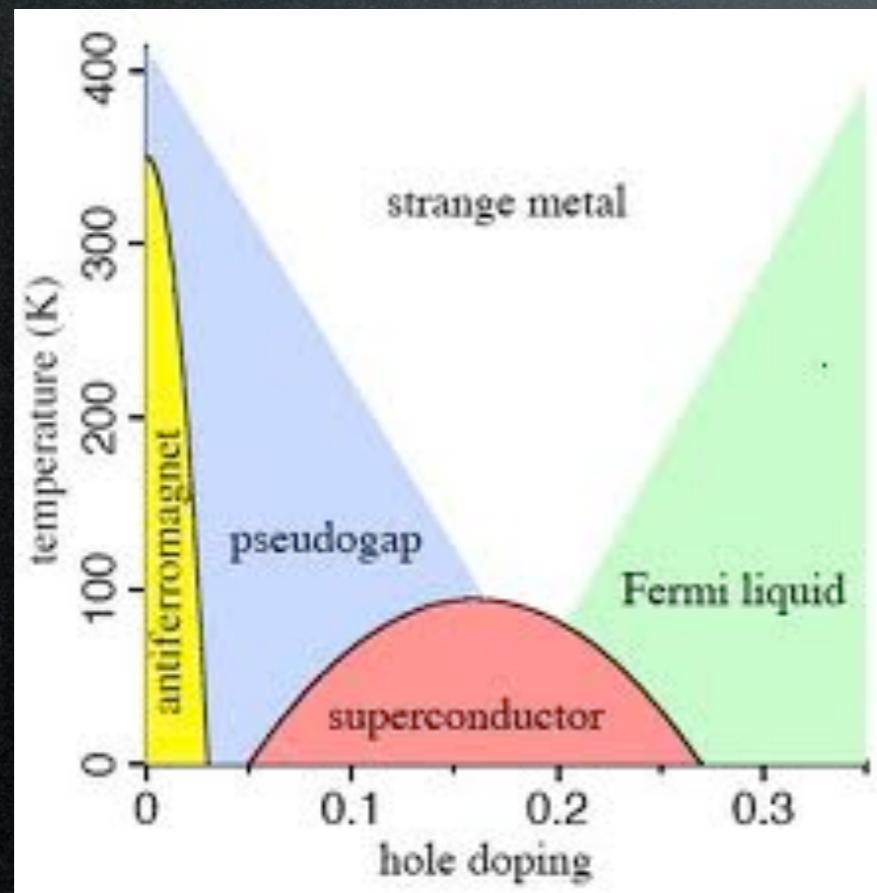
Recent Theoretical Advances in the Study of High- T_c Superconductivity using a 'Middle-top/down' Approach

The Phase Diagram

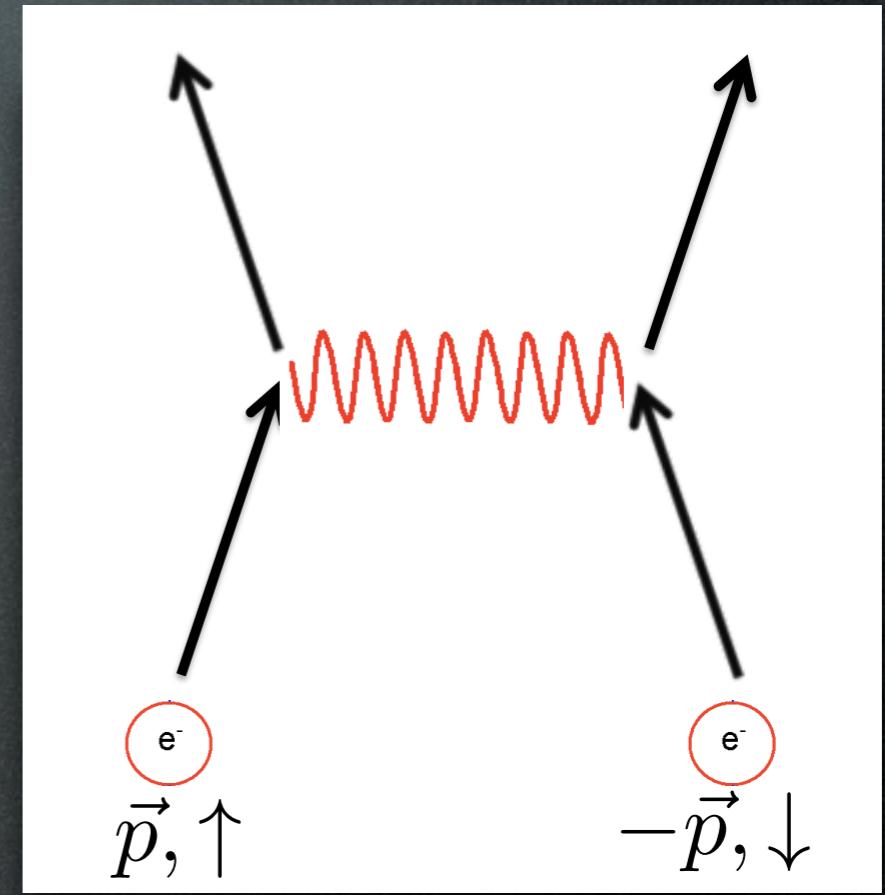


Recent Theoretical Advances in the Study of High- T_c Superconductivity using a 'Middle-top/down' Approach

The Phase Diagram



The Mechanism



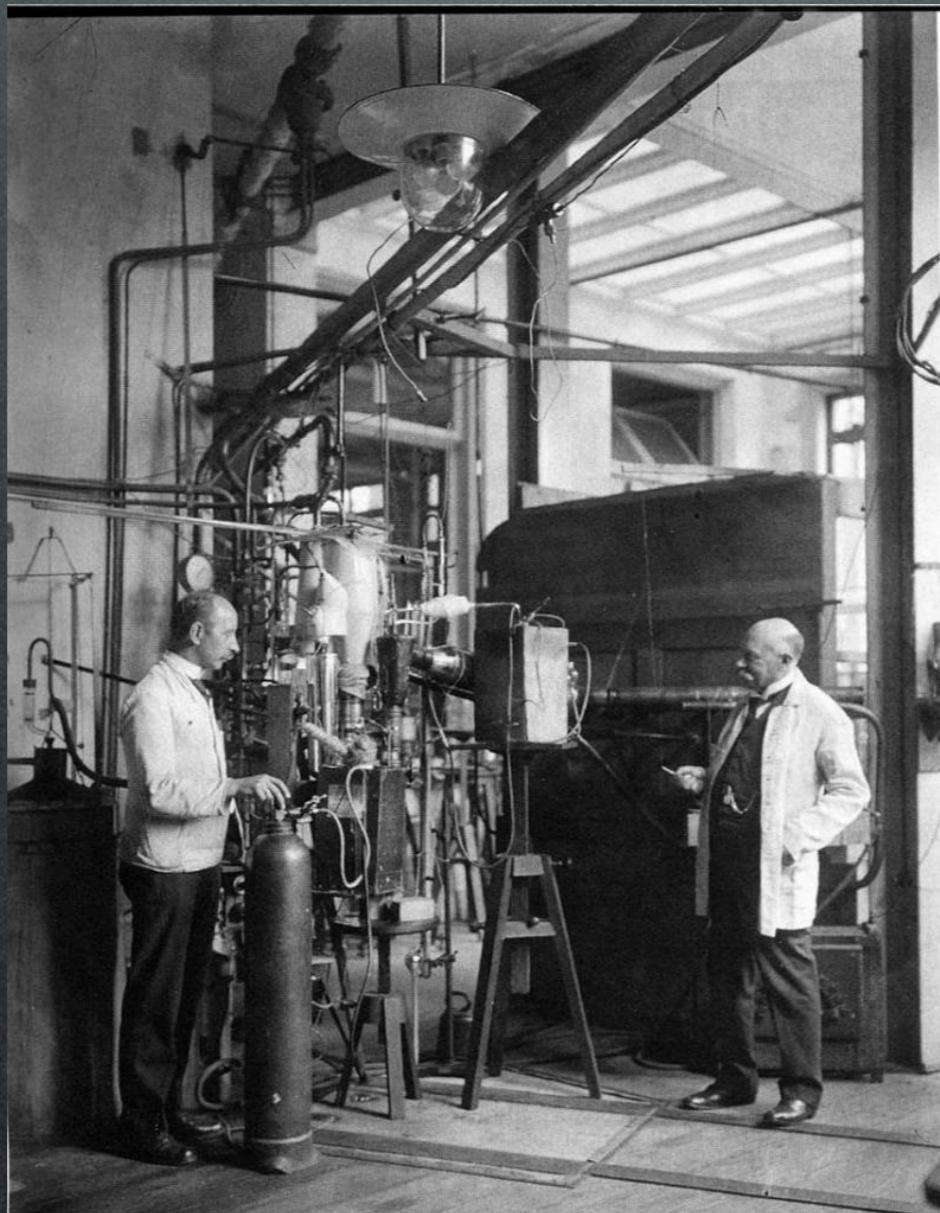
Please STOP ME and ASK
QUESTIONS

CONVENTIONAL SUPERCONDUCTIVITY

Heike Kamerlingh Onnes

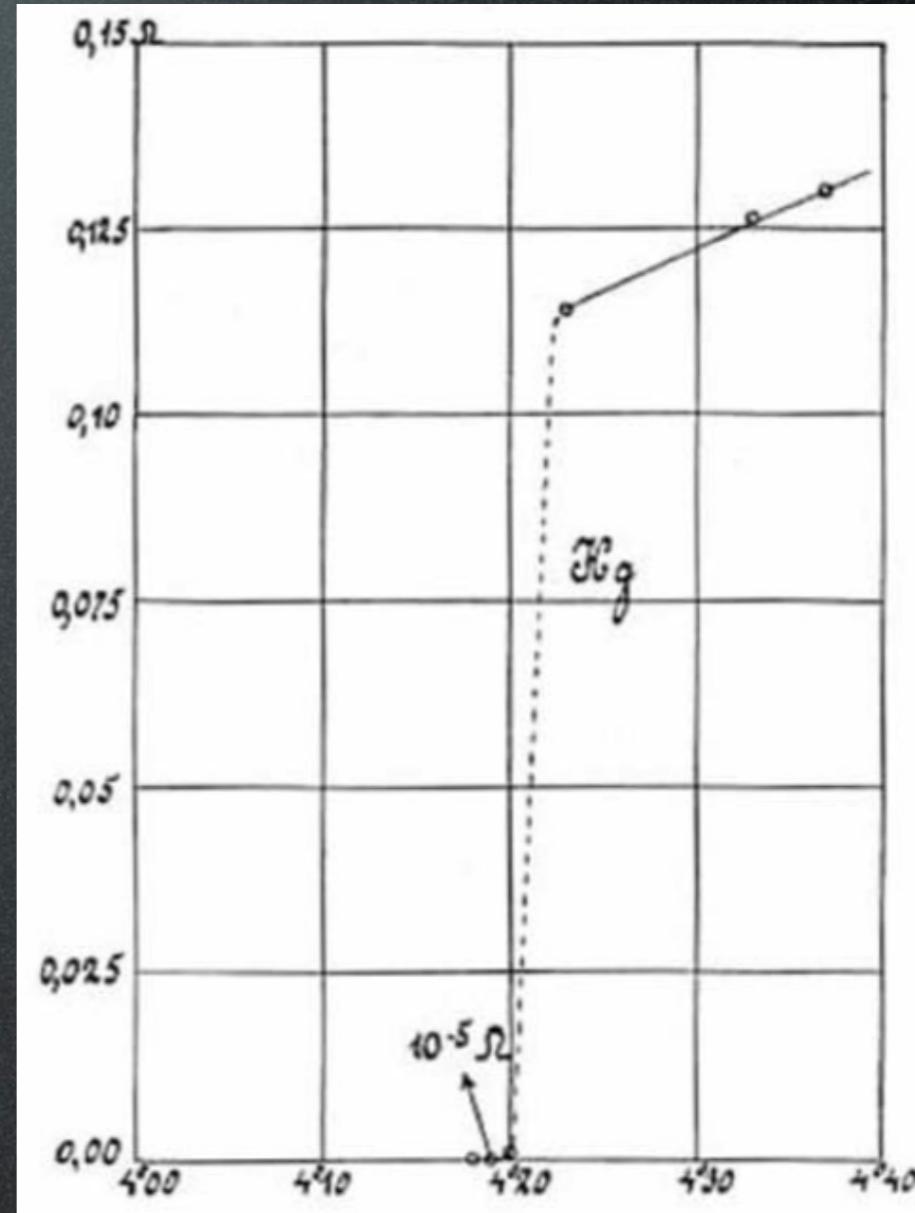


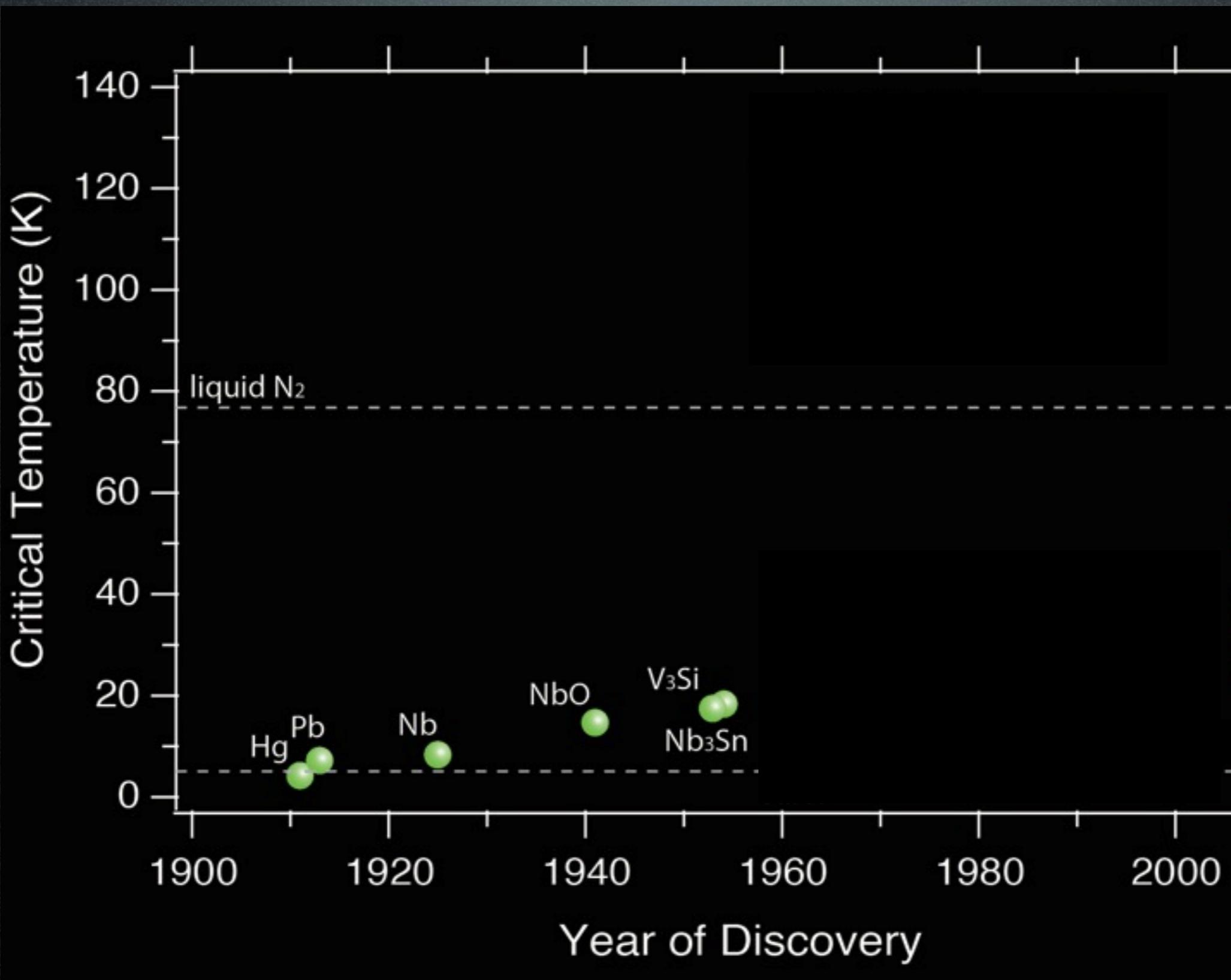
Liquefied Helium in 1908



Verslagen van de Afdeeling
Natuur-kunde der Kon. Acad. van
Wetenschappen te Amsterdam,
pp. 1479, 28 April 1911.

Superconductivity 1911



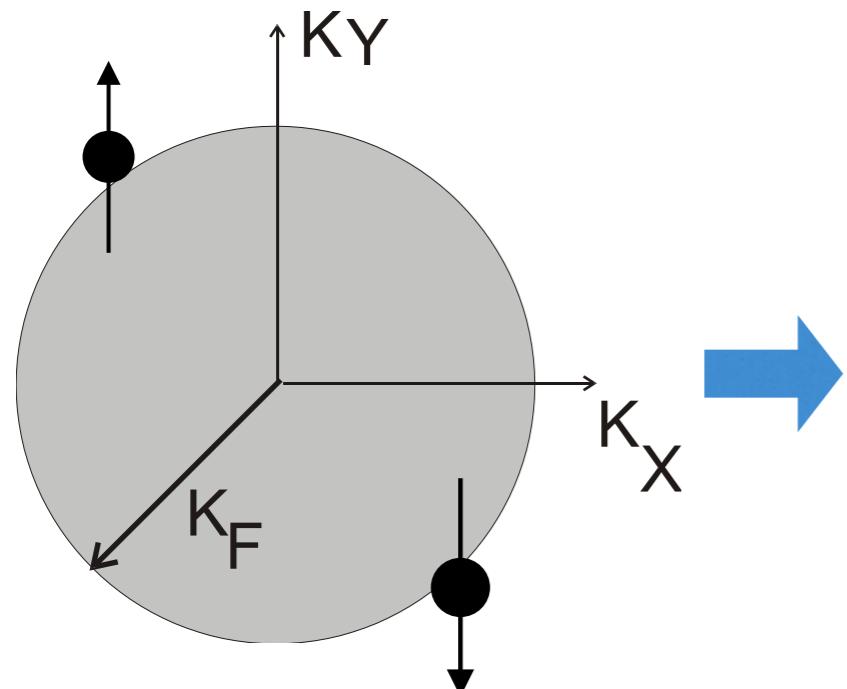


BCS theory of conventional superconductivity

BCS, Phys Rev 108, 1175 (1957)

Bogoliubov, Nuovo Cimento 7, 794 (1958)

Normal State (Metal)



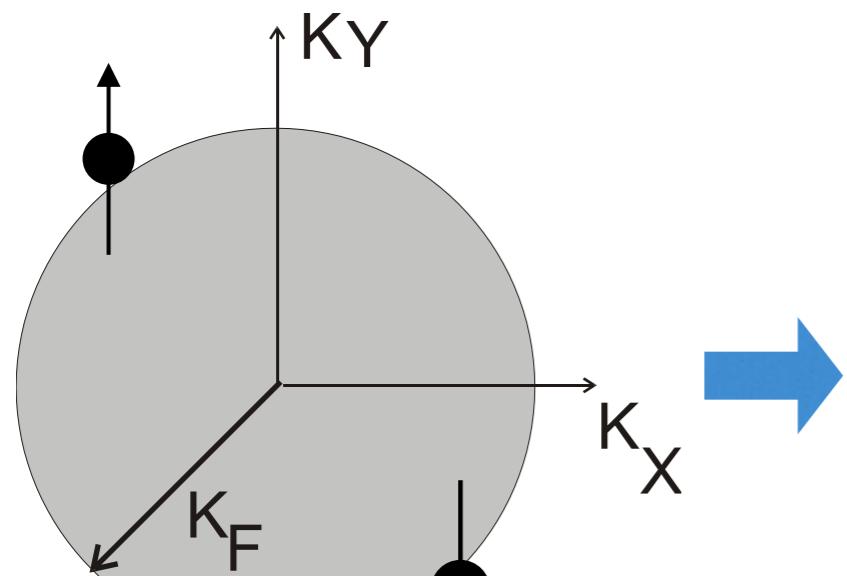
Degenerate
~free electron gas

BCS theory of conventional superconductivity

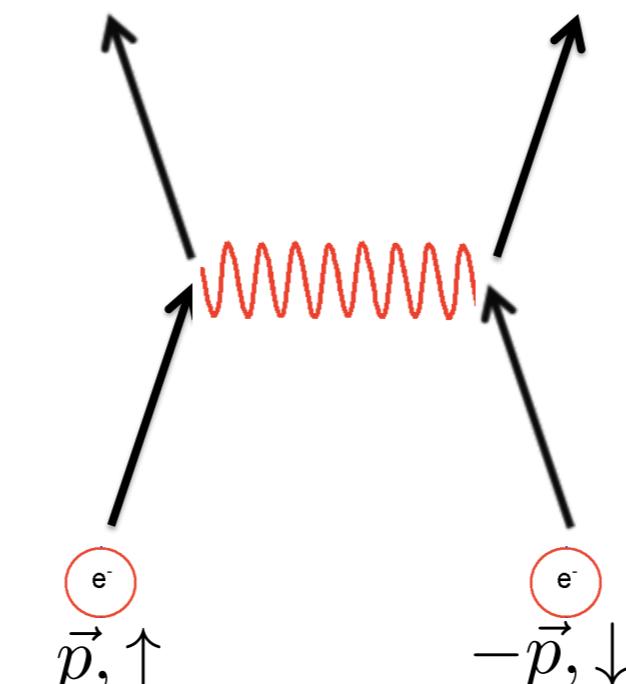
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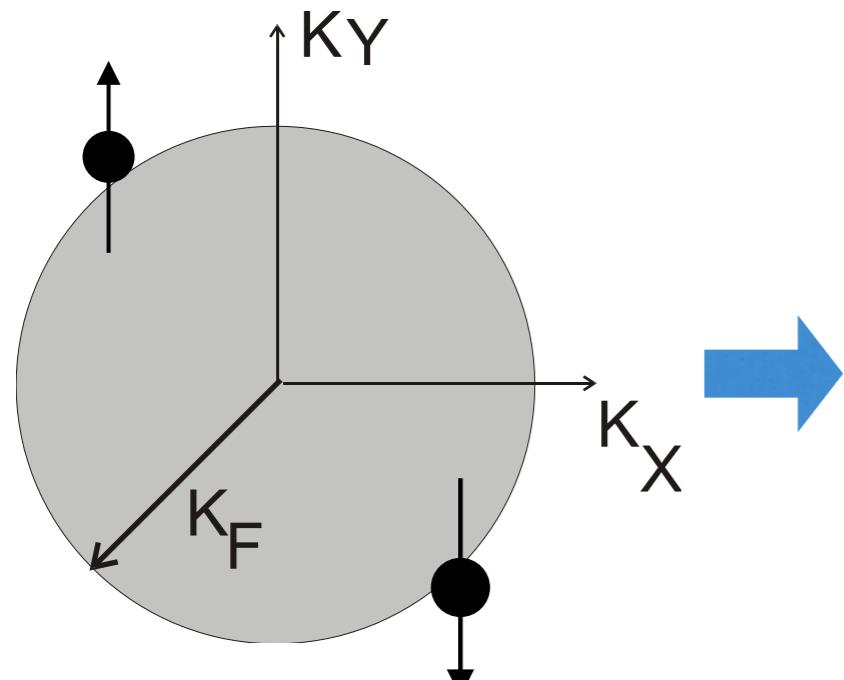
Electrons interacting with
Lattice Vibration Mode

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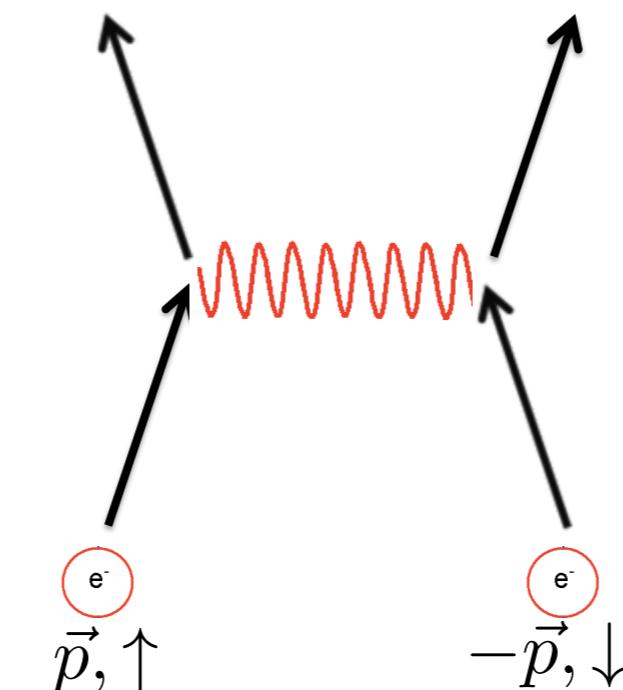
Bogoliubov, Nuovo Cimento 7, 794 (1958)

Normal State (Metal)



Degenerate
~free electron gas

Weak coupling instability



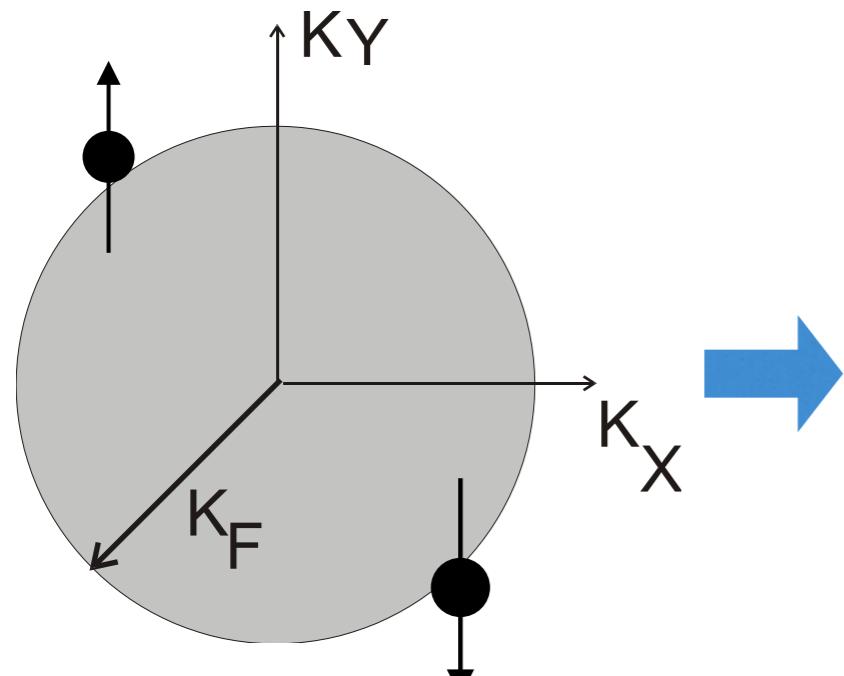
Electrons interacting with
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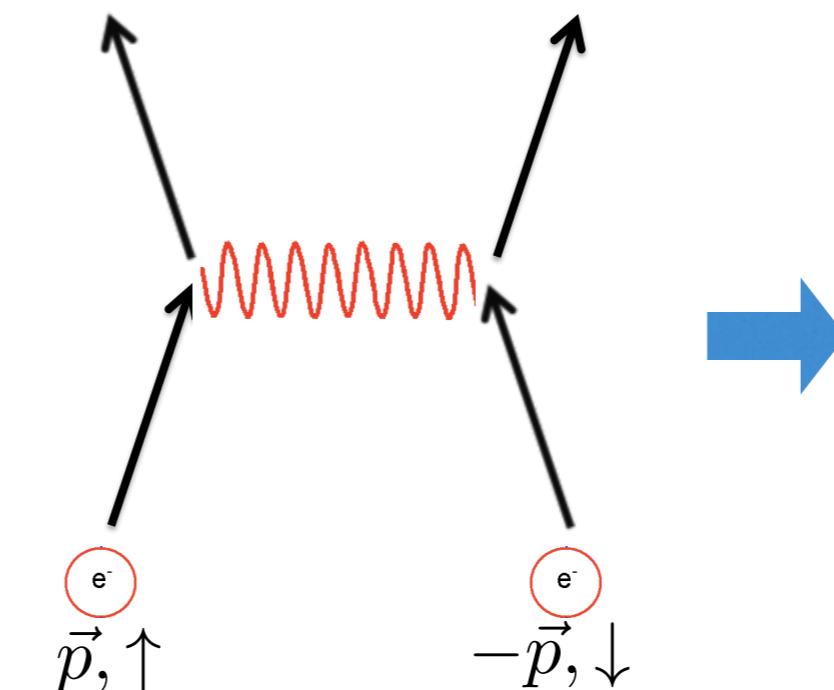
Bogoliubov, Nuovo Cimento 7, 794 (1958)

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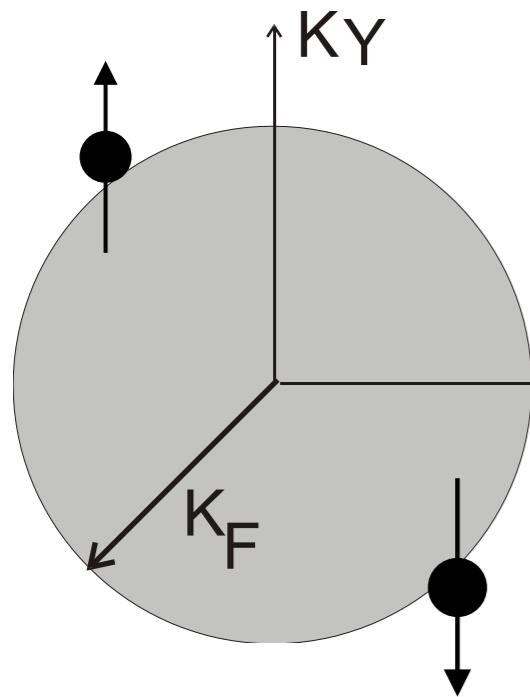
Low T- Superconducting
Ground/Excited States

BCS theory of conventional superconductivity

BCS, Phys Rev 108, 1175 (1957)

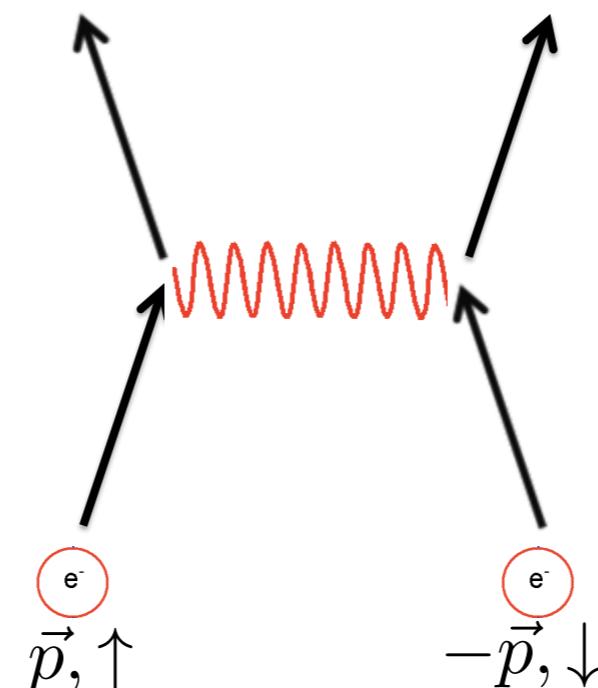
Bogoliubov, Nuovo Cimento 7, 794 (1958)

Normal State (Metal)



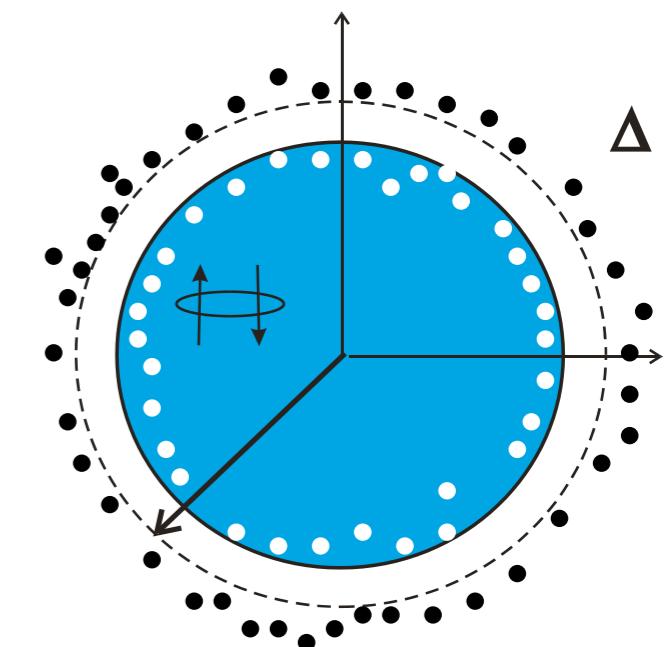
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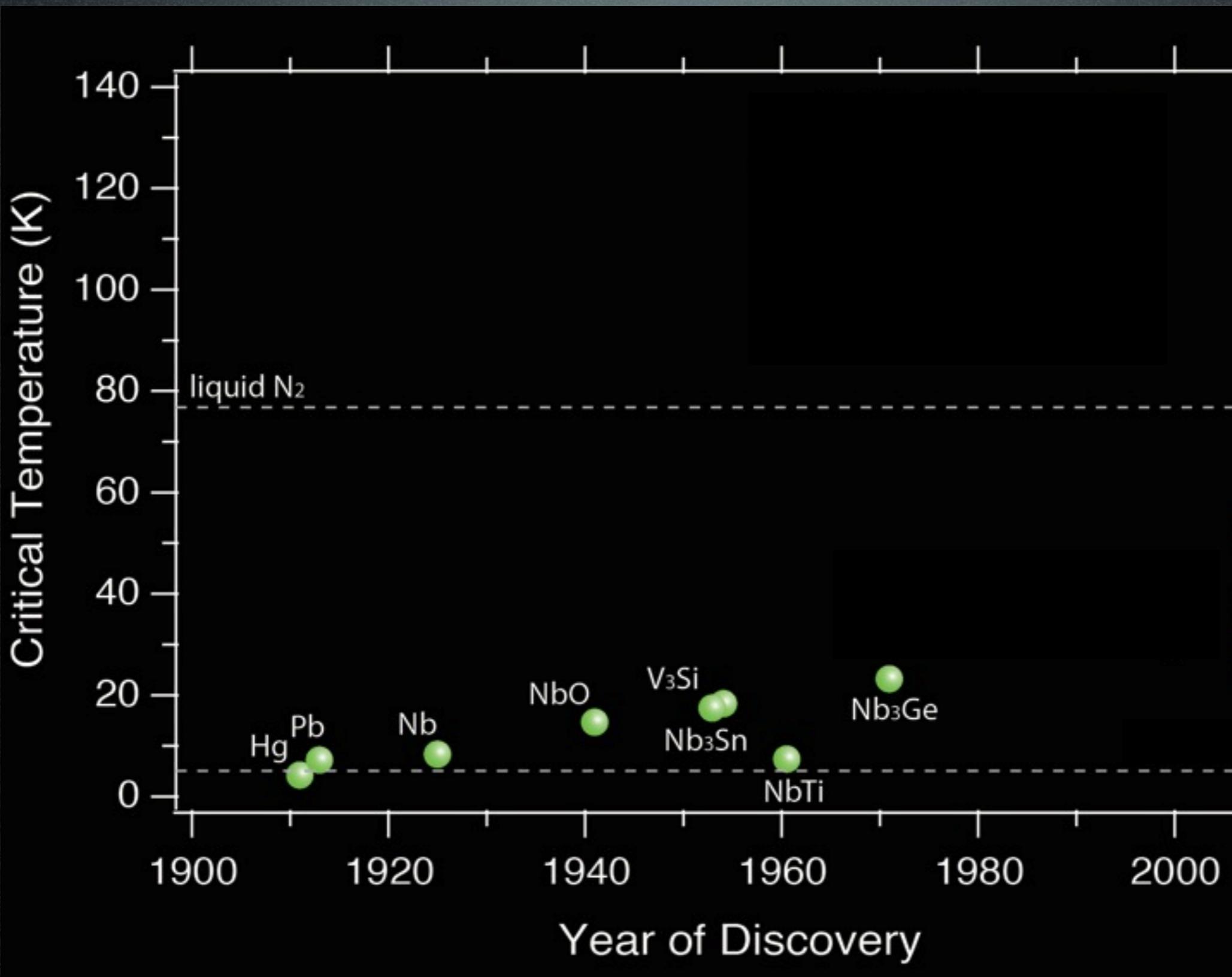


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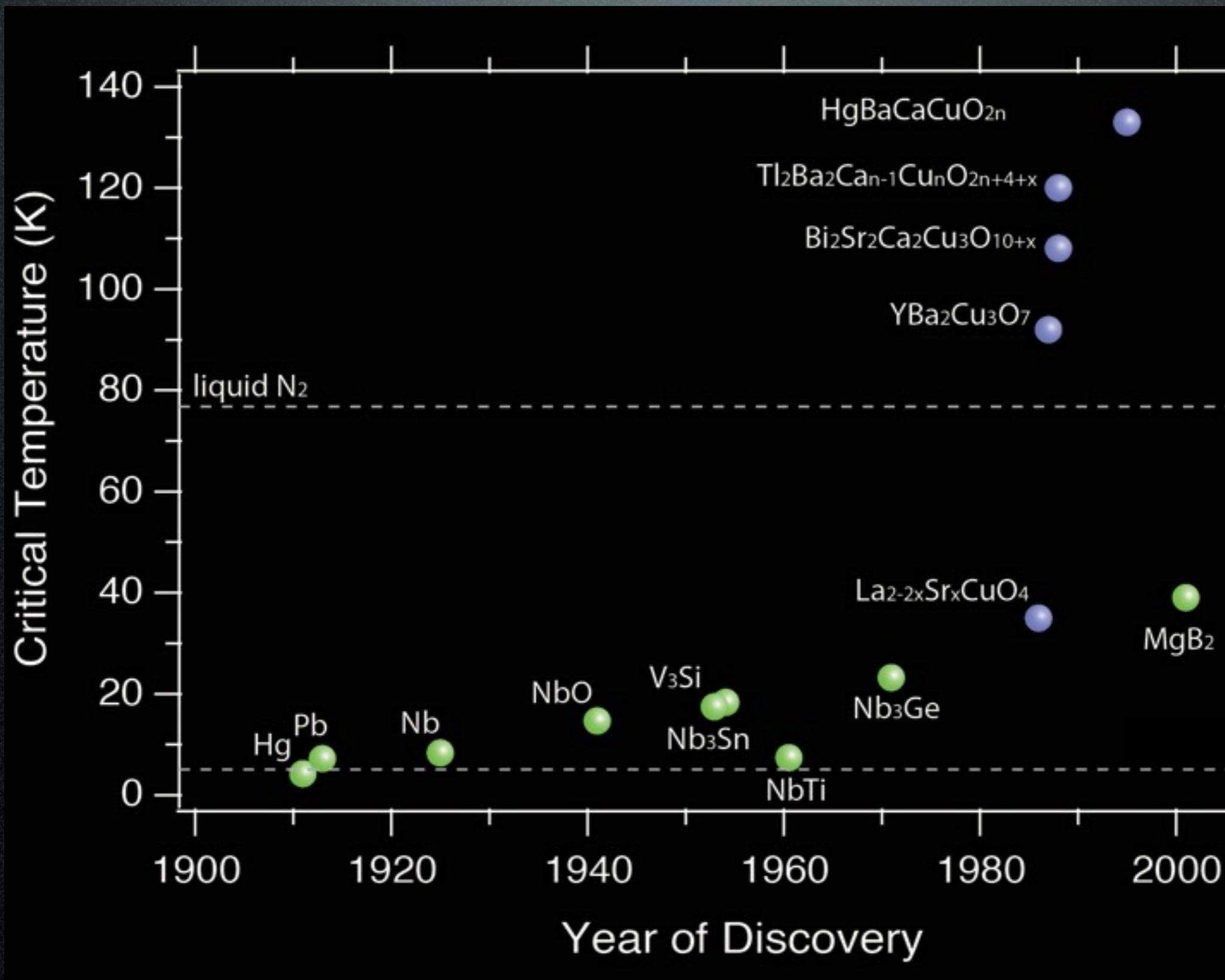
Low T- Superconducting
Ground/Excited States



- Gas of Cooper Pairs
- Pair-Energy Gap Δ
- Bog. quasiparticles



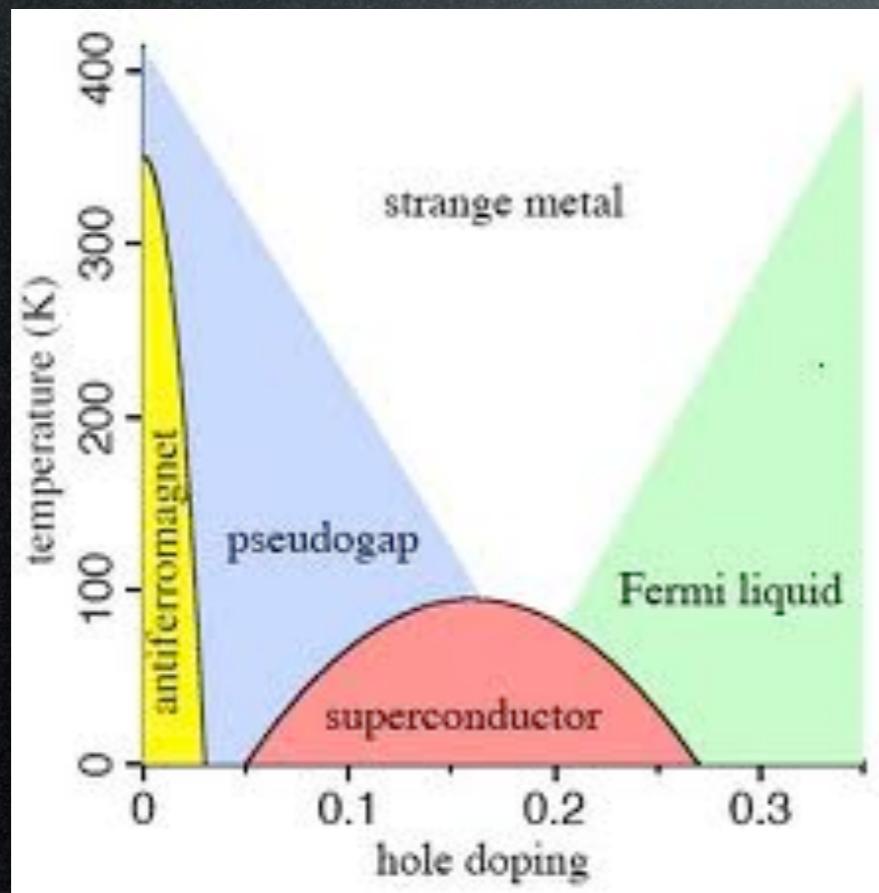
Correlated (High-T_c) Superconductivity



Key Questions in High-T_c Superconductivity:

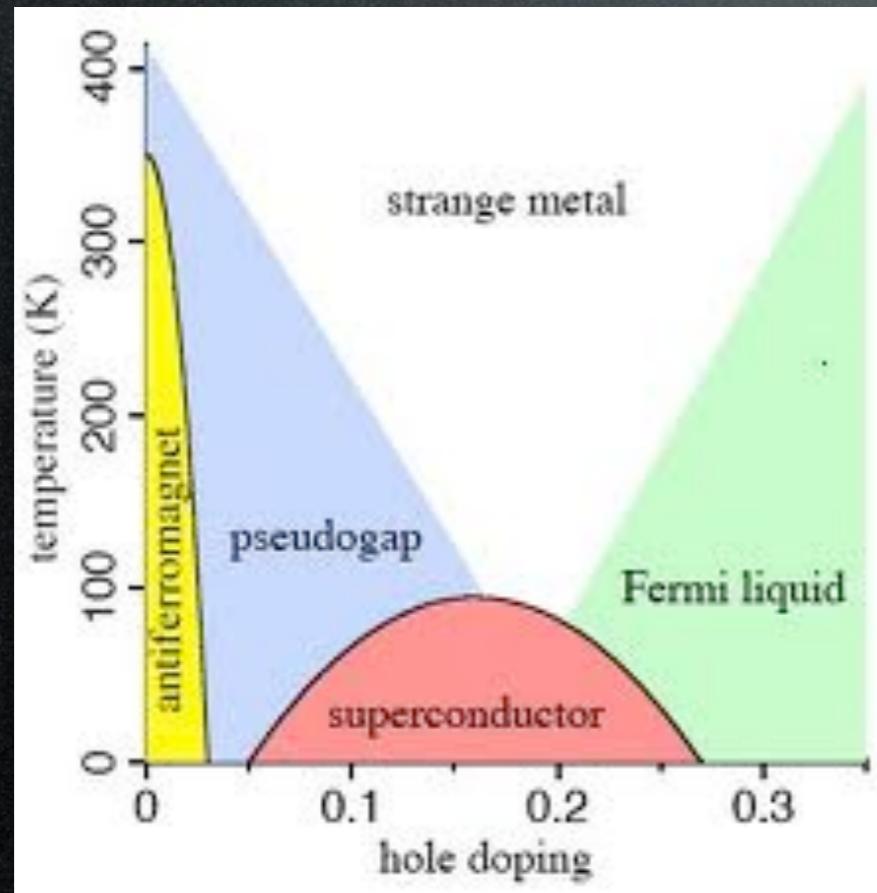
Key Questions in High- T_c Superconductivity:

The Phase Diagram?

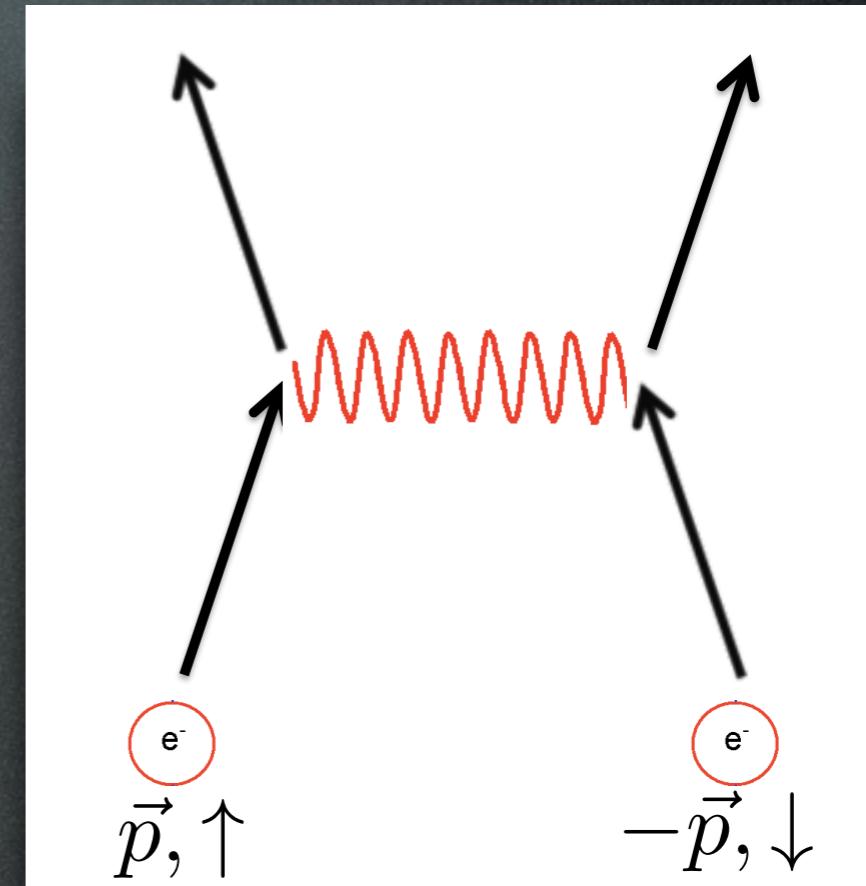


Key Questions in High- T_c Superconductivity:

The Phase Diagram?



The Mechanism?



The Challenge of Strong (Intermediate) Coupling

Interaction Energy vs Kinetic Energy

Liquid



$$V_{int} \ll E_{kin}$$

- Weak interaction
- K-space

Interaction Energy vs Kinetic Energy

Crystal



Liquid



$$V_{int} \gg E_{kin}$$

- Strong interaction
- Real space

$$V_{int} \ll E_{kin}$$

- Weak interaction
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Interaction Energy vs Kinetic Energy

Crystal



Liquid



$$V_{int} \gg E_{kin}$$

- Strong interaction
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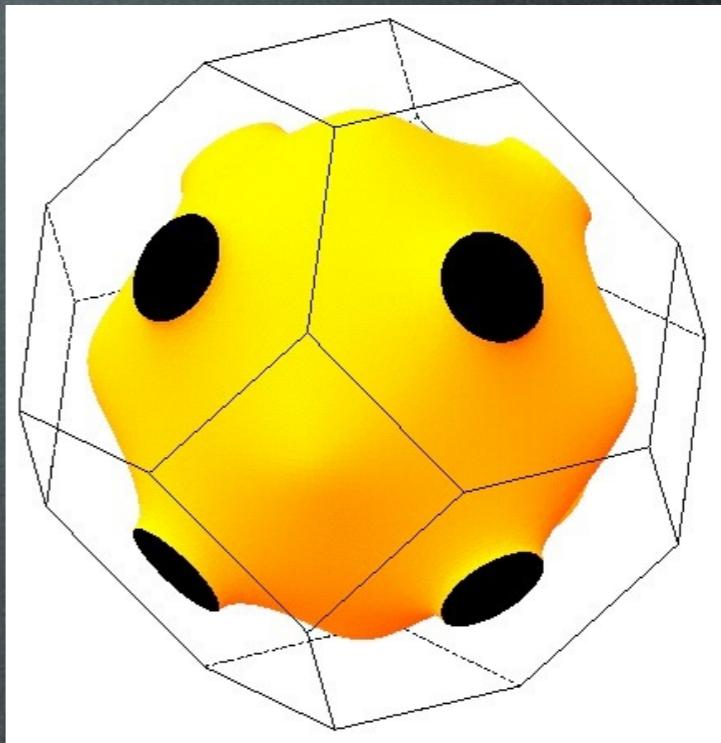
$$V_{int} \ll E_{kin}$$

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Freezing

Interaction Energy vs Kinetic Energy

Landau Fermi Liquid (1956)

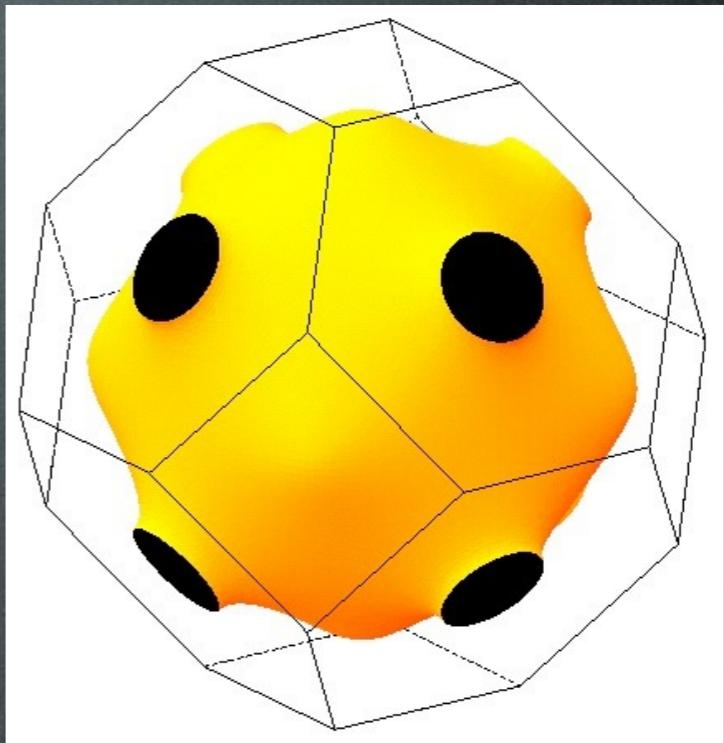


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Interaction Energy vs Kinetic Energy

Landau Fermi Liquid (1956)

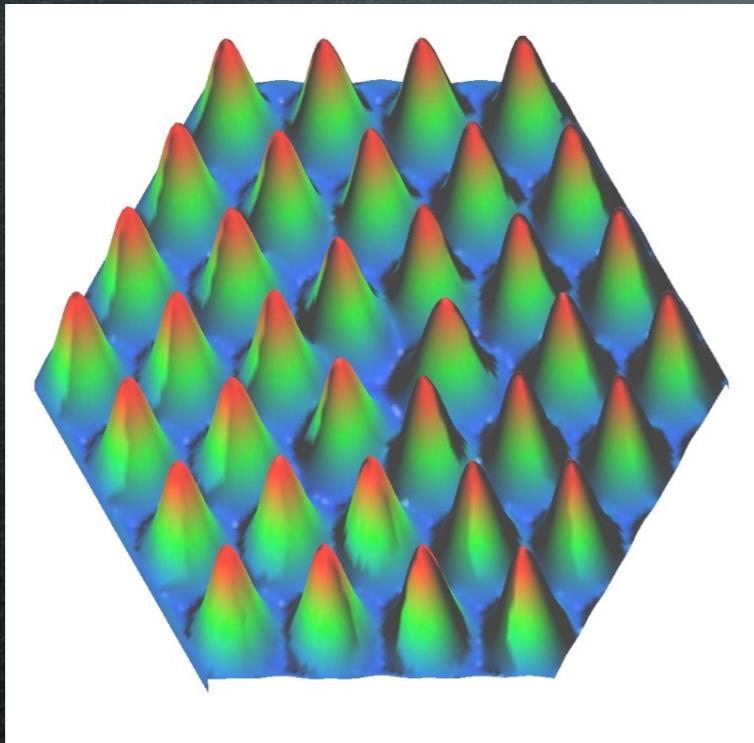


$$V_{int} \ll E_{kin}$$

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Fermi surface instabilities

Interaction Energy vs Kinetic Energy

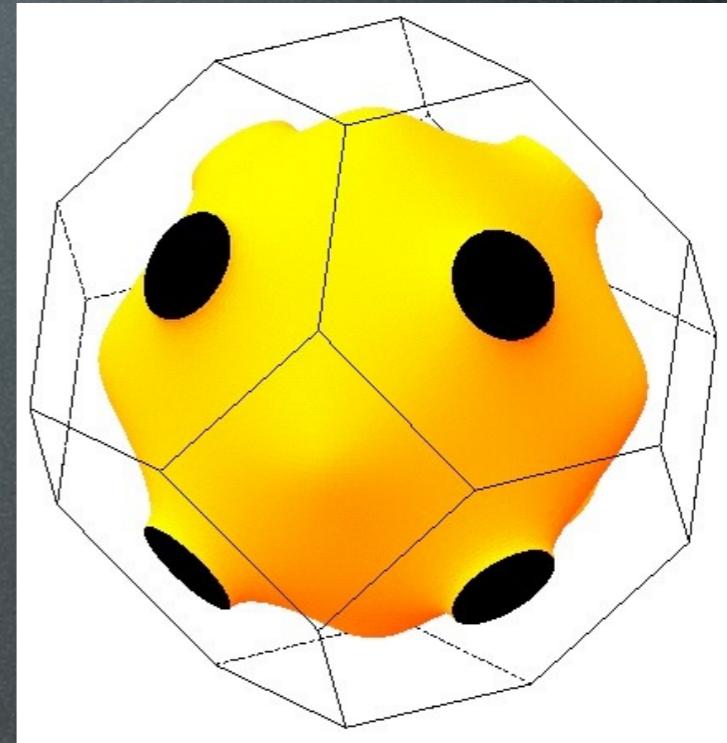


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Landau Fermi Liquid (1956)

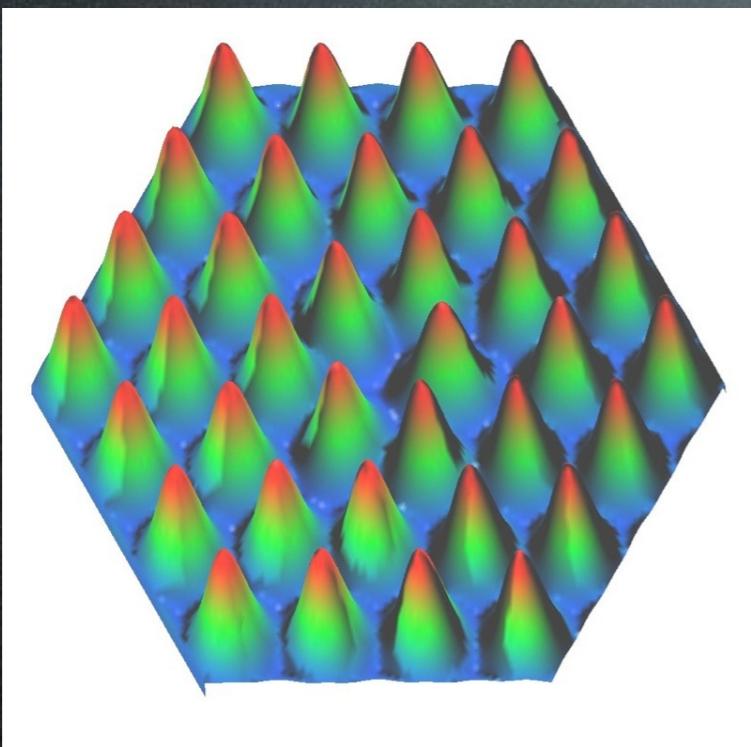


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Interaction Energy vs Kinetic Energy

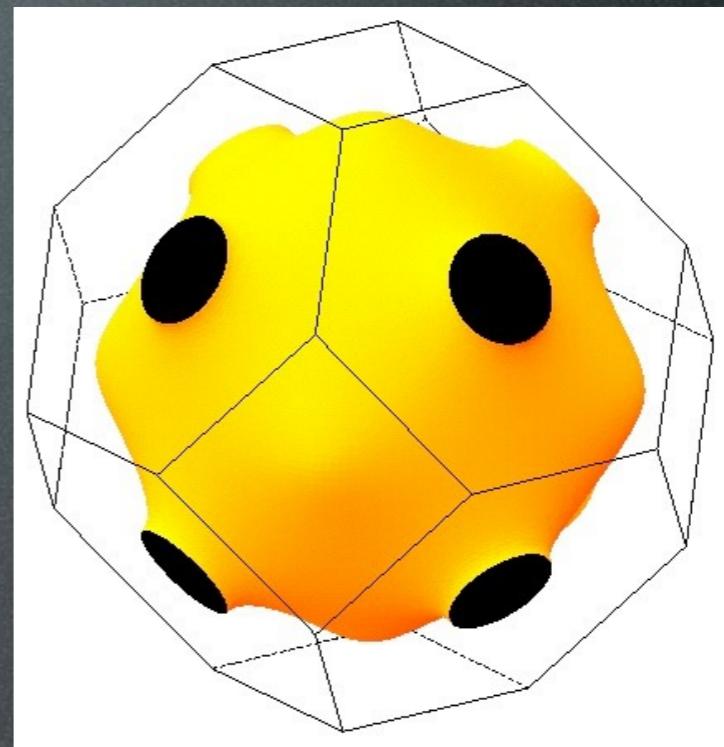
Wigner Crystal (1930)



$$V_{int} \gg E_{kin}$$

- Strong interaction
- Real space

Landau Fermi Liquid (1956)



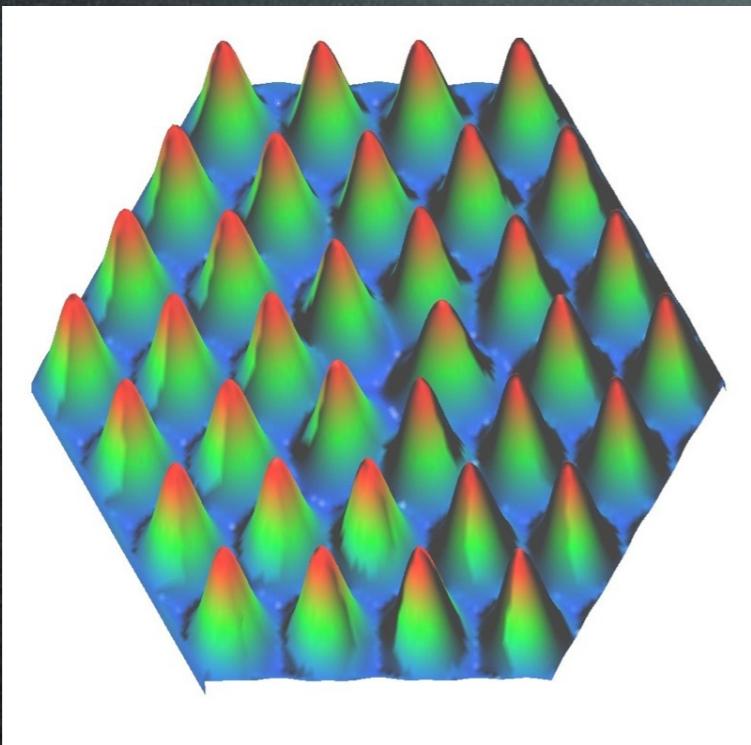
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Fermi surface instabilities

Interaction Energy vs Kinetic Energy

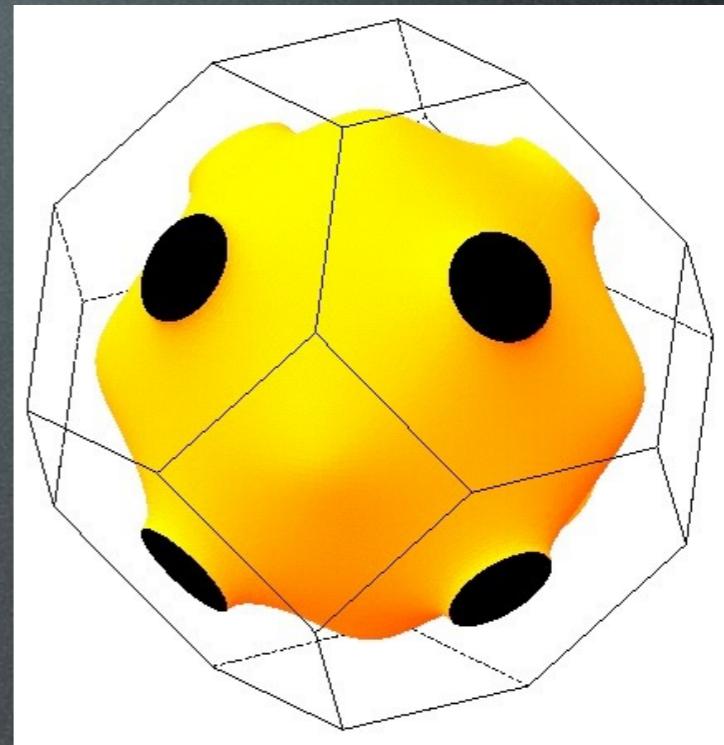
Wigner Crystal (1930)
Mott Insulator (1937)



$$V_{int} \gg E_{kin}$$

- Strong interaction
- Real space

Landau Fermi Liquid (1956)



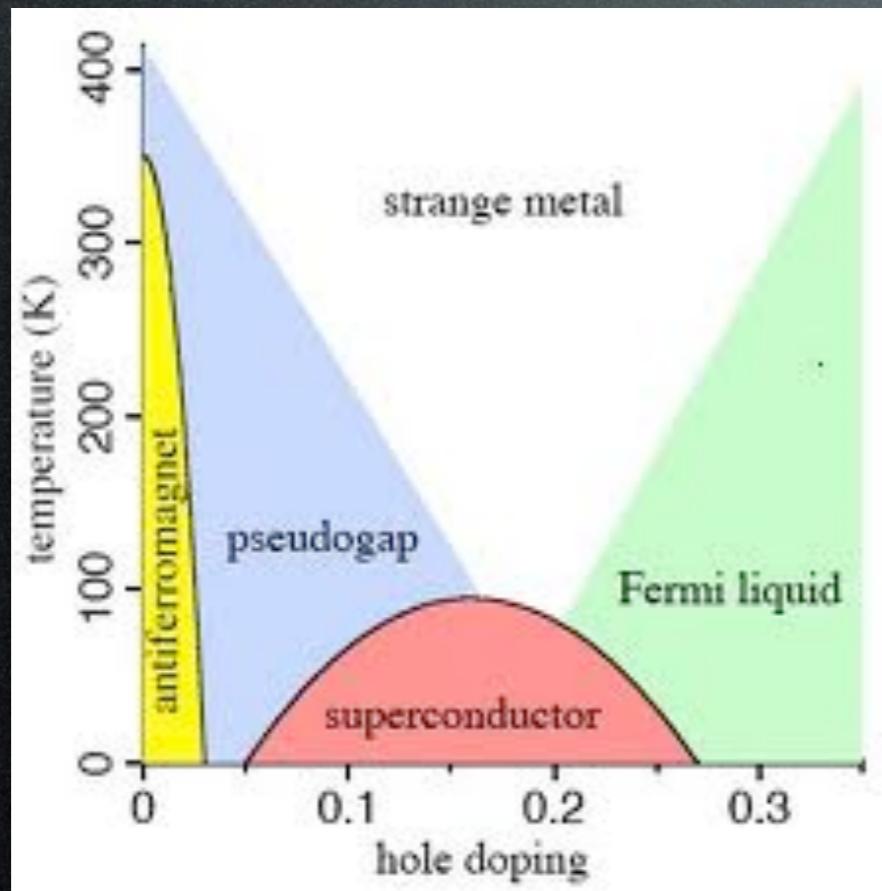
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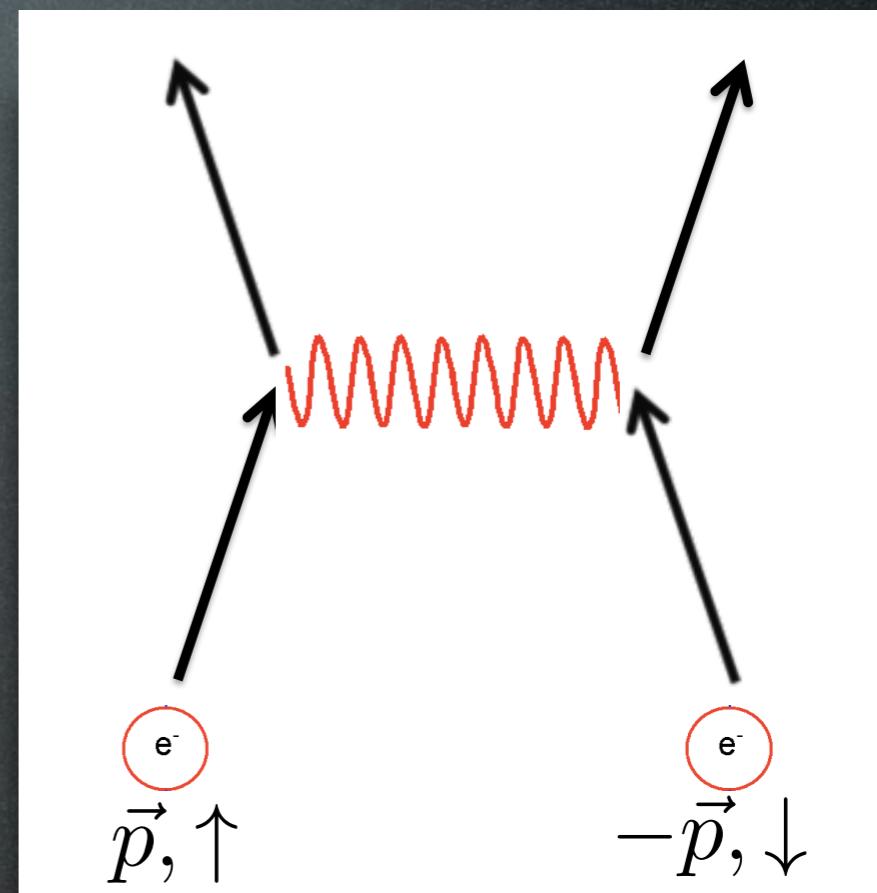
Fermi surface instabilities

Key Questions in High- T_c Superconductivity:

The Phase Diagram?

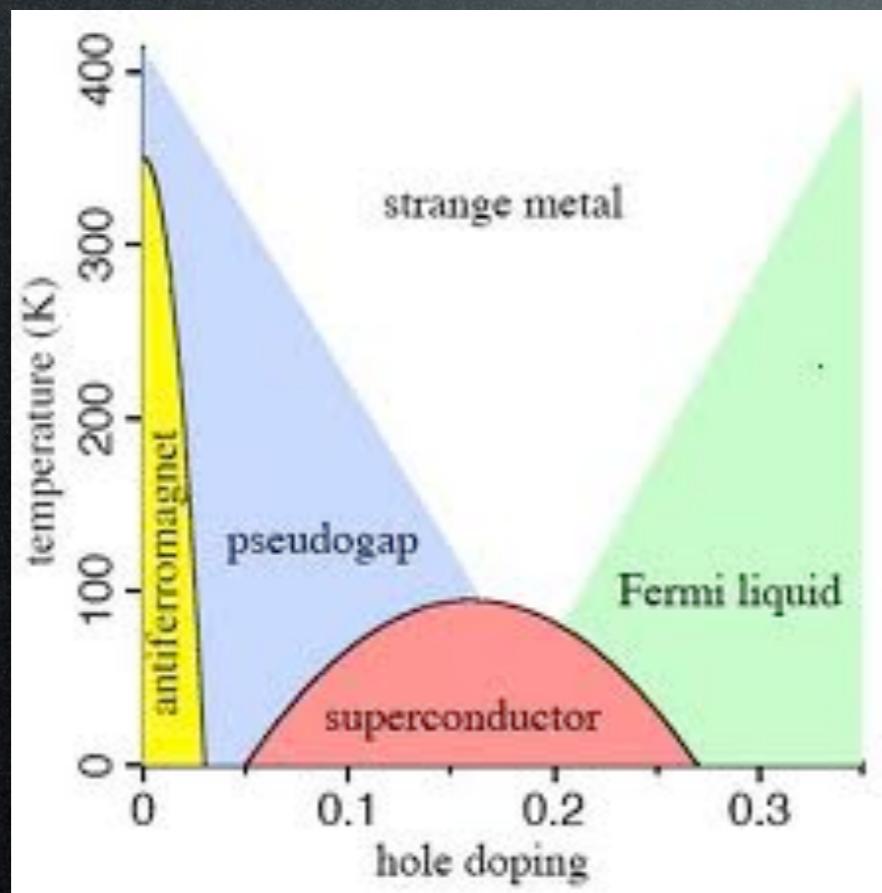


The Mechanism?

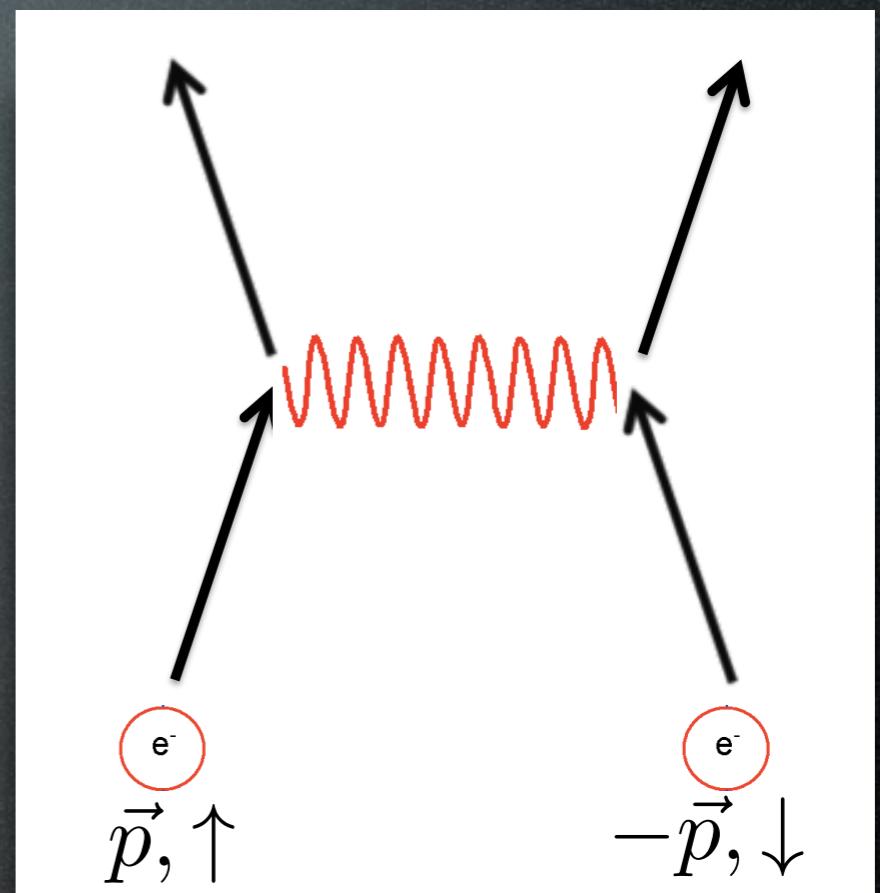


Key Questions in High- T_c Superconductivity:

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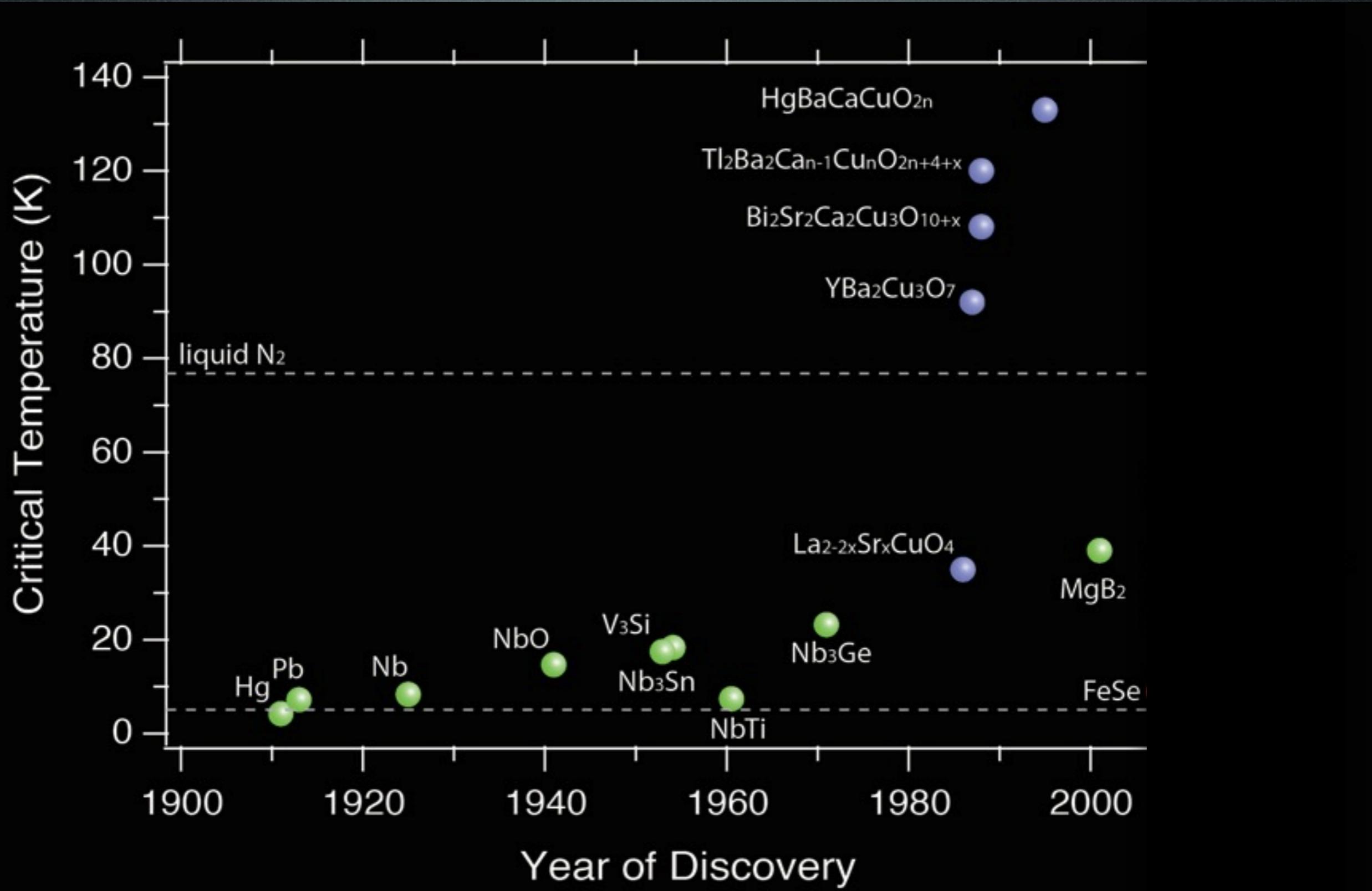


The Mechanism?



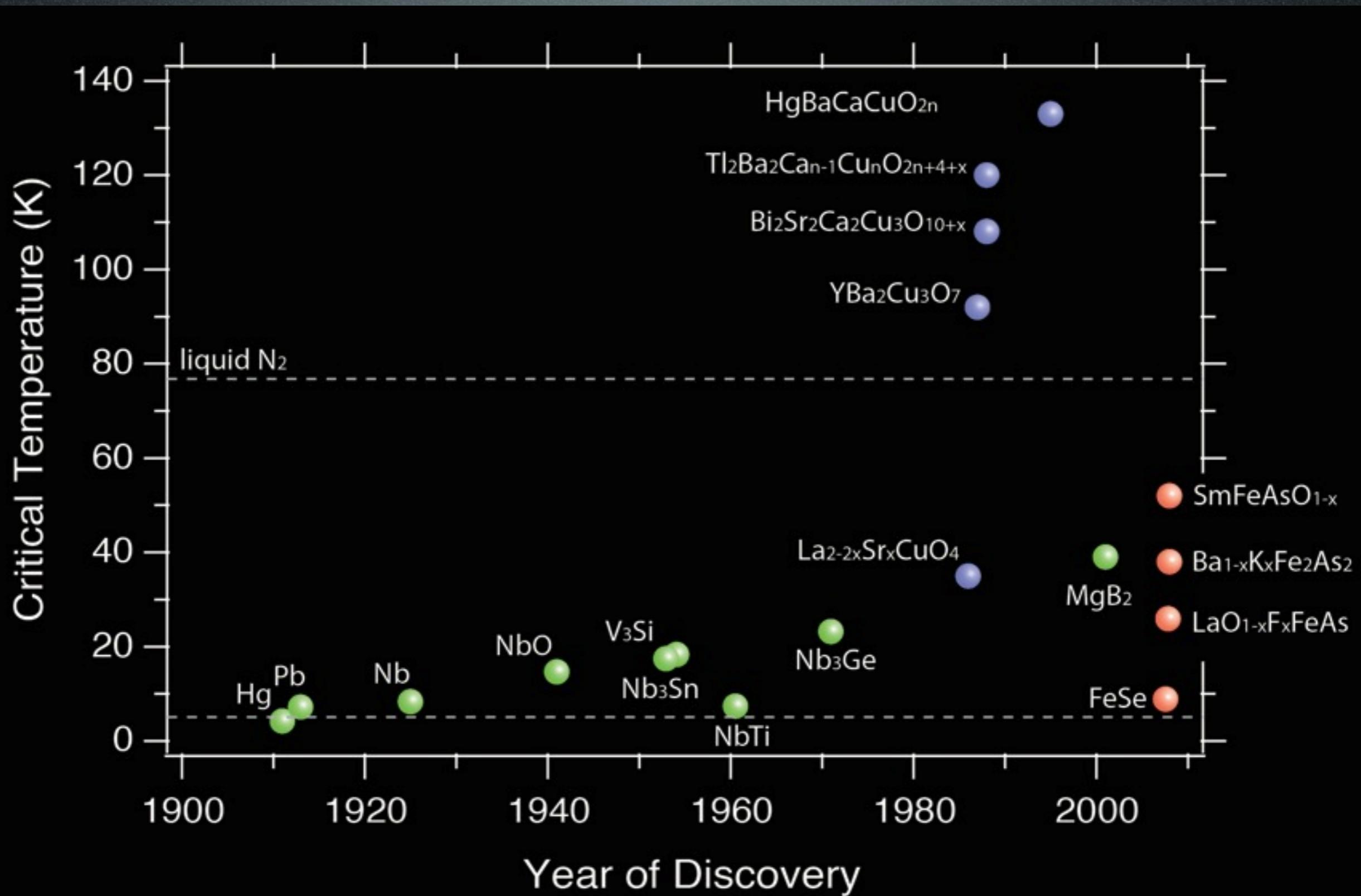
New Physics in the Intermediate Regime!

Recent Advances in Materials

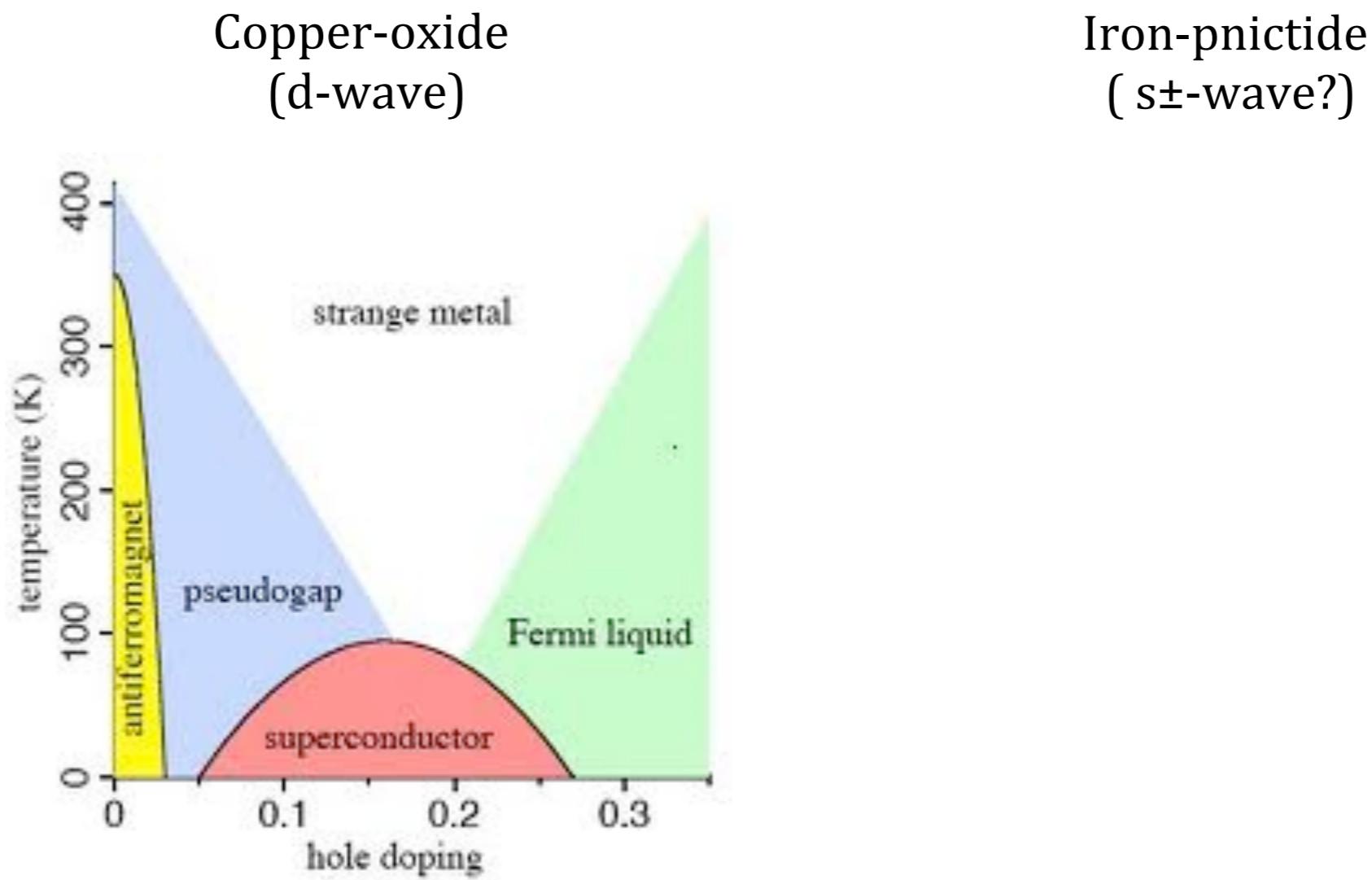


Recent Advances in Materials

Discovery of Fe-pnictide

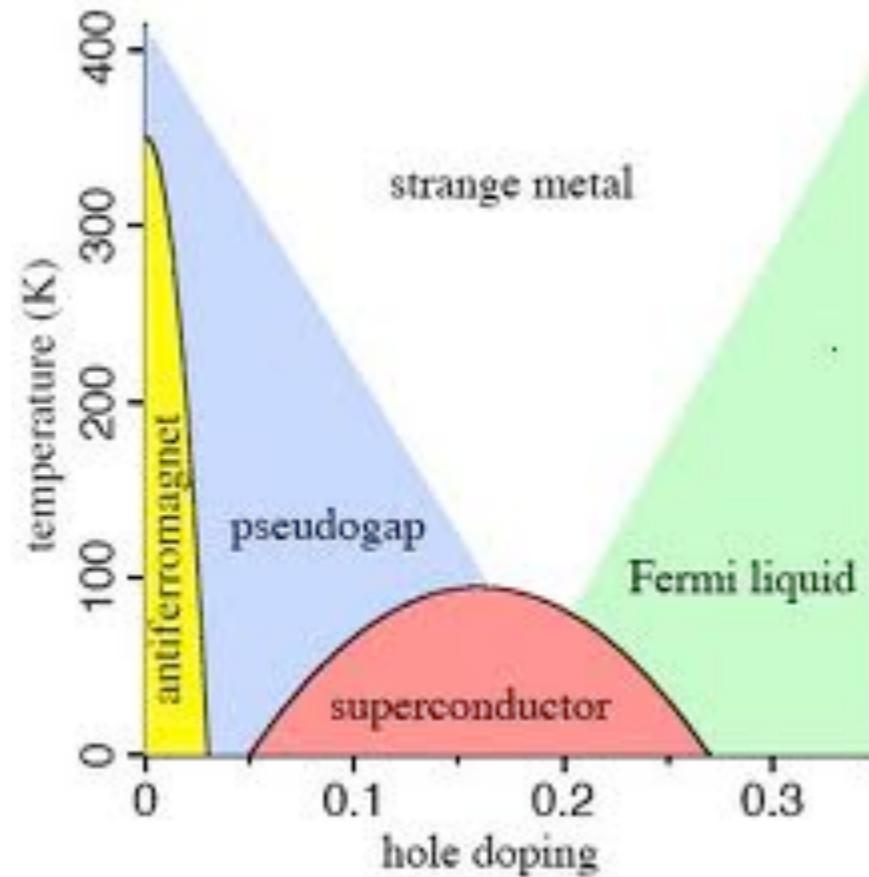


Copper-oxide vs Iron-pnictide

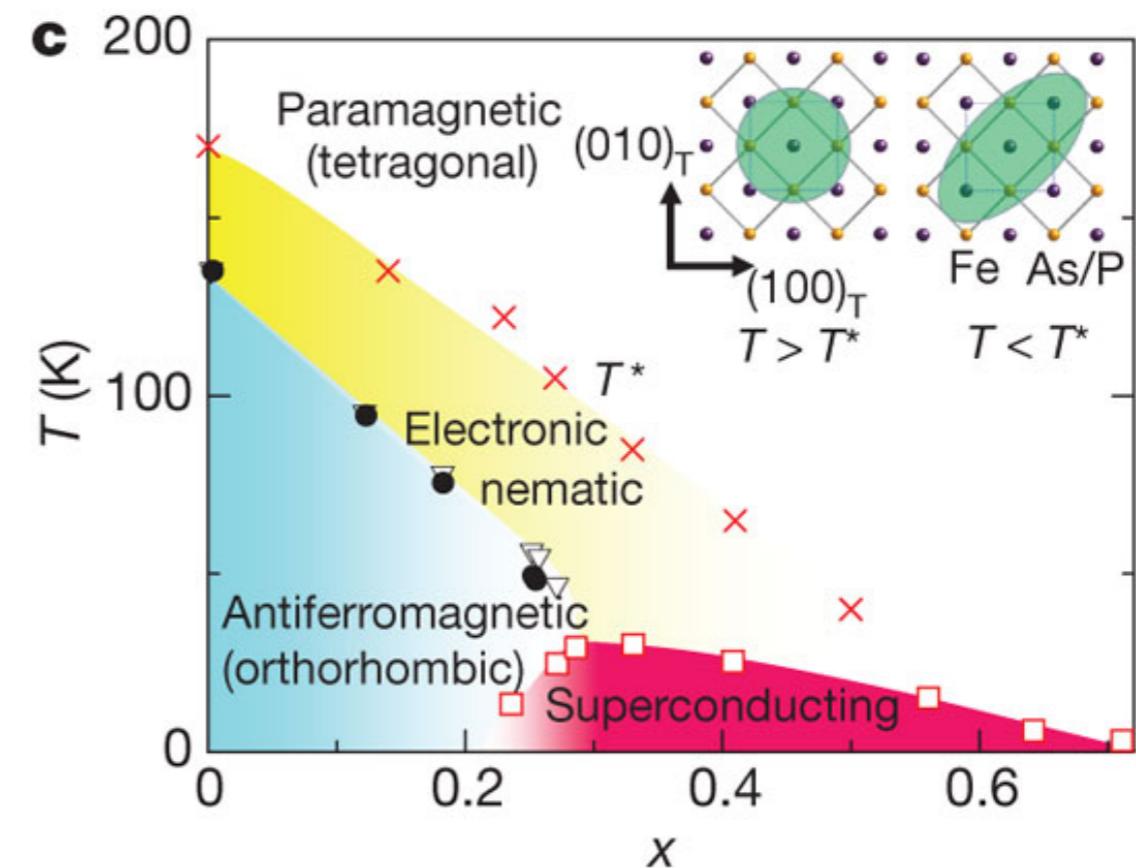


Copper-oxide vs Iron-pnictide

Copper-oxide
(d-wave)

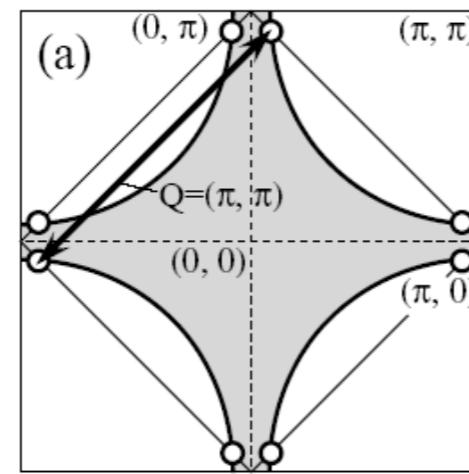
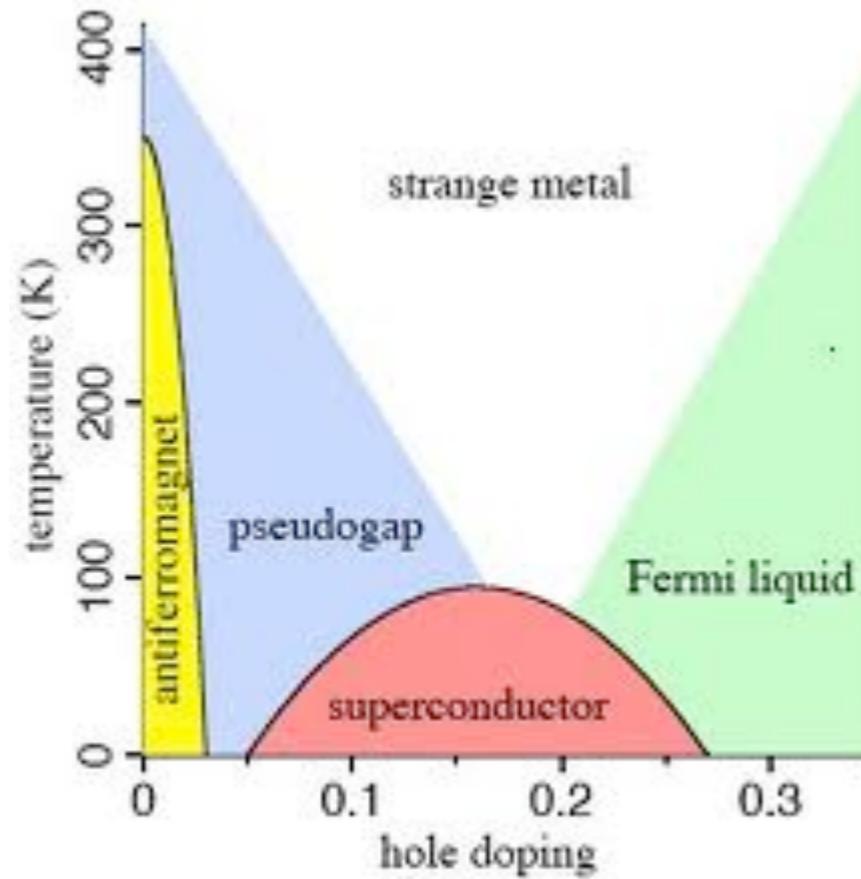


Iron-pnictide
(s±-wave?)

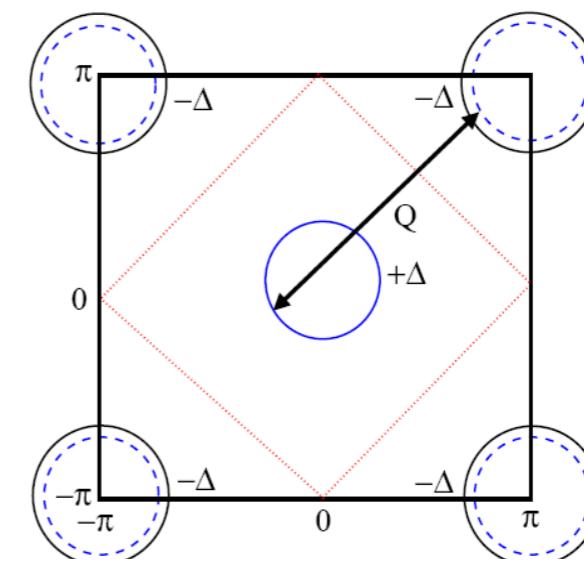
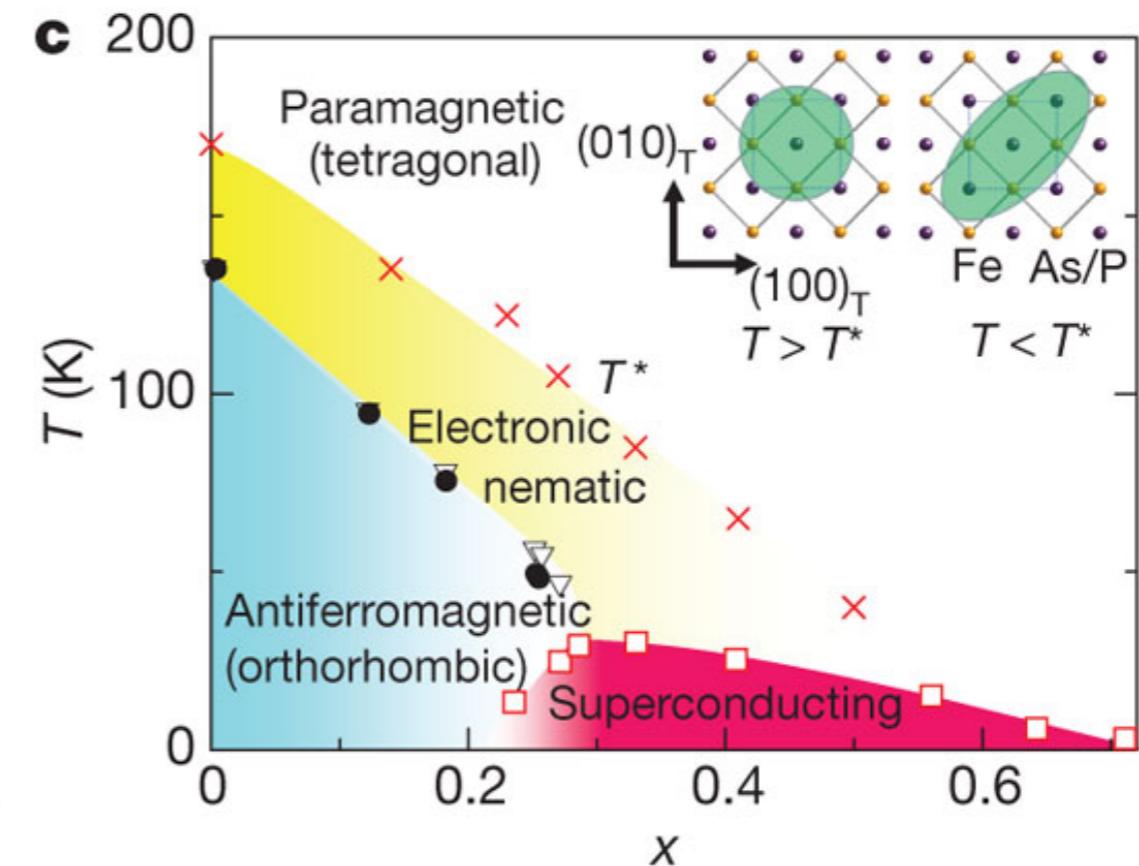


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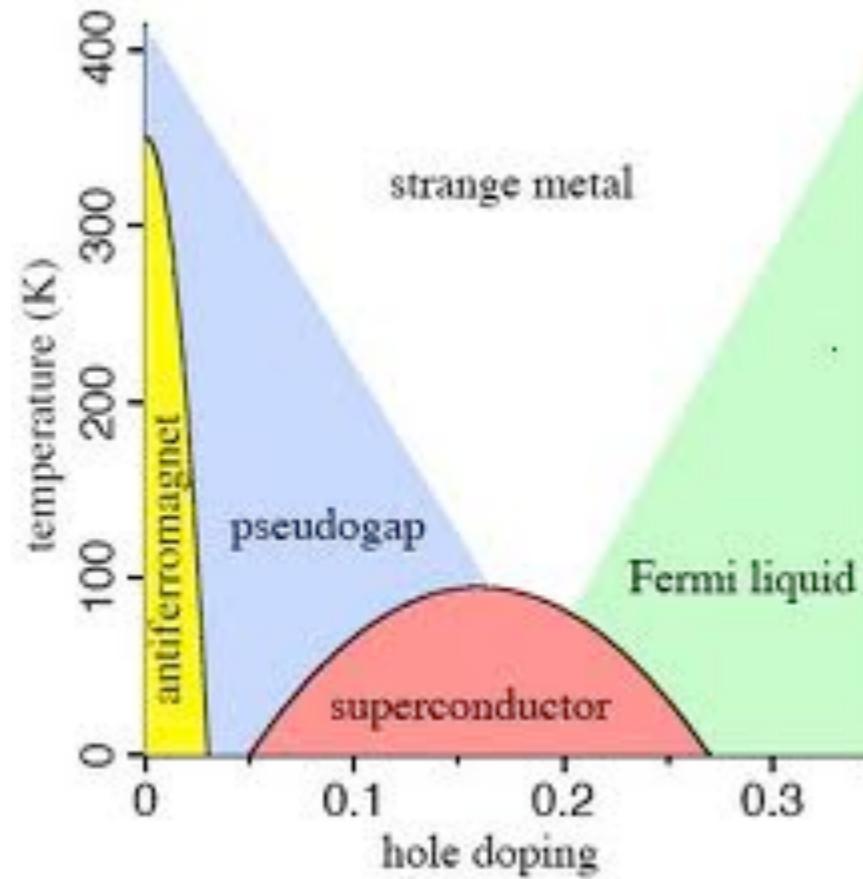


Iron-pnictide
(s±-wave?)

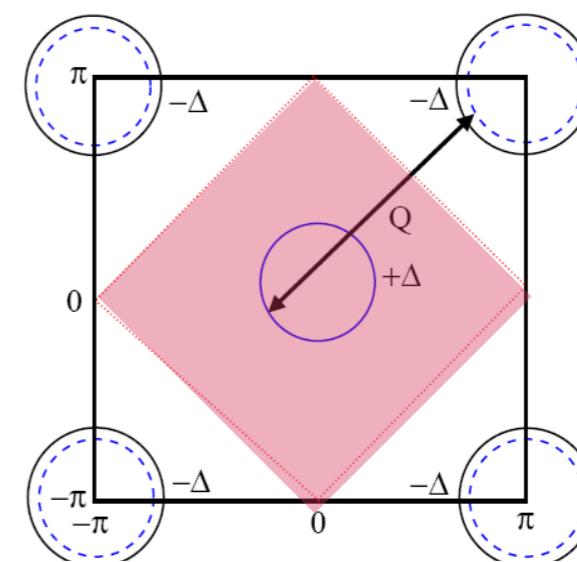
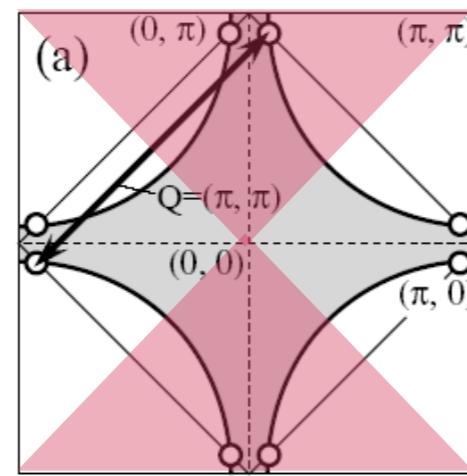
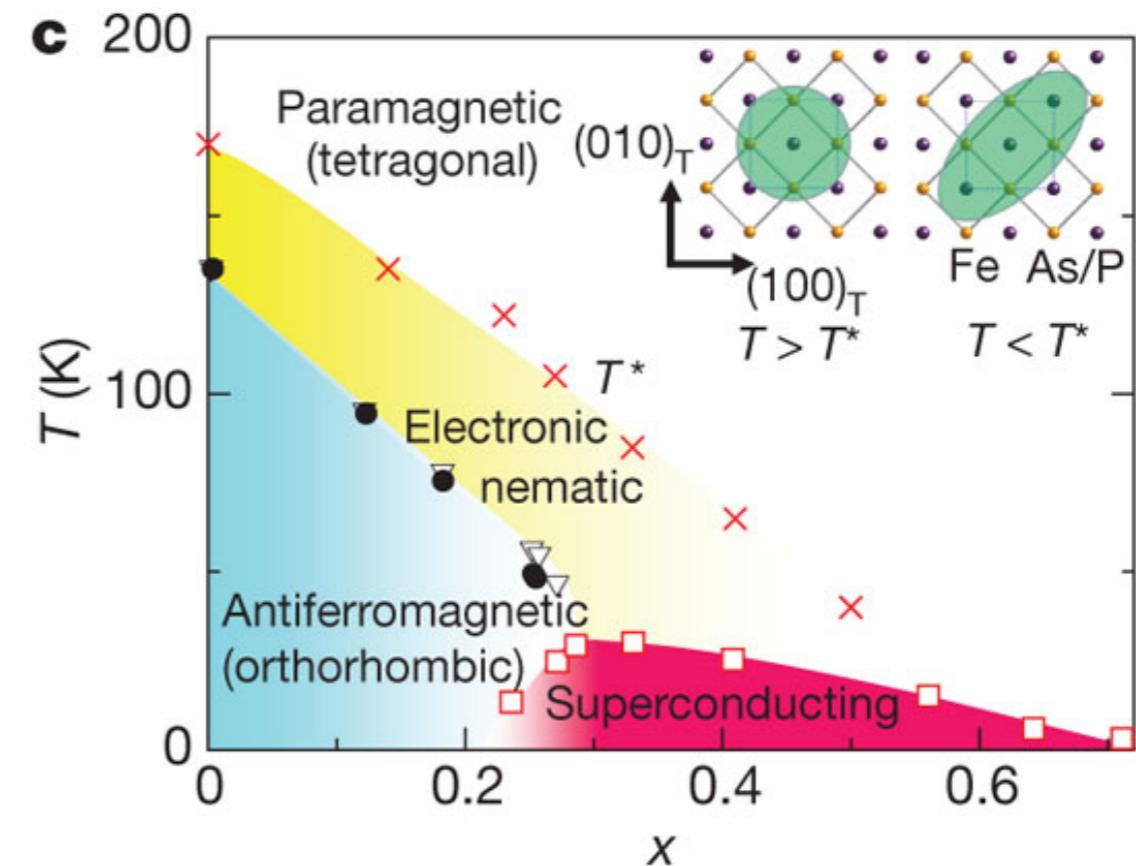


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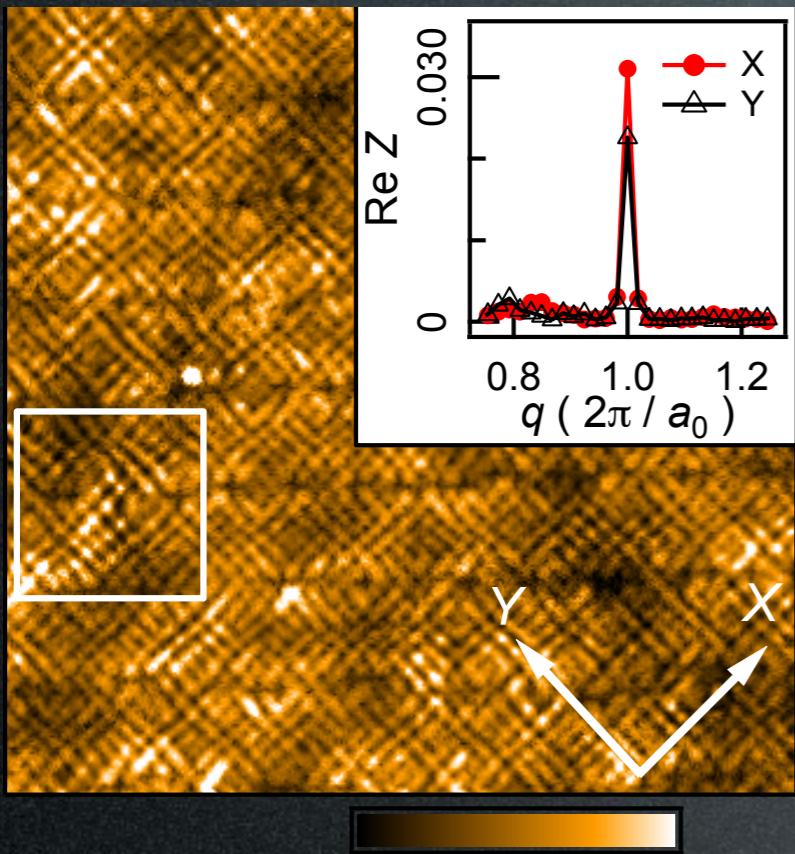
Copper-oxide
(d-wave)



Iron-pnictide
(s±-wave?)



Recent Advances in High Res. Probes



20nm x 20nm

- Y. Li "Unusual magnetic order in the pseudogap region of the superconductor HgBa₂CuO₄₊₁d"
- Nature 455 372 2008
- Jing Xia, "Polar Kerr-Effect Measurements of YBa₂Cu₃O_{6+x} Superconductor: Evidence for Broken Symmetry near the Pseudogap Temperature"
- PRL 100 127002 2008
- M. J. Lawler "Intra-unit-cell electronic nematicity of the high-Tc copper-oxide pseudogap states"
- Nature 466 347 2010
- R. Daou "Broken rotational symmetry in the pseudogap phase of a high-Tc superconductor"
- Nature 463 519 2010
- S. De Almeida-Didry Evidence for intra-unit-cell magnetic order in Bi₂Sr₂CaCu₂O₈
PHYSICAL REVIEW B 86 020504(R) 2012
- Tao Wu, "Magnetic-field-induced charge-stripe order in the high-temperature superconductor YBa₂Cu₃O_y"
- Nature 477 191 2011
- G. Ghiringhelli, "Long-Range Incommensurate Charge Fluctuations in (Y,Nd)Ba₂Cu₃O_{6+x}"
- Science 337 821 2012
- J. Chang, "Direct observation of competition between superconductivity and charge density wave order in YBa₂Cu₃O_{6.67}"
- Nature Physics 8 871 2012

Recent Advances in Theory

Recent Advances in Theory

- New numerical approaches:
Functional Renormalization Group

Recent Advances in Theory

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Functional Renormalization Group
- A handle on order parameter symmetry
: Weak coupling RG for superconductivity
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Recent Advances in Theory

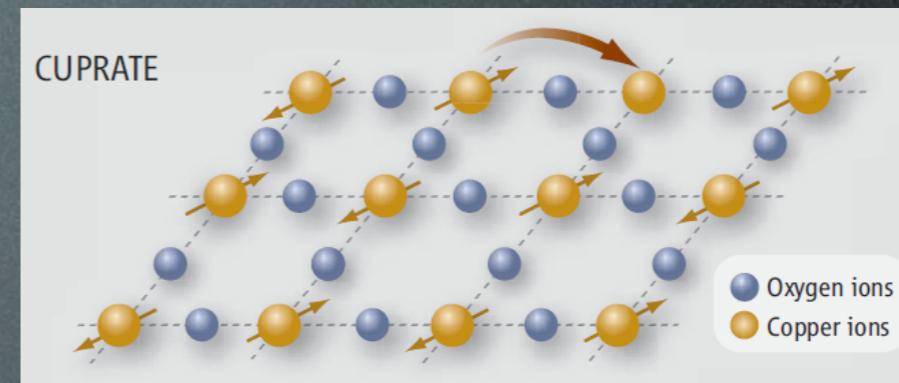
- New numerical approaches:
Functional Renormalization Group
- A handle on order parameter symmetry
: Weak coupling RG for superconductivity
driven by purely repulsive interaction
- A new perspective of intertwined order
- Insight into the minimal model:
the role of oxygen sites

Recent Advances in Theory

A Middle-Up/Down Approach

Recent Advances in Theory

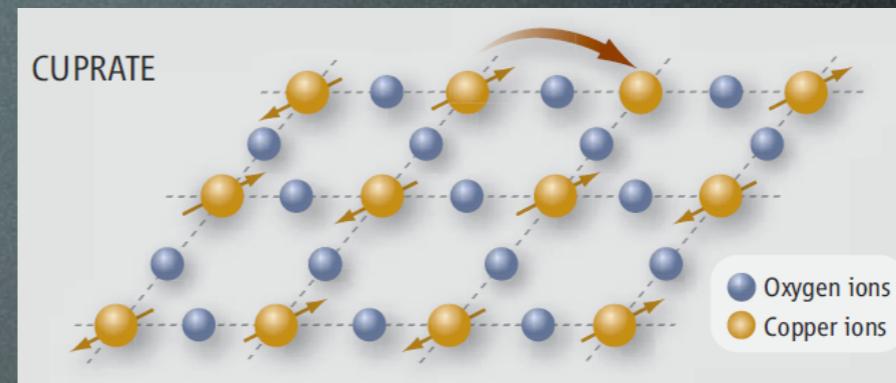
Top-down:



A Middle-Up/Down Approach

Recent Advances in Theory

Top-down:



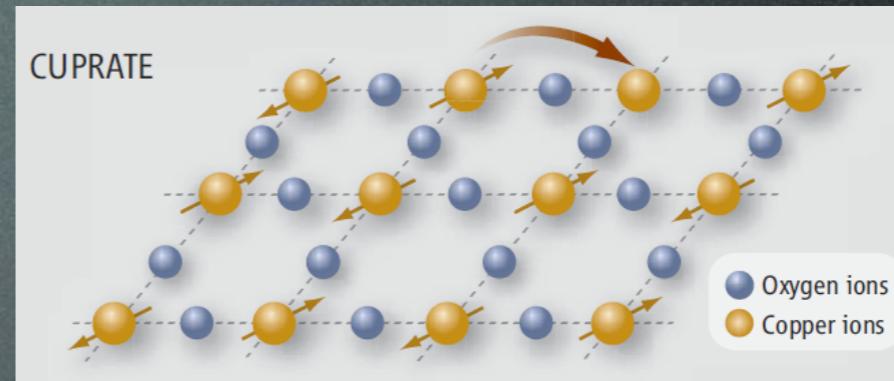
Bottom-up:



A Middle-Up/Down Approach

Recent Advances in Theory

Top-down:



Middle-down/up:

Symmetry Principles

Bottom-up:

Neutron
Scattering



STM

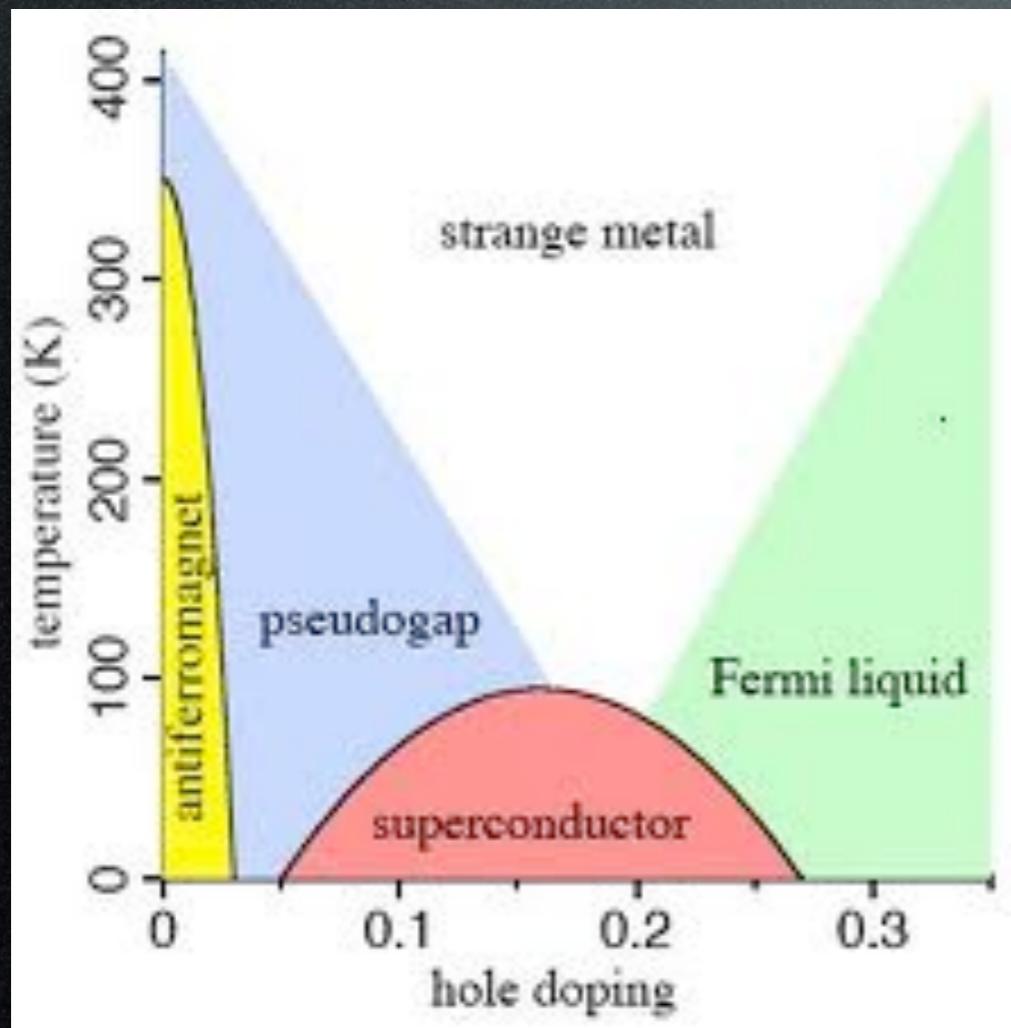


ARPES

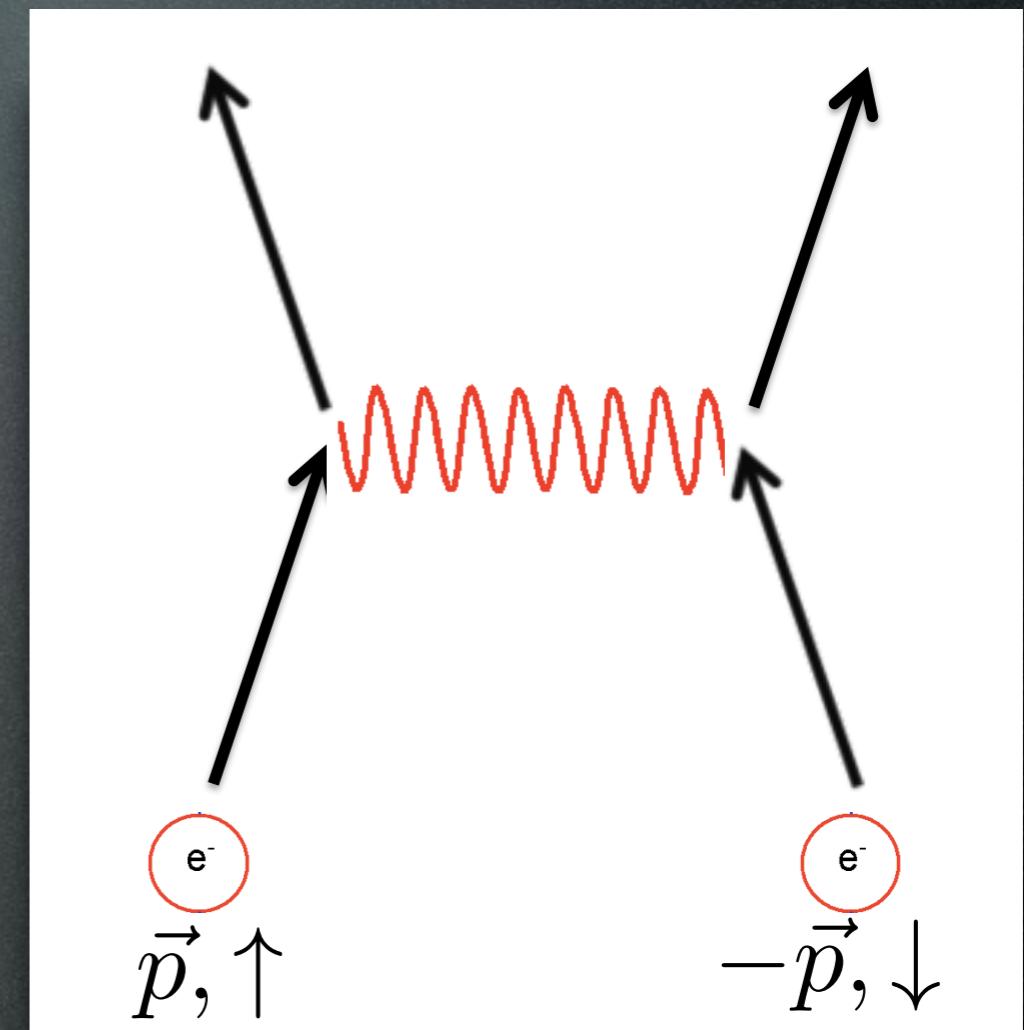
A Middle-Up/Down Approach

Key Questions in High- T_c Superconductivity:

The Phase Diagram?

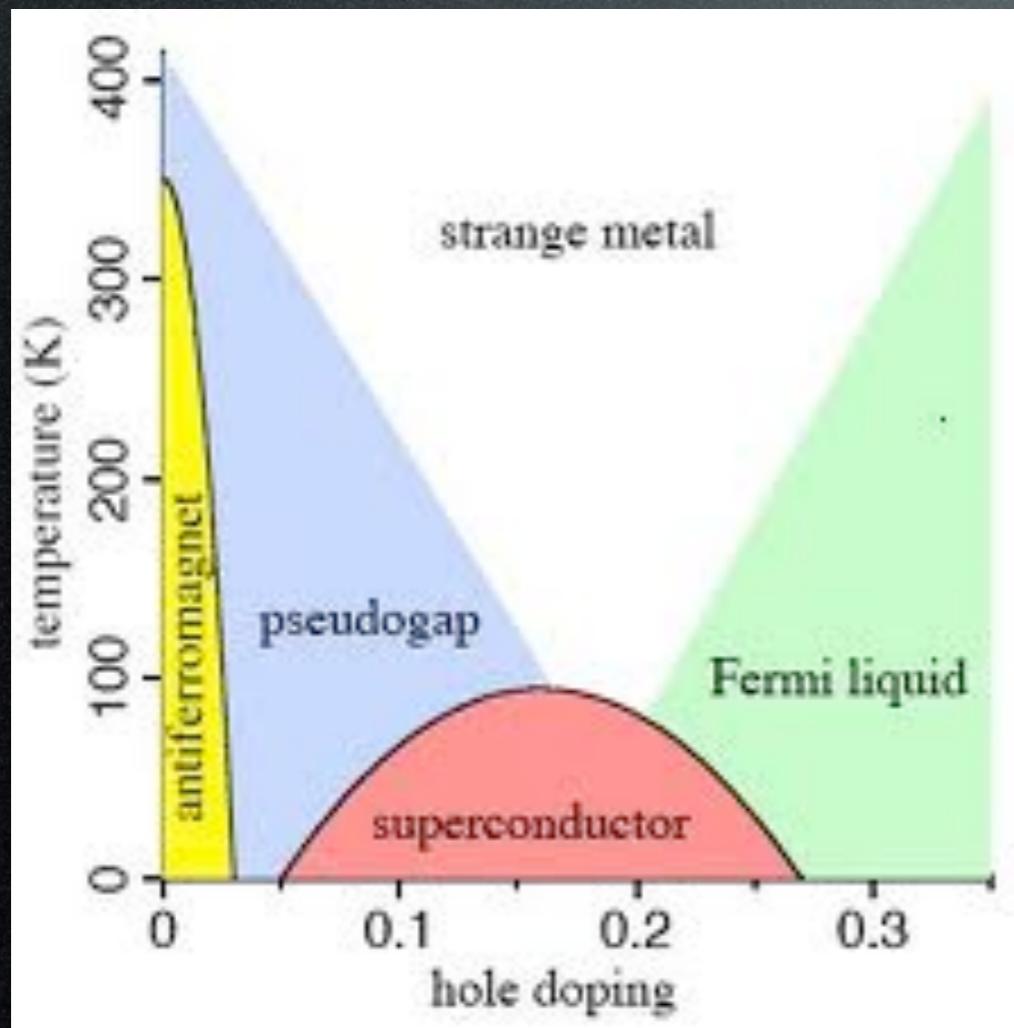


The Mechanism?

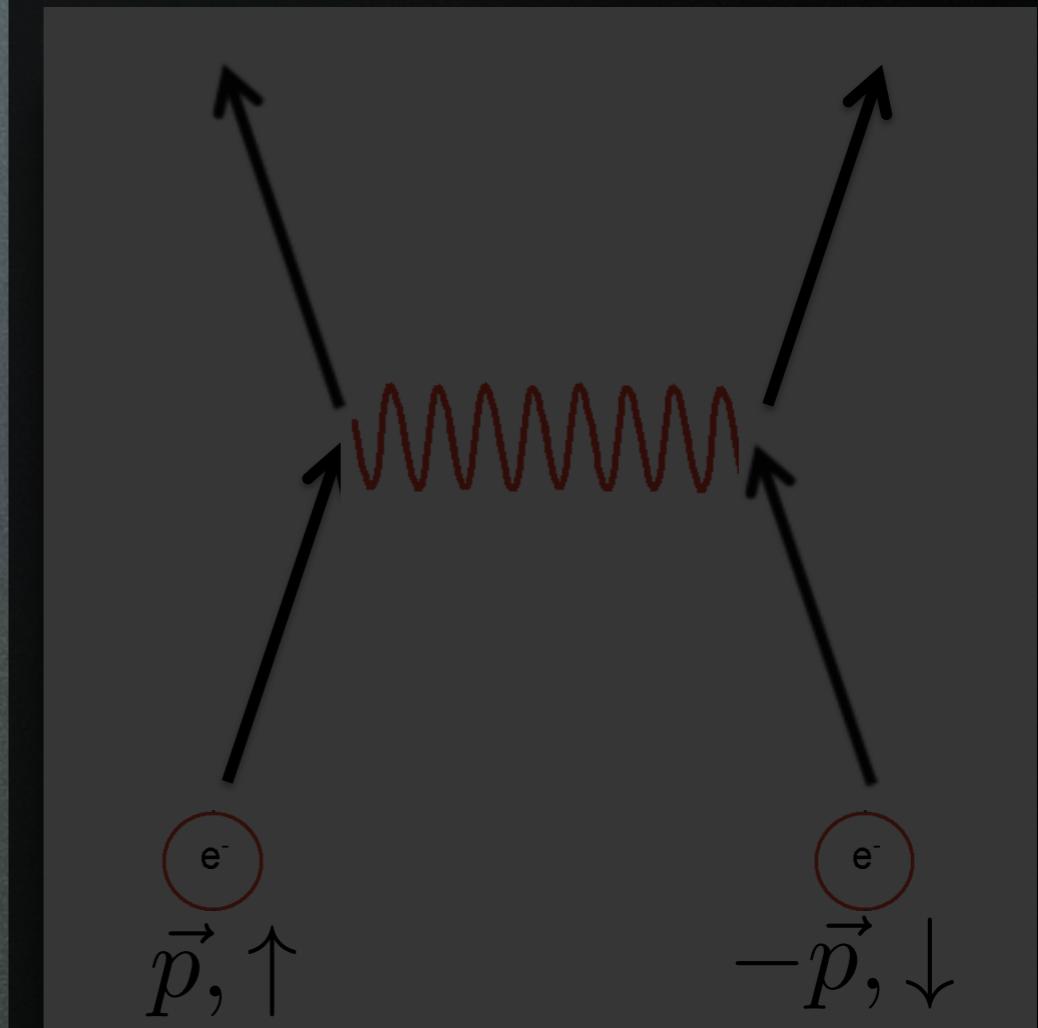


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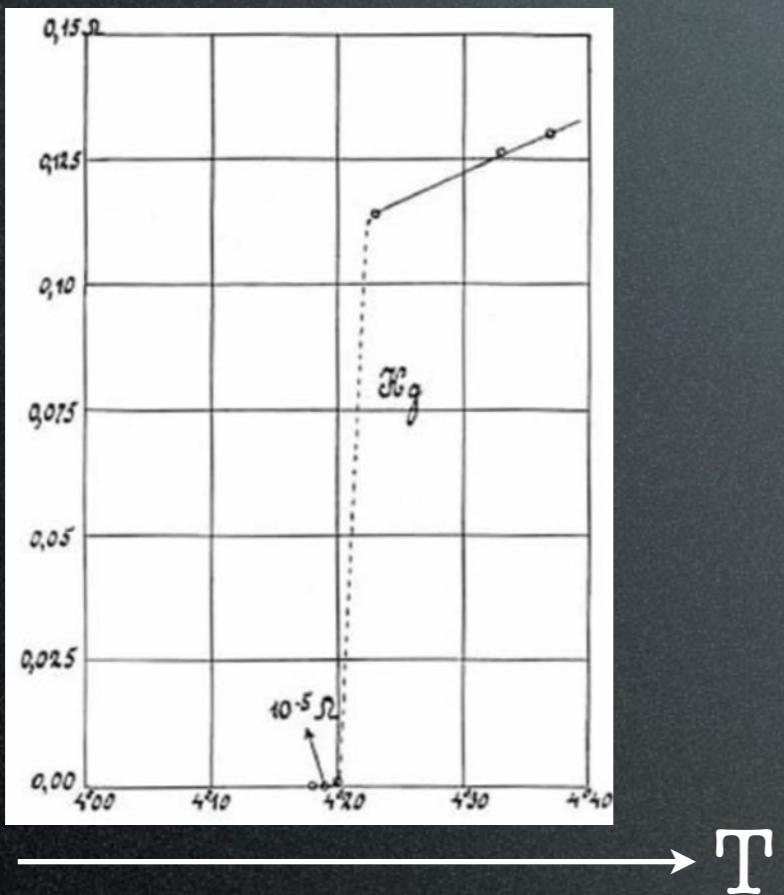


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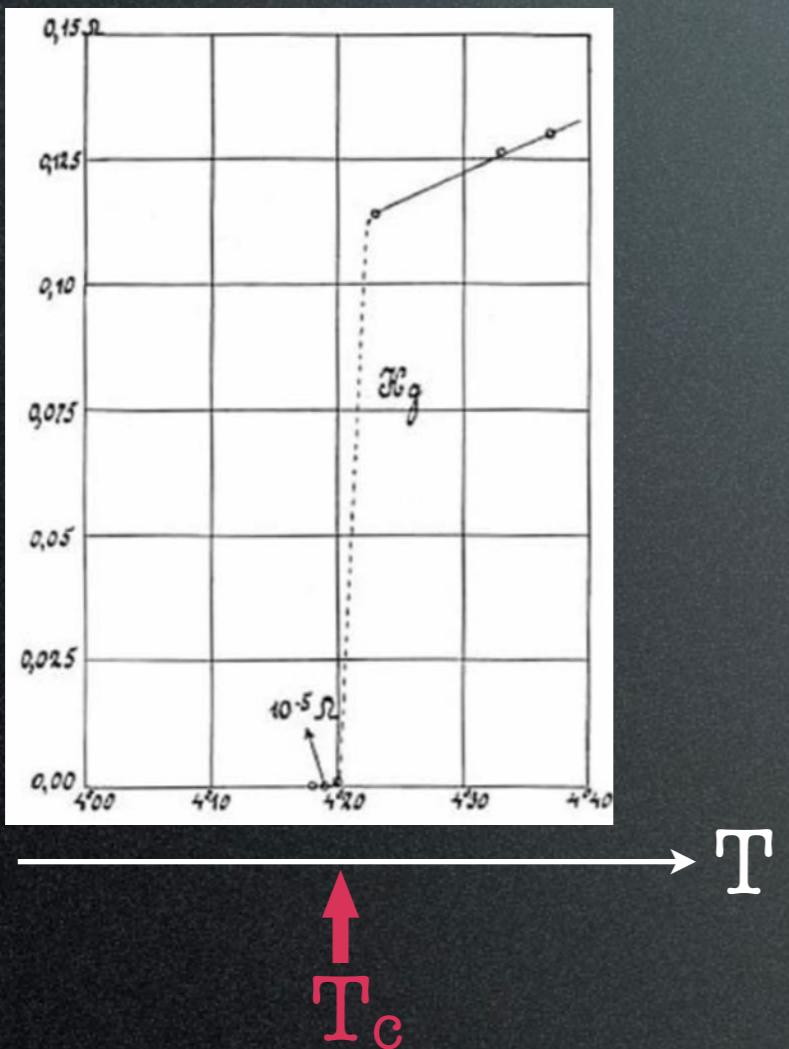
The Complex Phase Diagram

Simple PD of
conventional SC



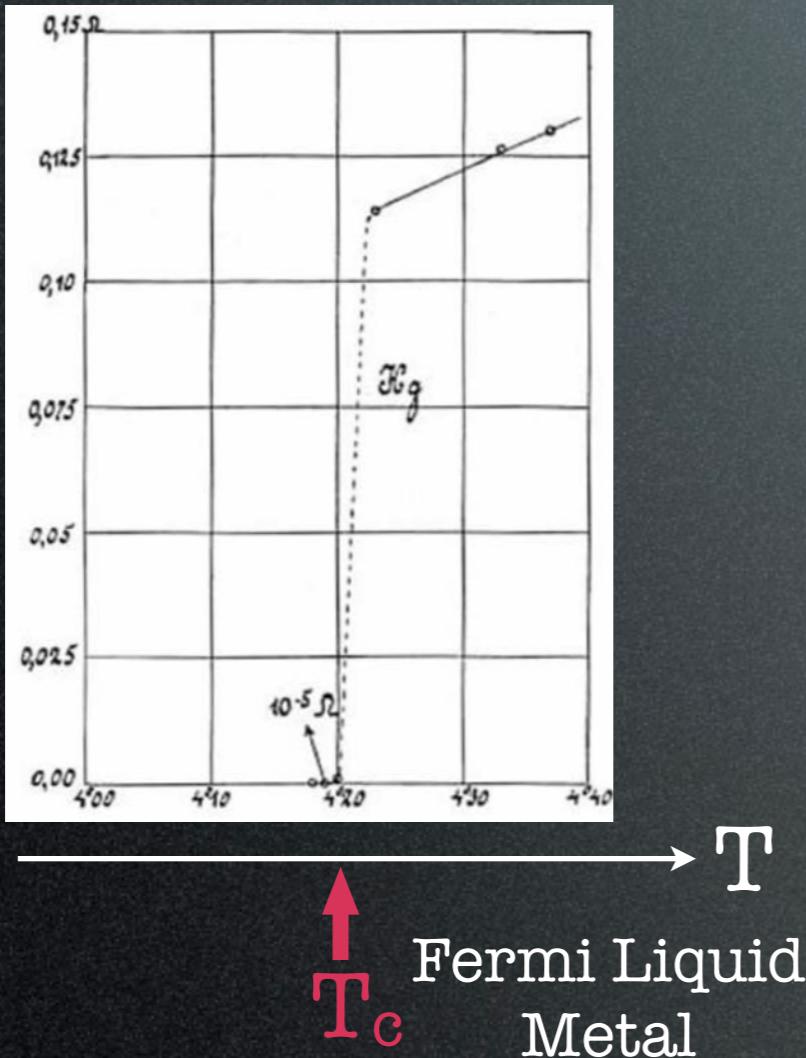
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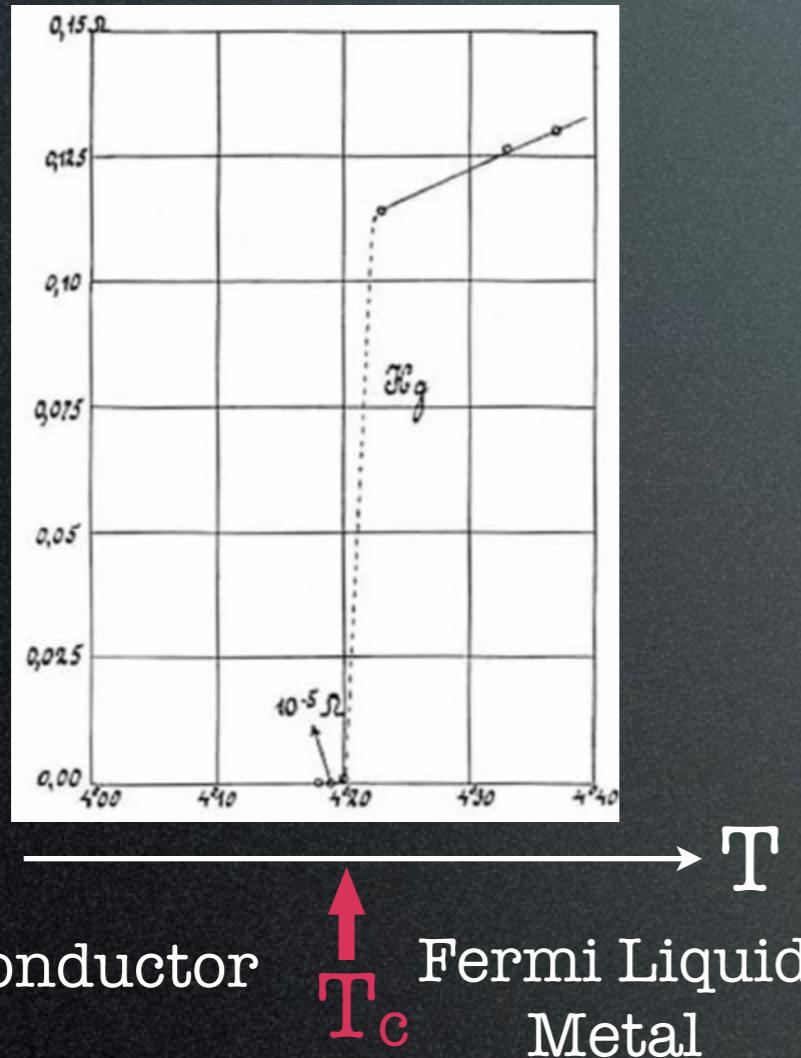
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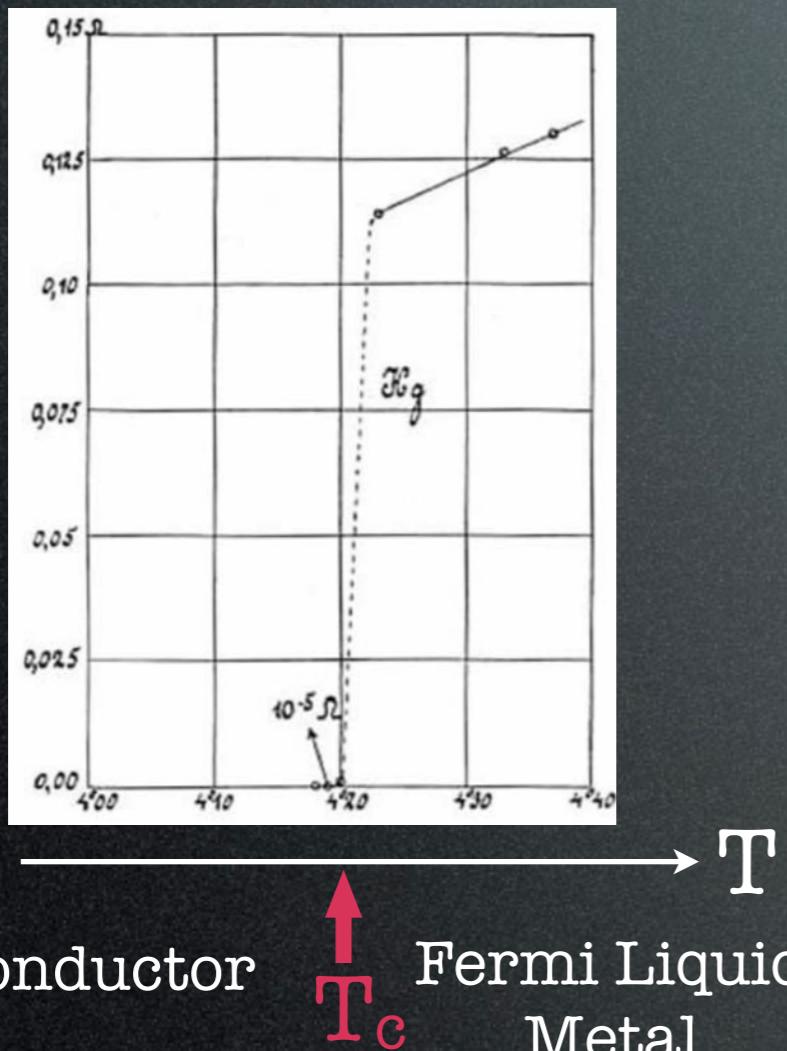
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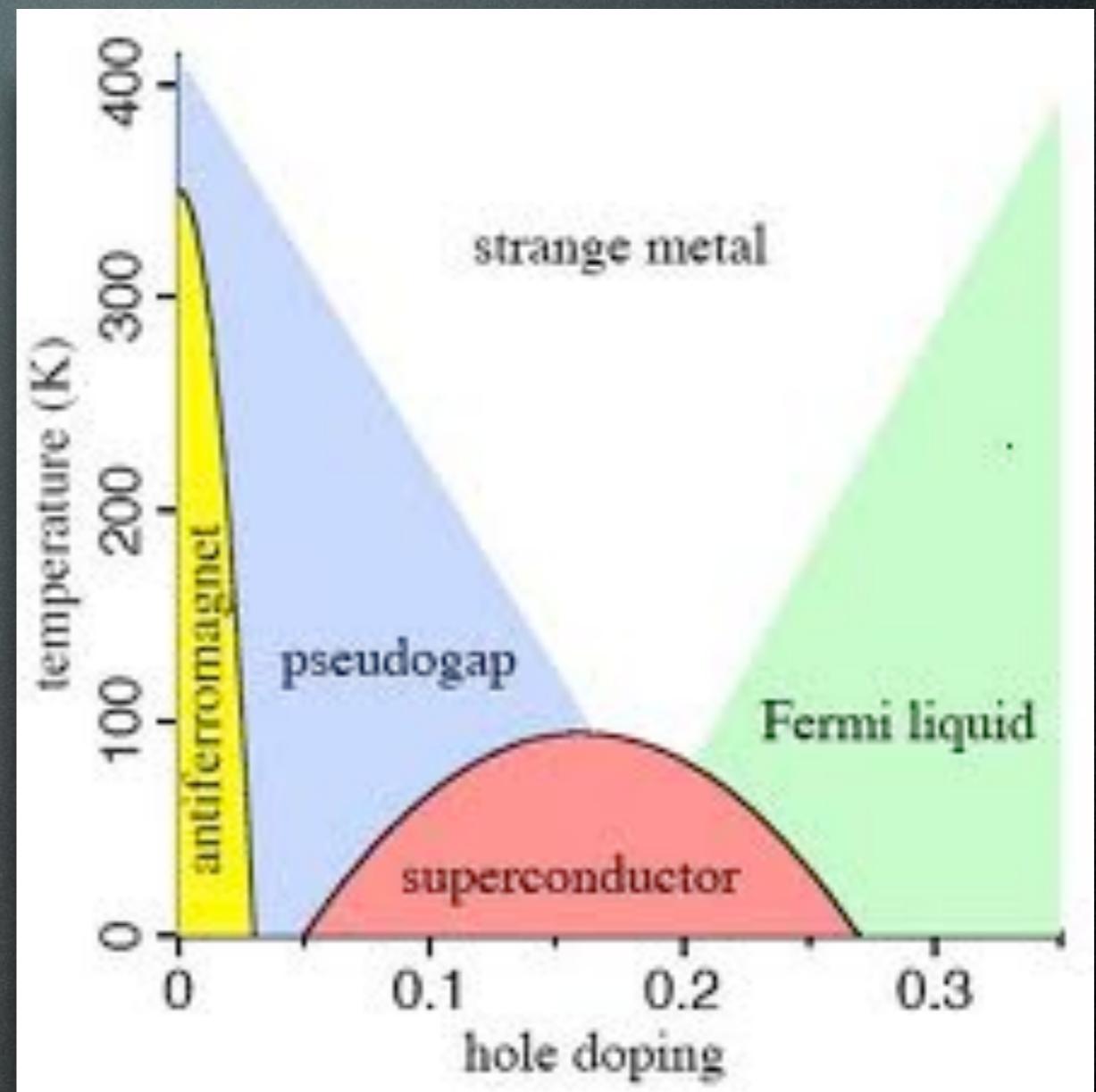


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Simple PD of conventional SC

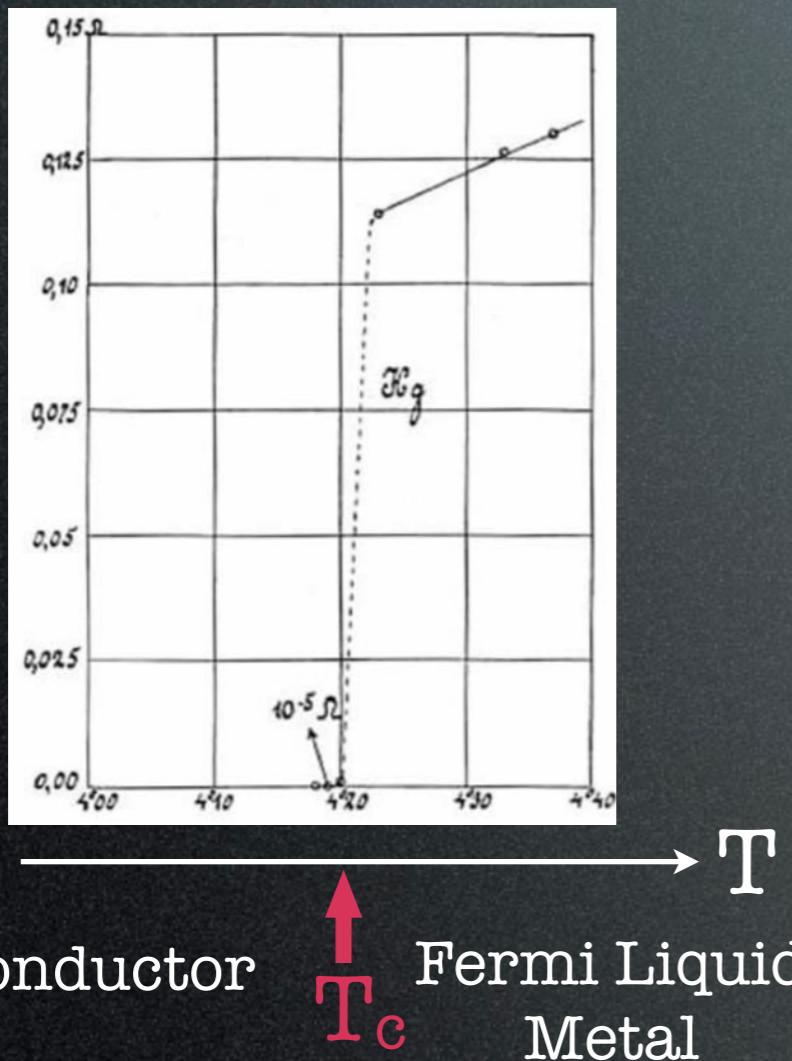


Complex PD of high T_c SC

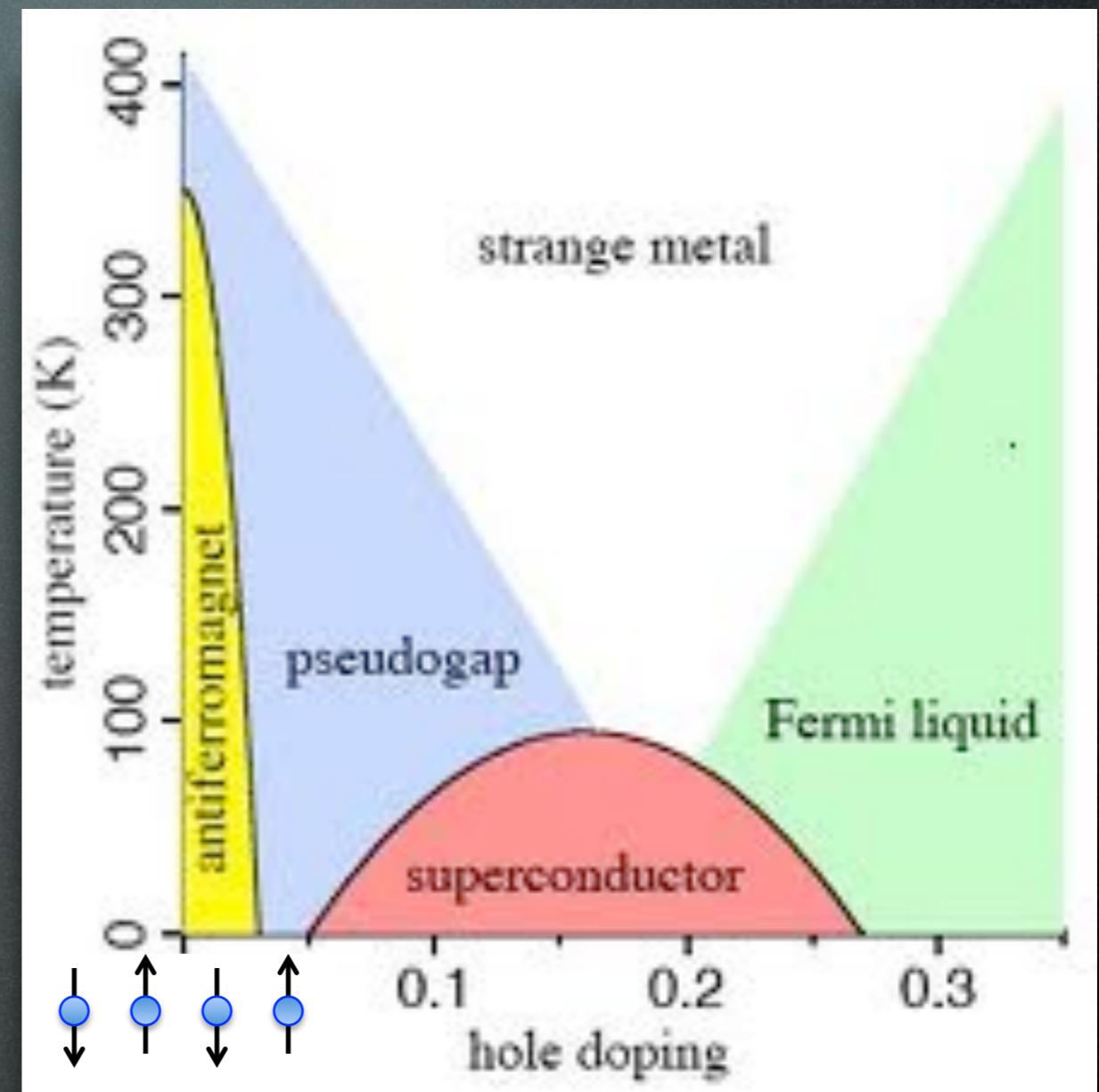


The Complex Phase Diagram

Simple PD of conventional SC

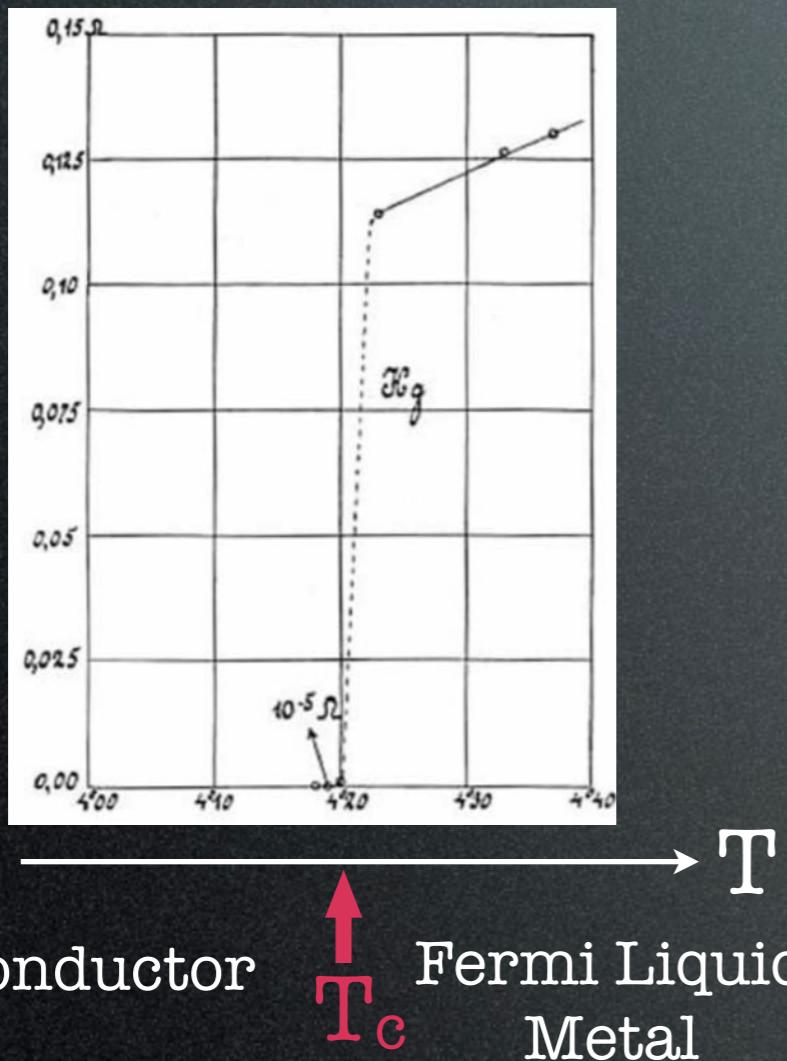


Complex PD of high T_c SC

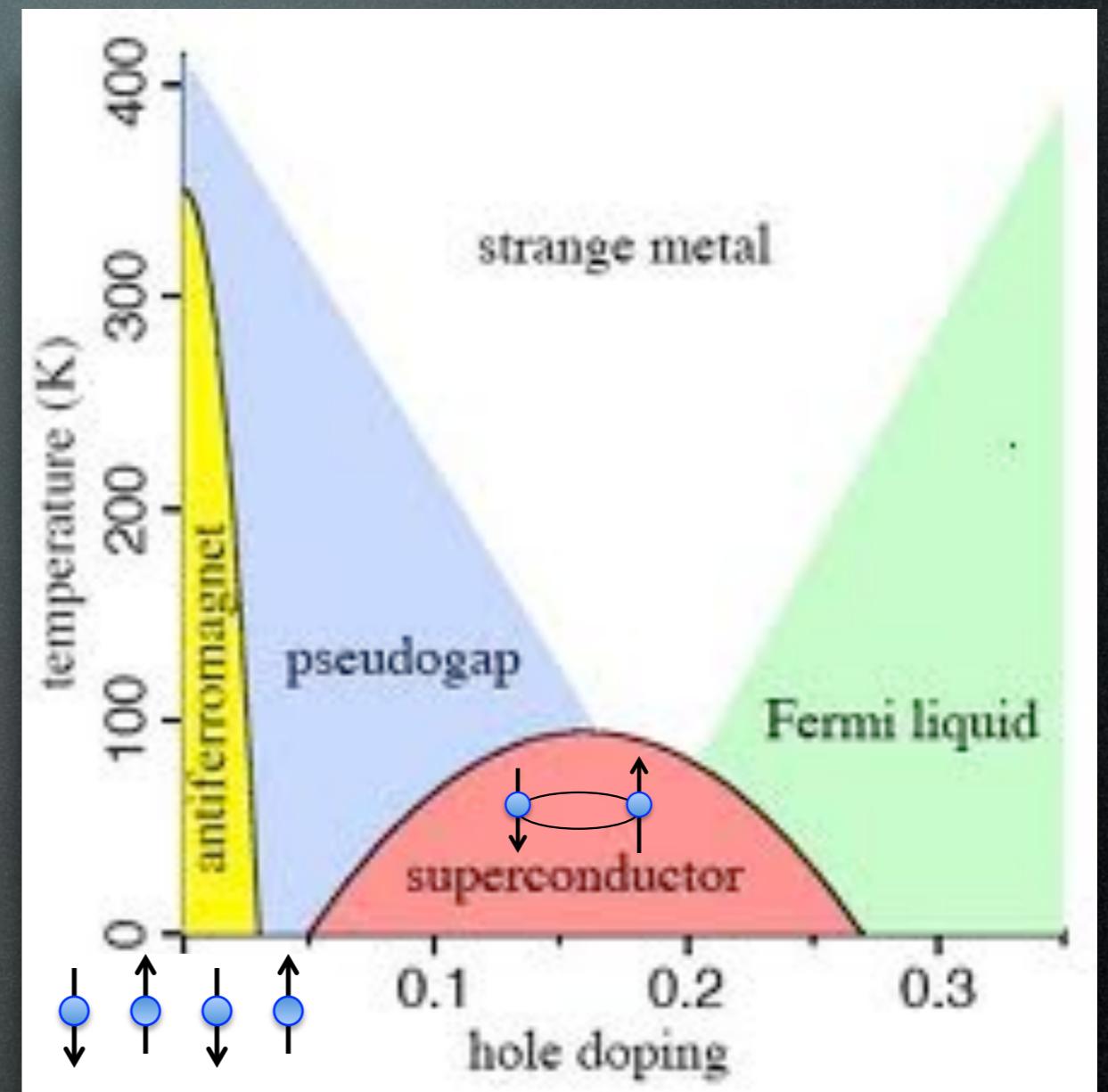


The Complex Phase Diagram

Simple PD of conventional SC

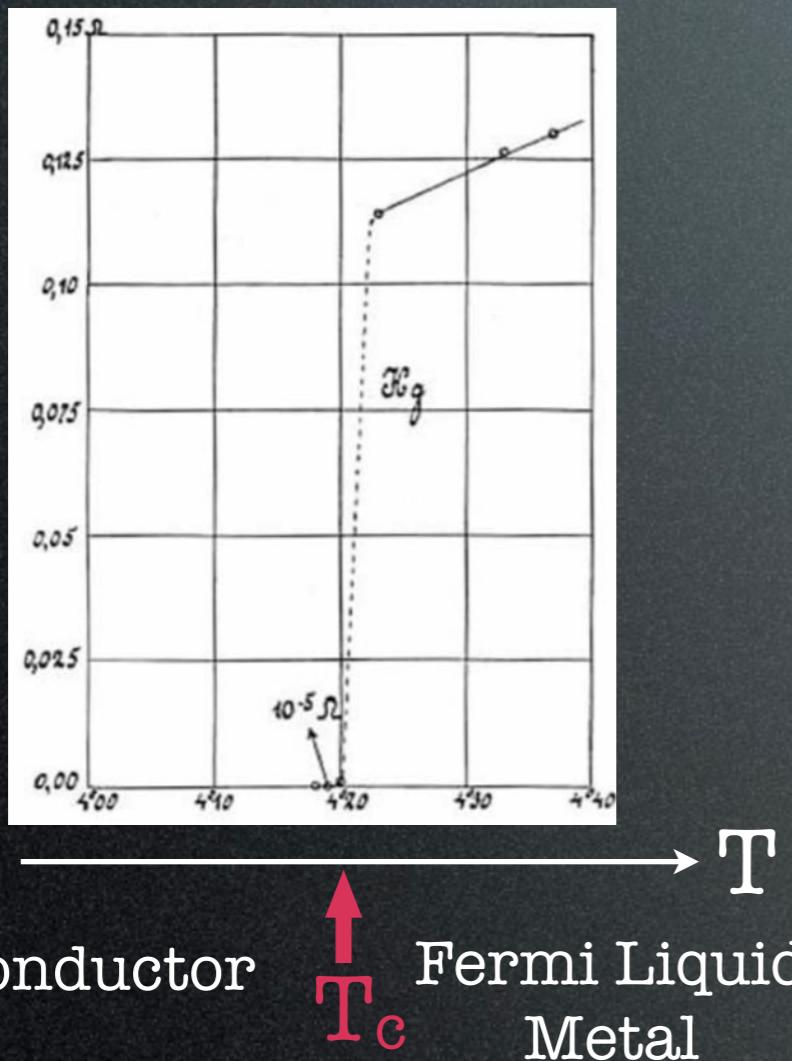


Complex PD of high T_c SC

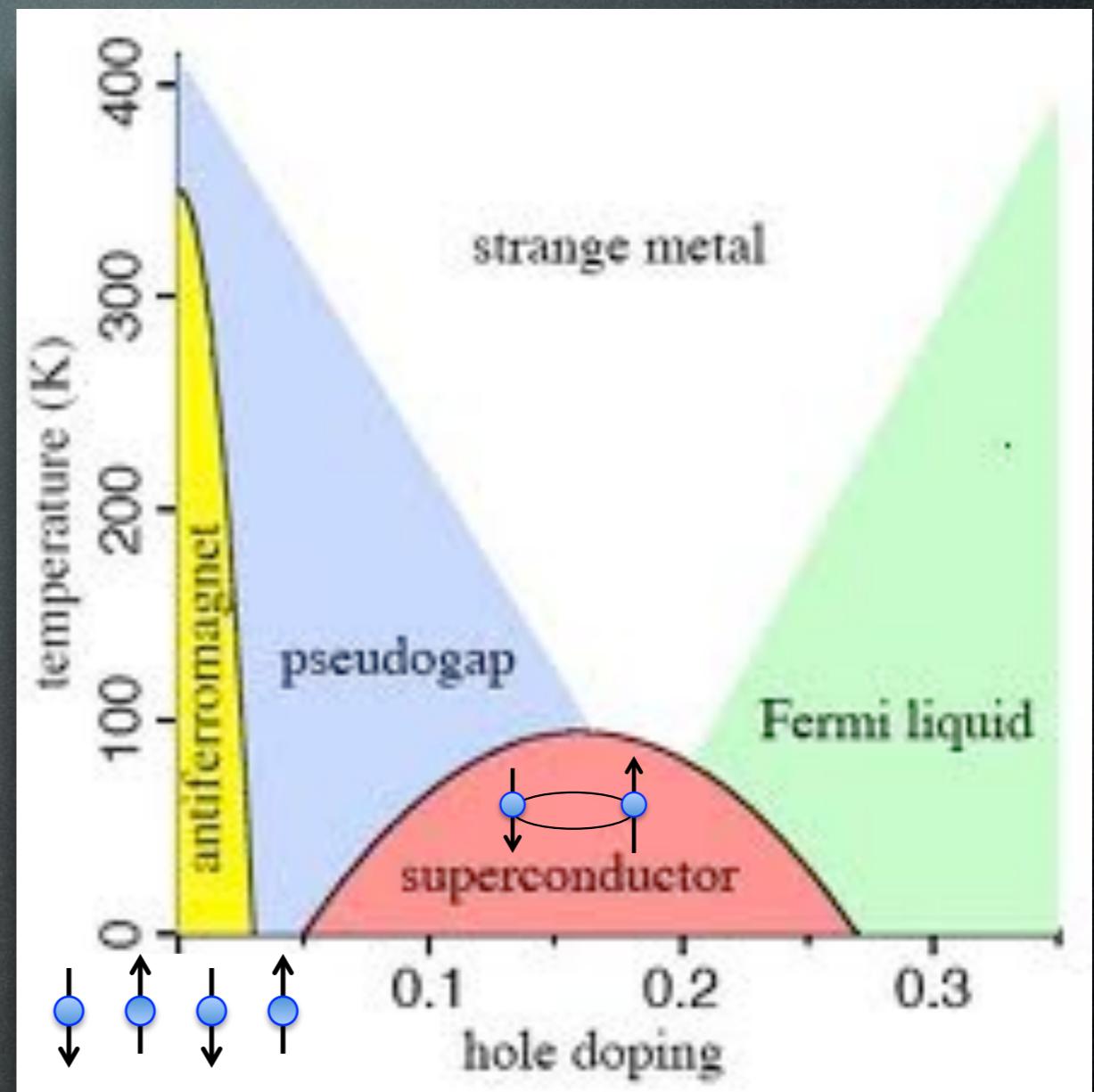


The Complex Phase Diagram

Simple PD of conventional SC



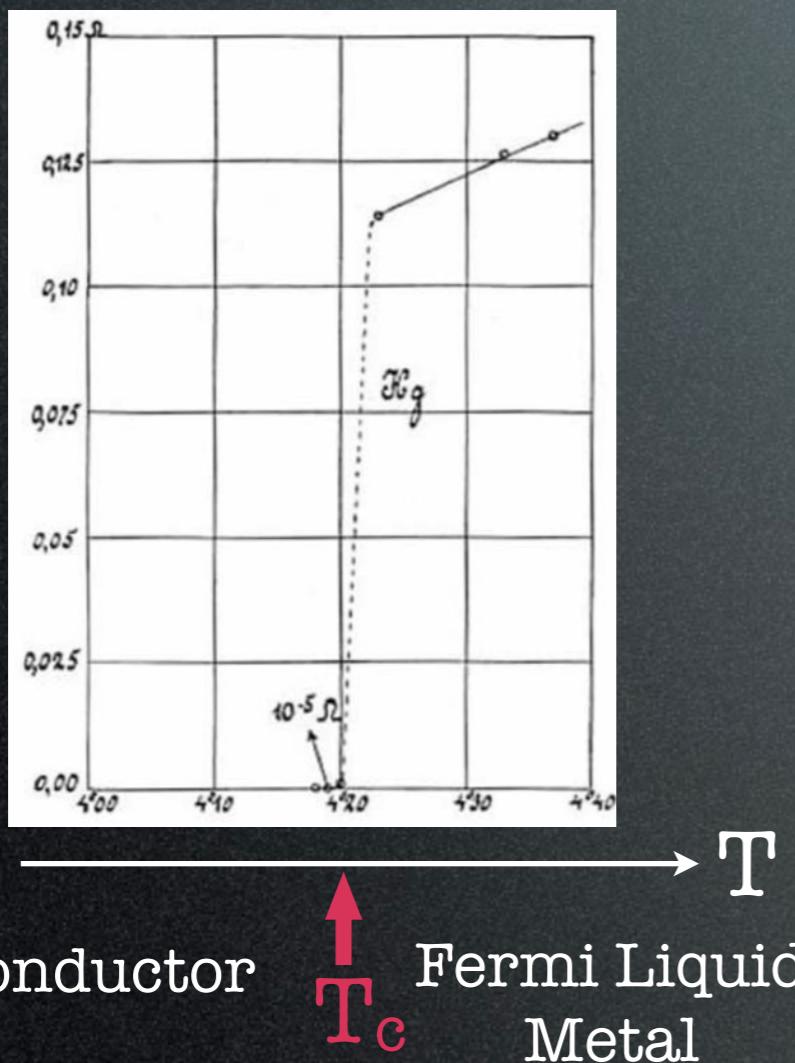
Complex PD of high T_c SC



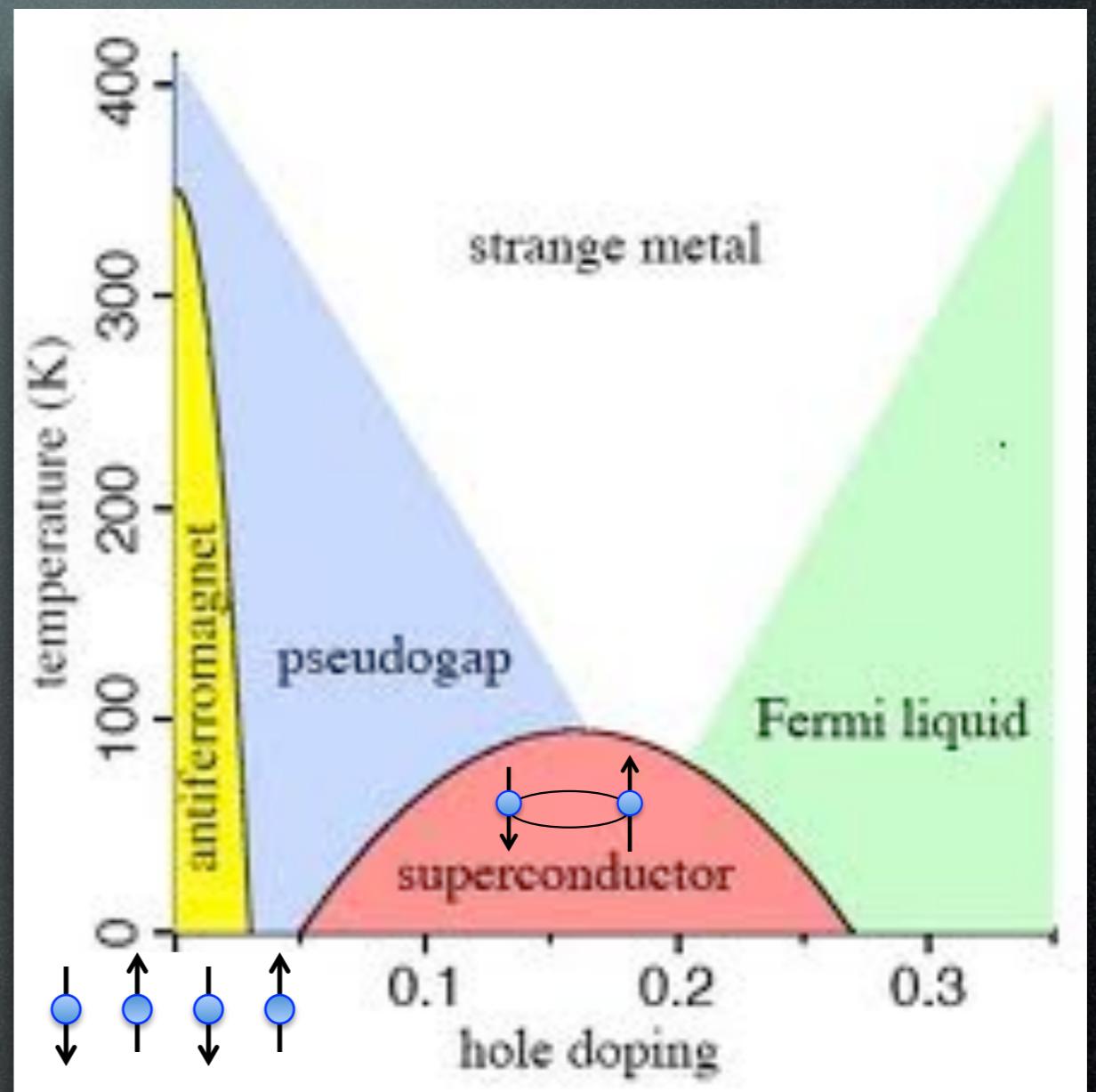
- Phases in between FL & MI

The Complex Phase Diagram

Simple PD of conventional SC



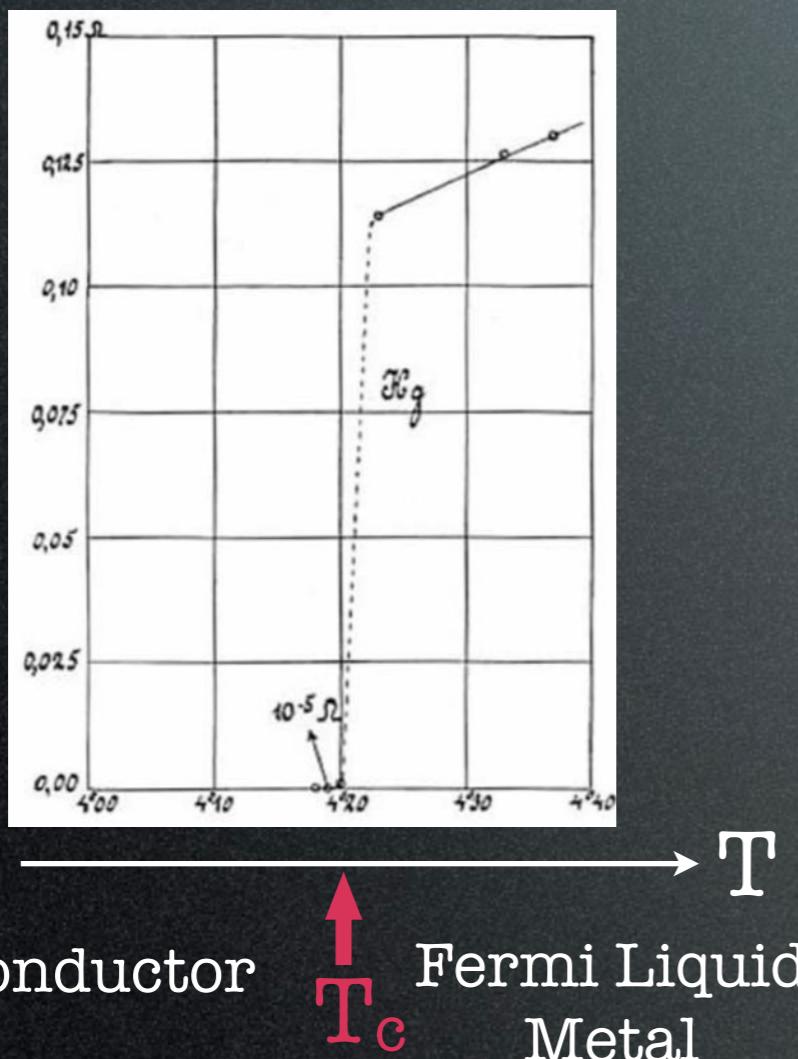
Complex PD of high T_c SC



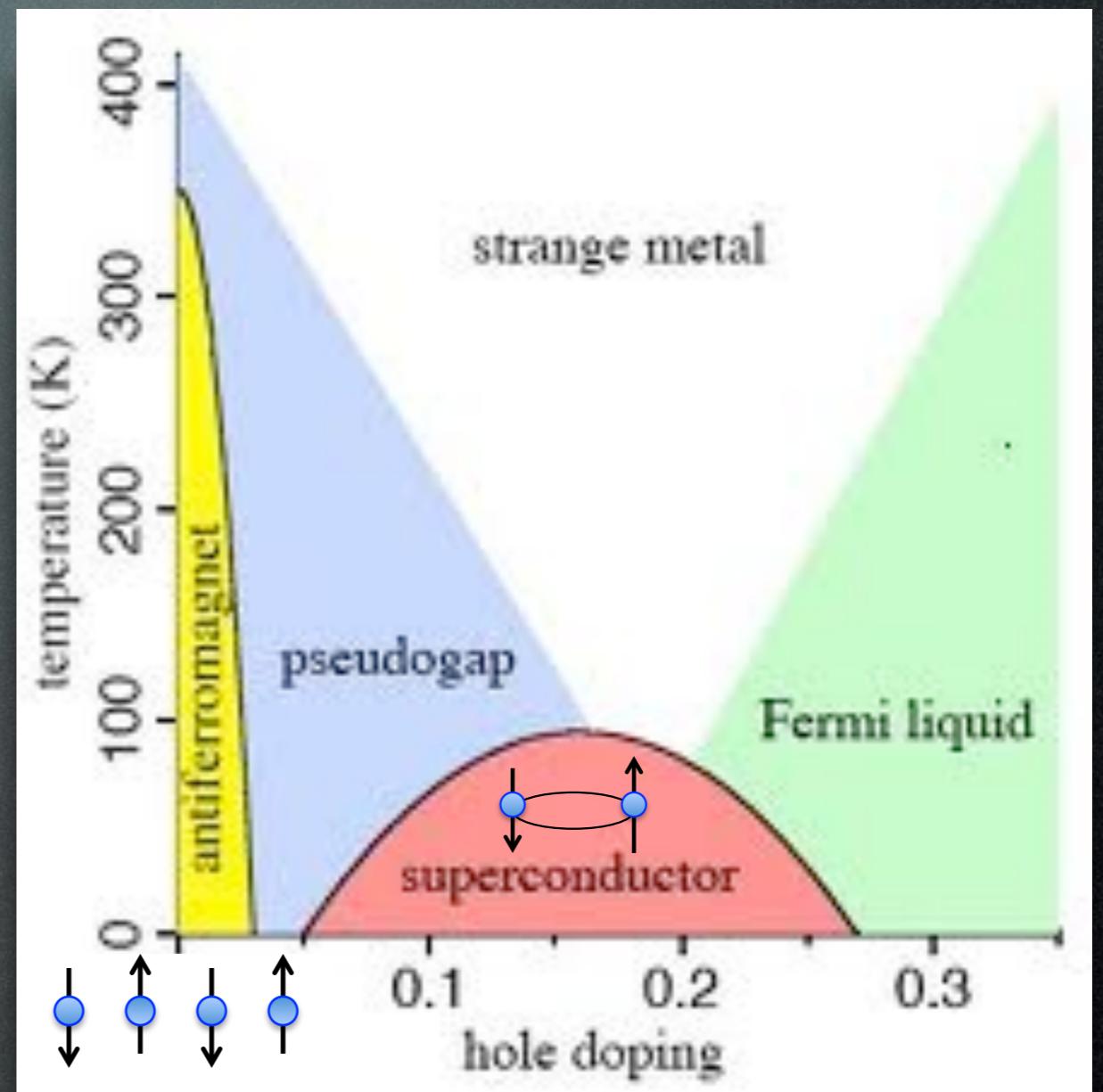
- Phases in between FL & MI
- Multiple “phases” at similar T

The Complex Phase Diagram

Simple PD of conventional SC



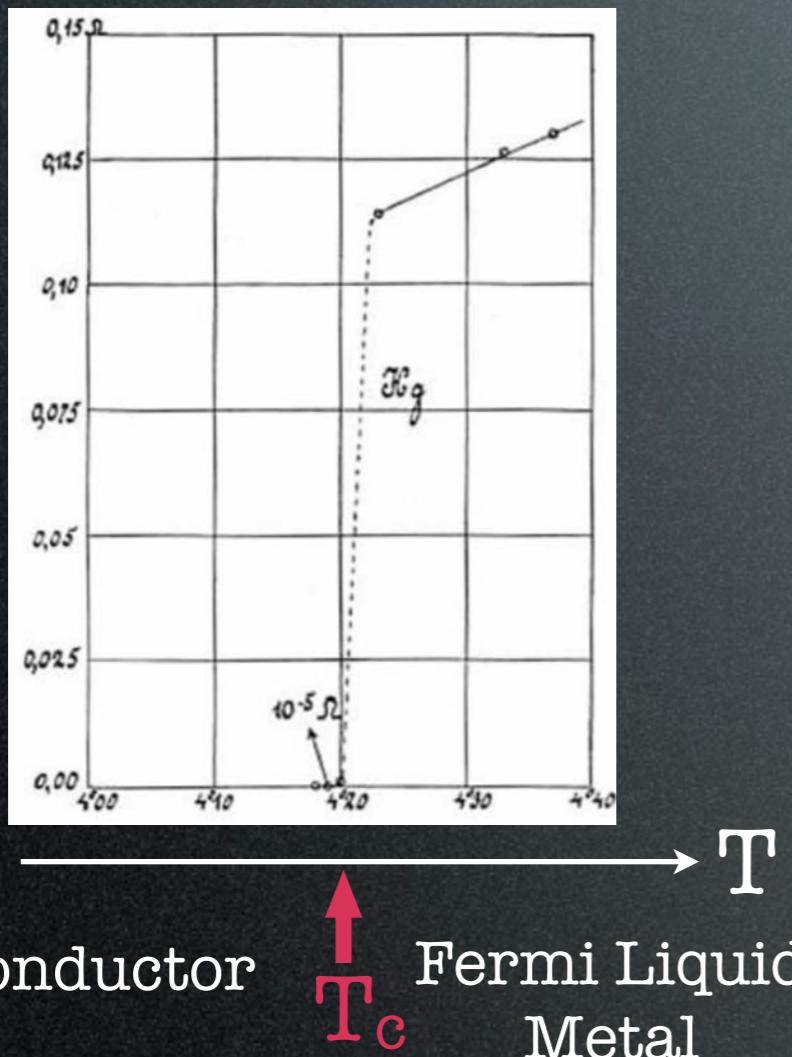
Complex PD of high T_c SC



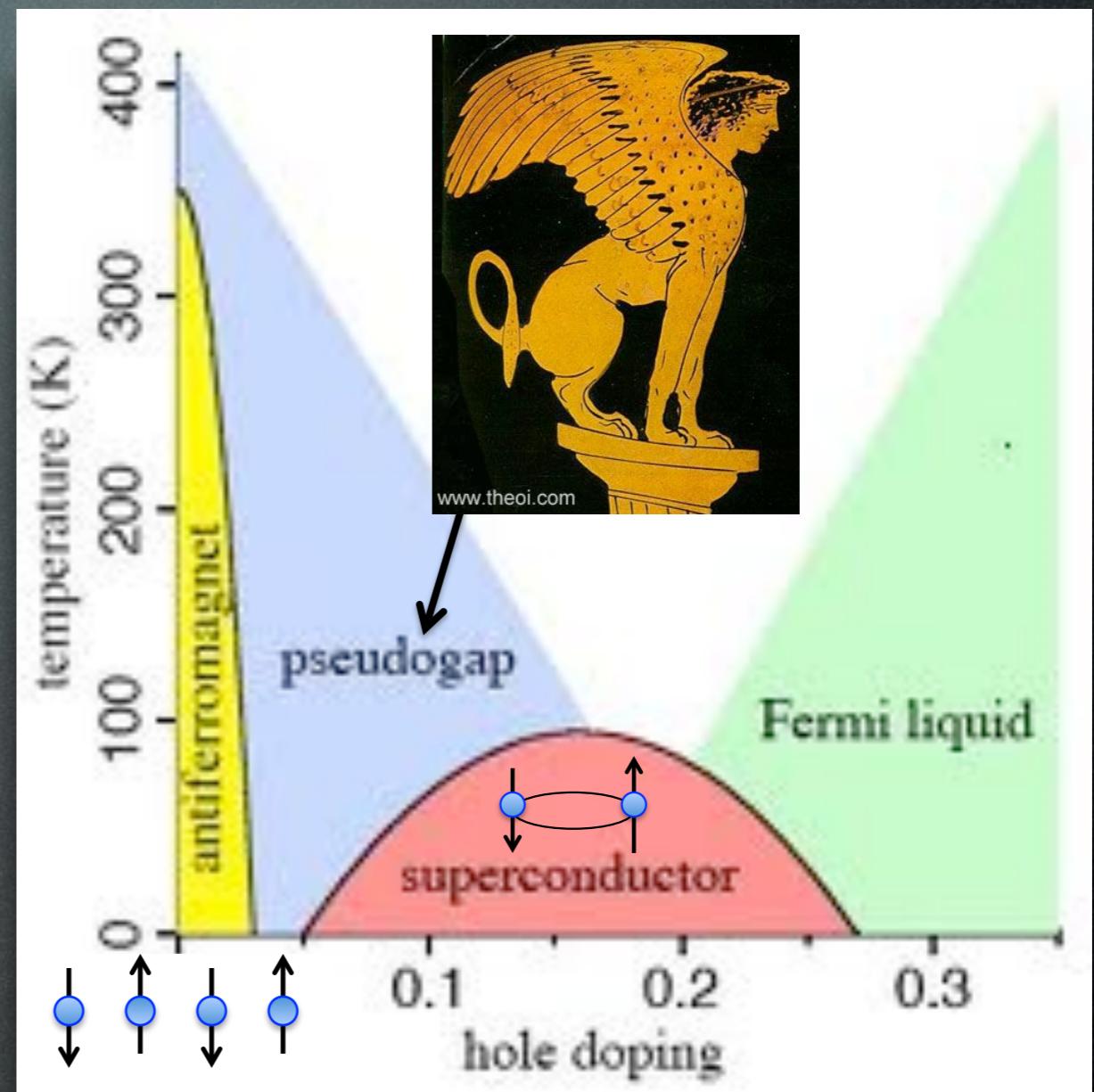
- Phases in between FL & MI
- Multiple “phases” at similar T
- Unidentifiable regions

The Complex Phase Diagram

Simple PD of conventional SC

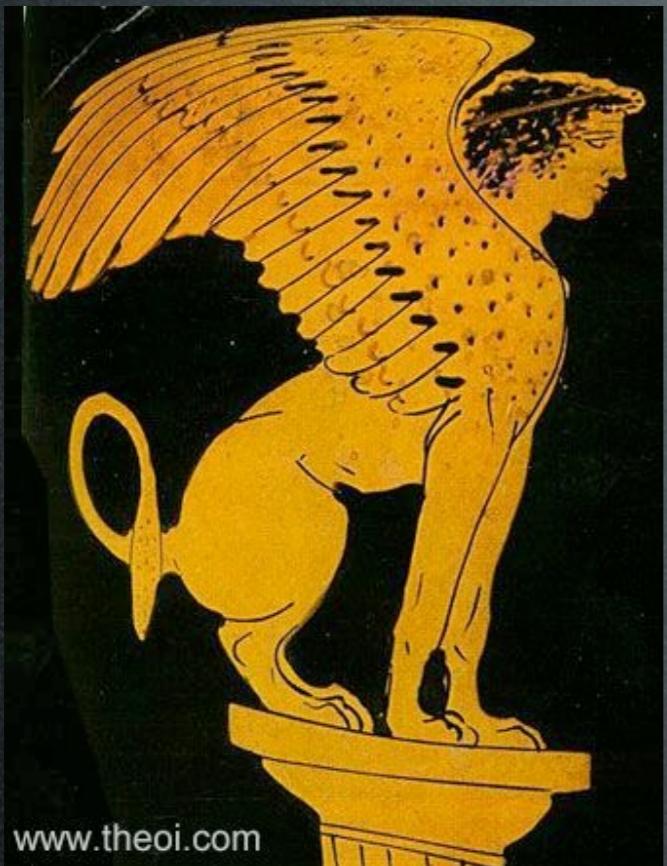


Complex PD of high T_c SC



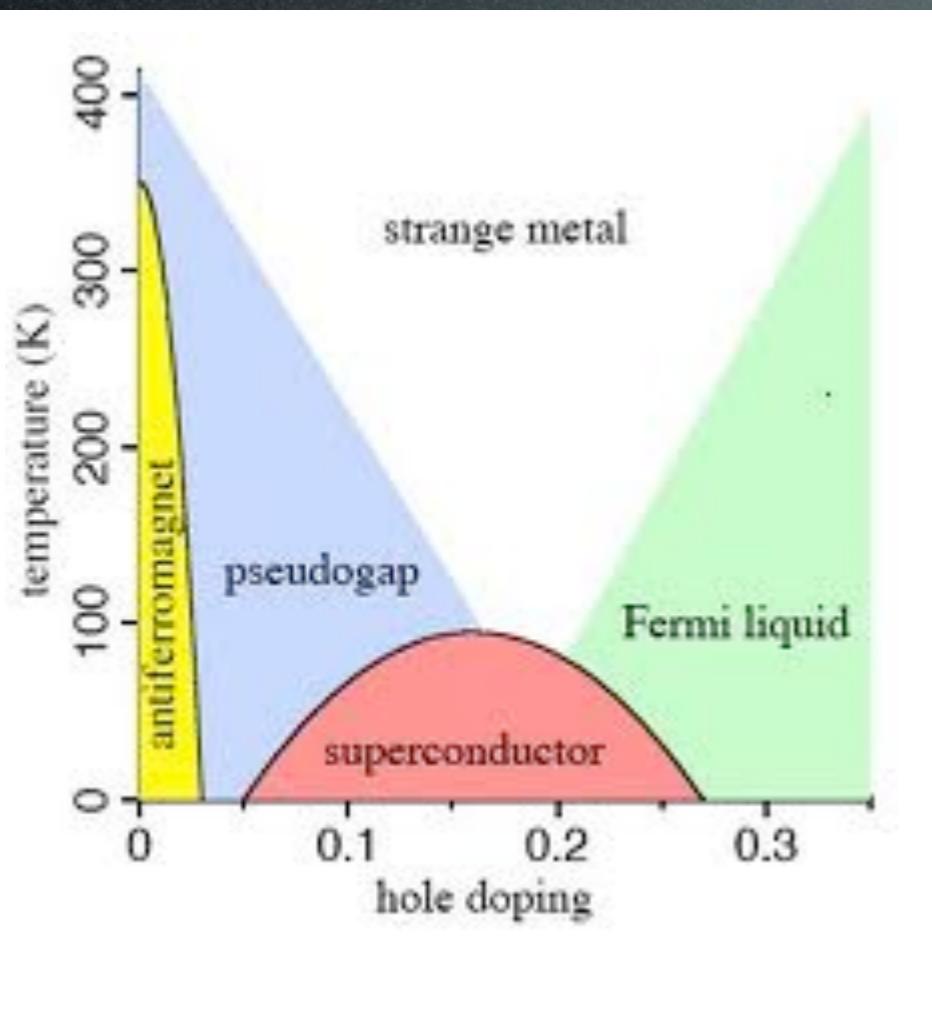
- Phases in between FL & MI
- Multiple “phases” at similar T
- Unidentifiable regions

Riddles



www.theoi.com

Riddles of Pseudo Gap



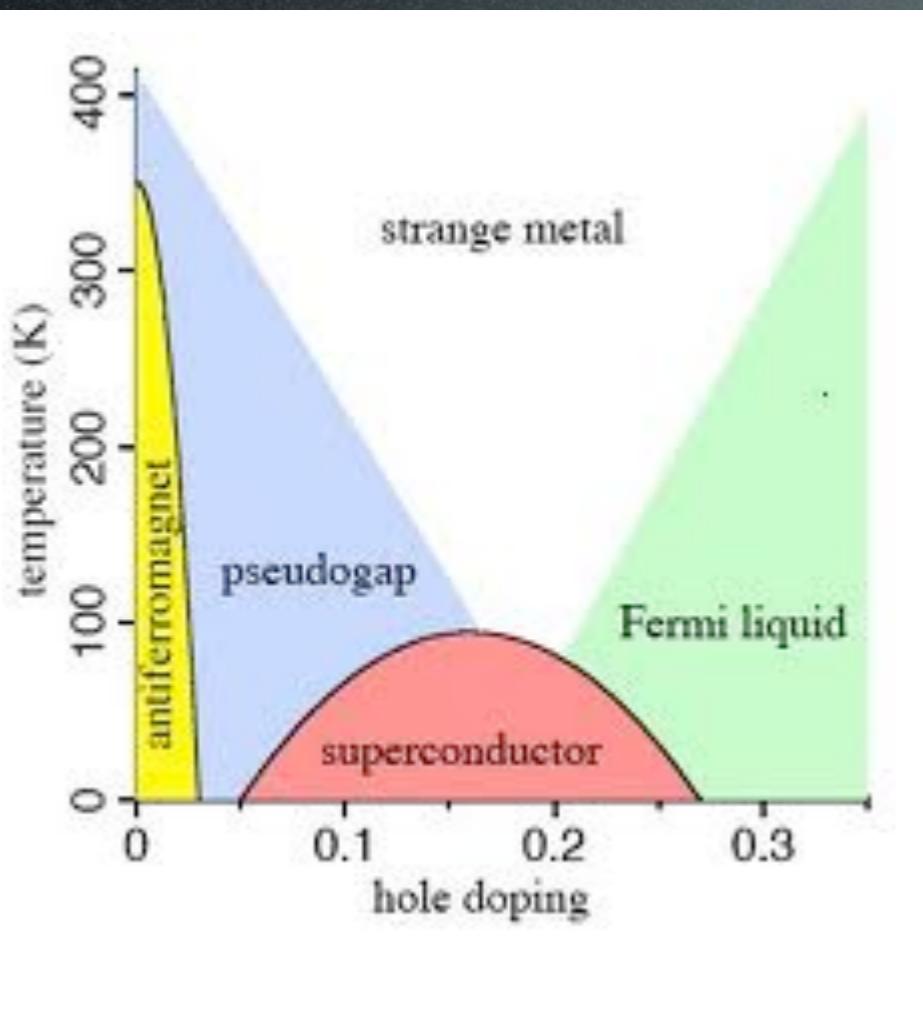
AF: Antiferromagnet

SC: Superconductor

PG: Pseudogap

HTS: High temperature Superconductor

Riddles of Pseudo Gap



- Cross-over or Phase transition?

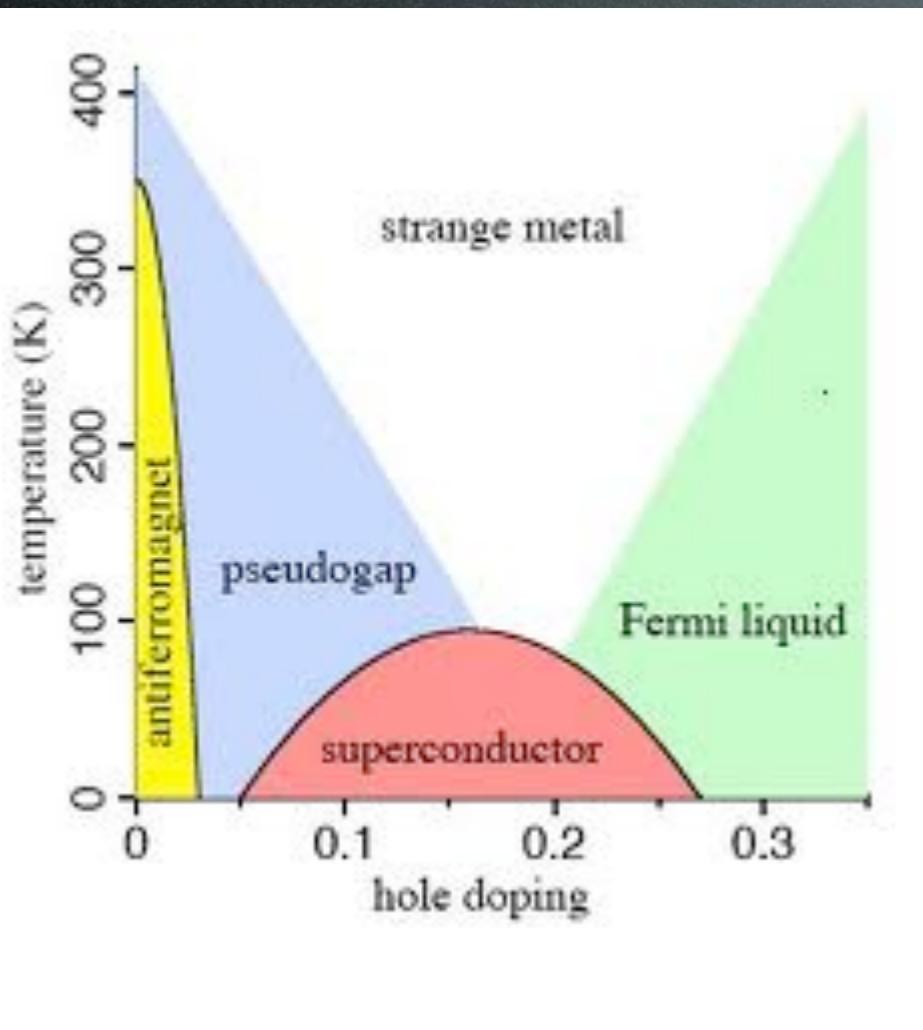
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Riddles of Pseudo Gap



- Cross-over or Phase transition?
- Symmetry breaking?

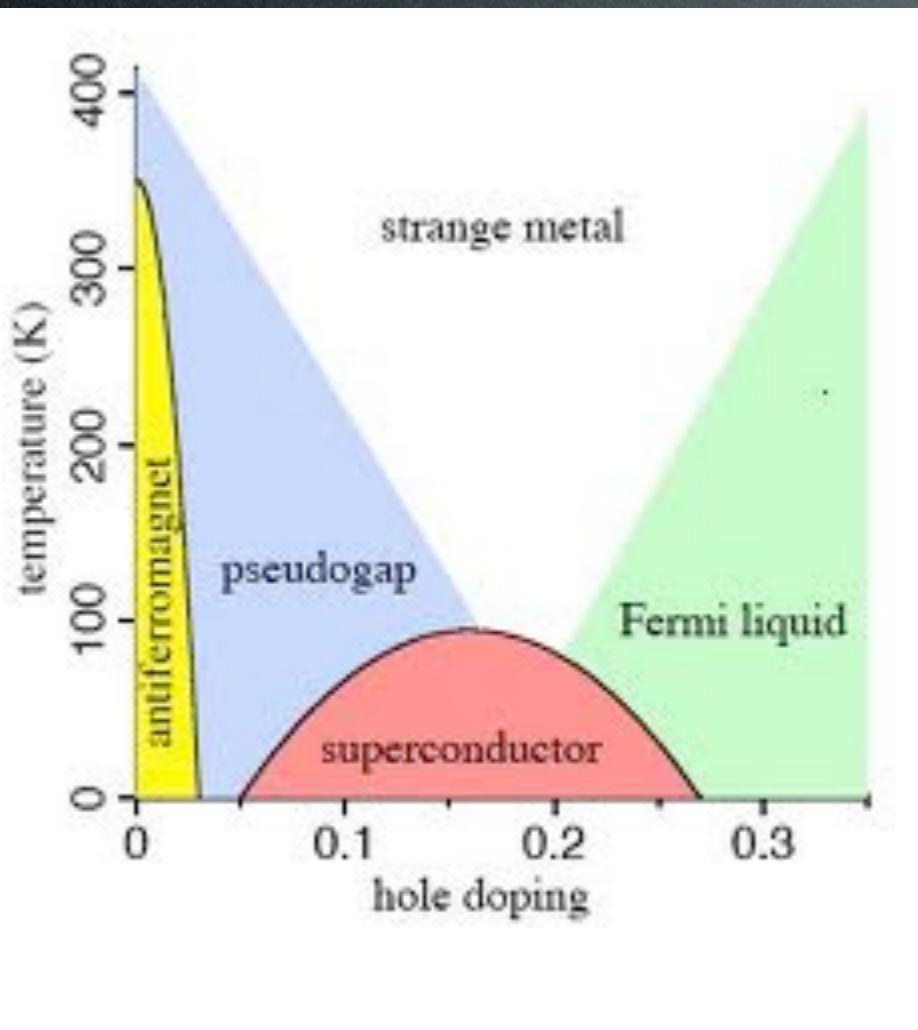
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Riddles of Pseudo Gap



- Cross-over or Phase transition?
- Symmetry breaking?
- What are broken symmetries?

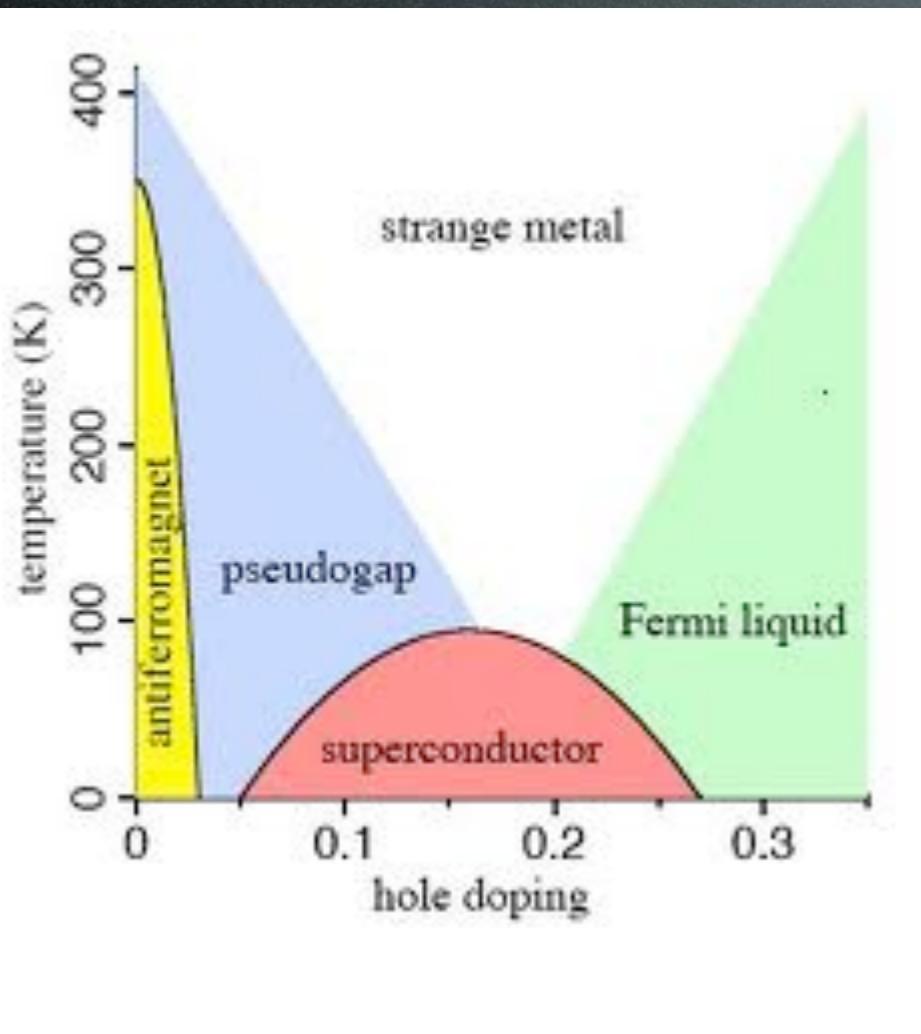
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Riddles of Pseudo Gap



- Cross-over or Phase transition?
- Symmetry breaking?
- What are broken symmetries?

➡ Challenge:

- 1) Define and detect order parameter

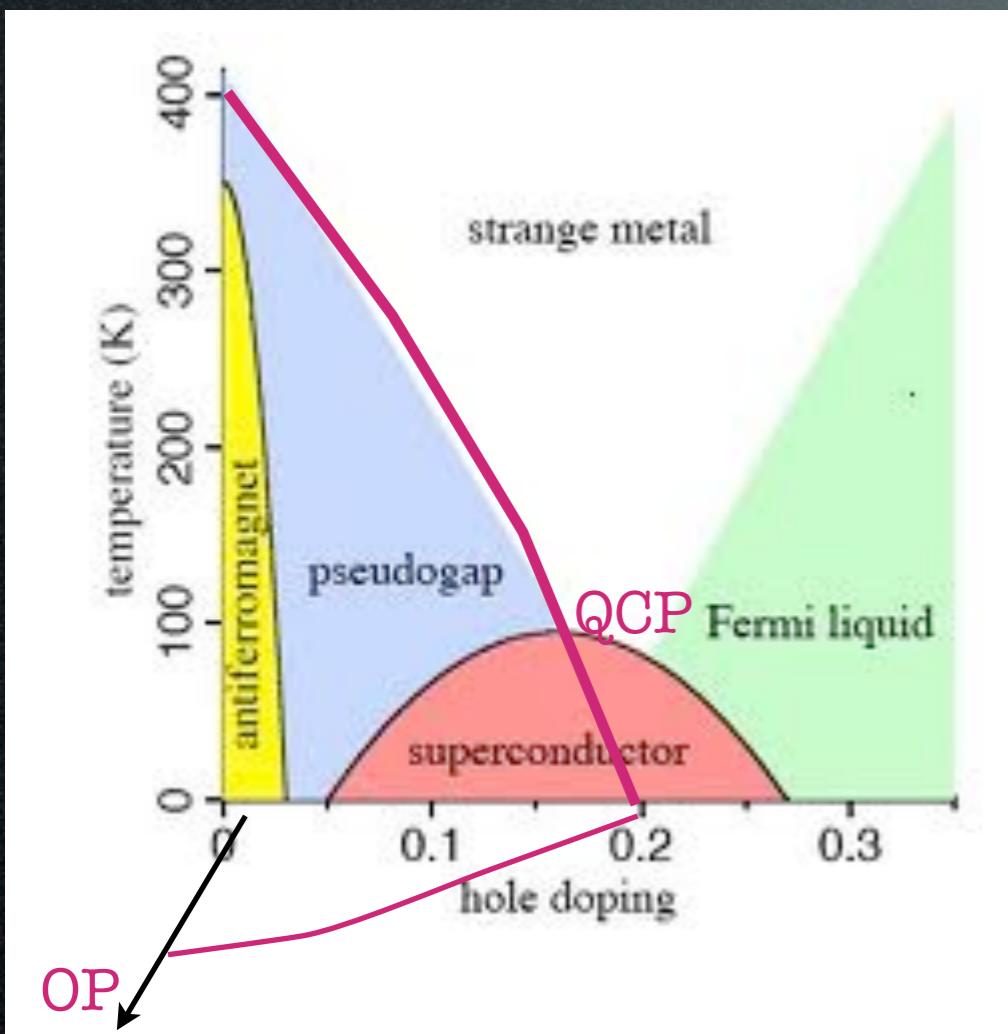
AF: Antiferromagnet

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Riddles of Pseudo Gap



- Cross-over or Phase transition?
- Symmetry breaking?
- What are broken symmetries?

→ Challenge:

- 1) Define and detect order parameter

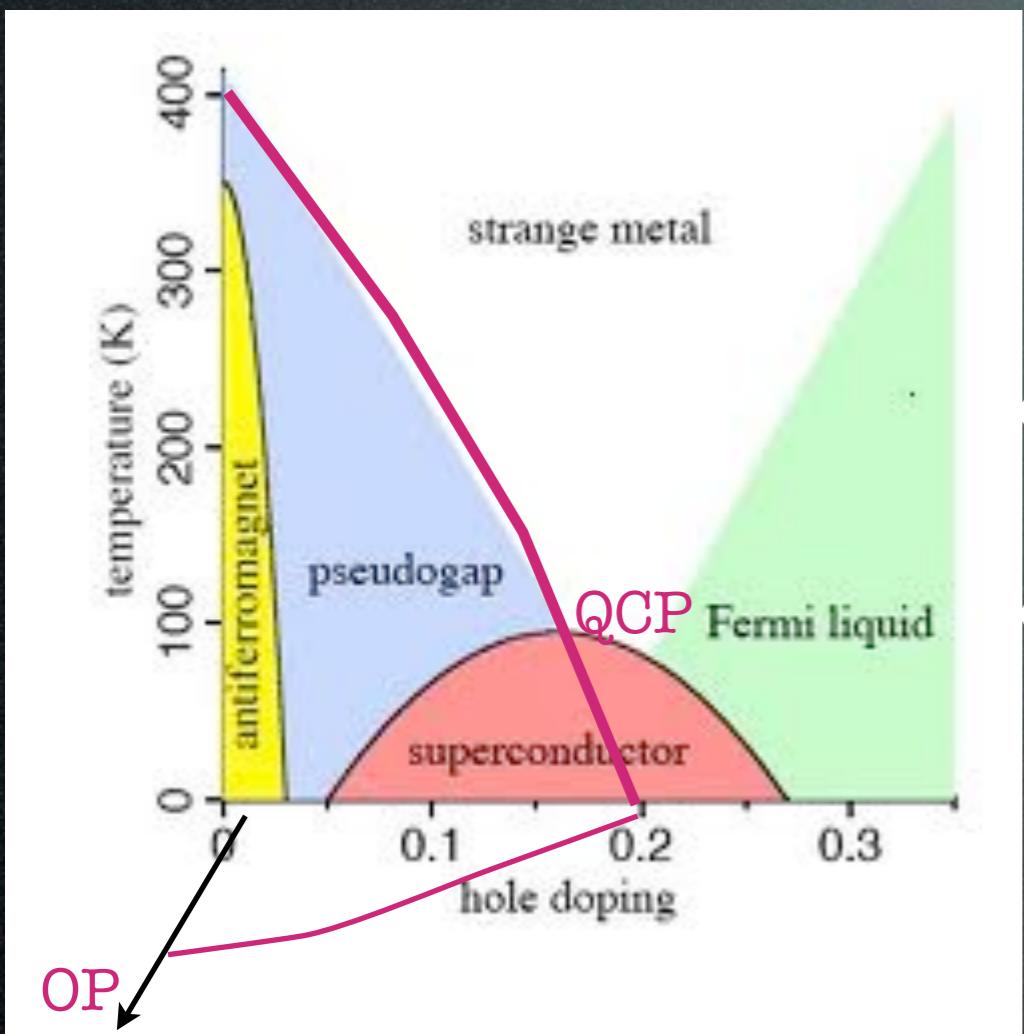
AF: Antiferromagnet

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Riddles of Pseudo Gap



- Cross-over or Phase transition?
- Symmetry breaking?
- What are broken symmetries?

→ Challenge:

- 1) Define and detect order parameter
- 2) Locate the Quantum Critical Point (QCP)

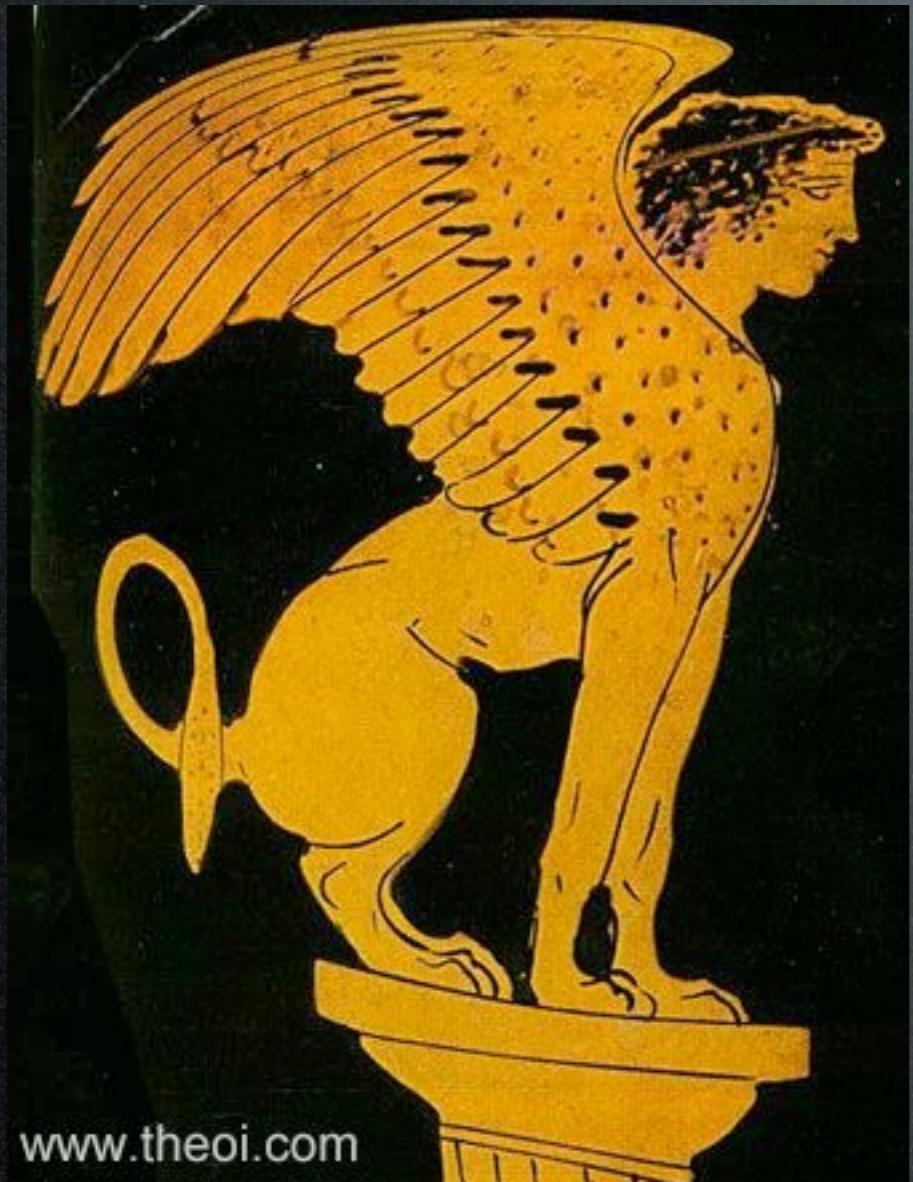
AF: Antiferromagnet

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HTS: High temperature Superconductor

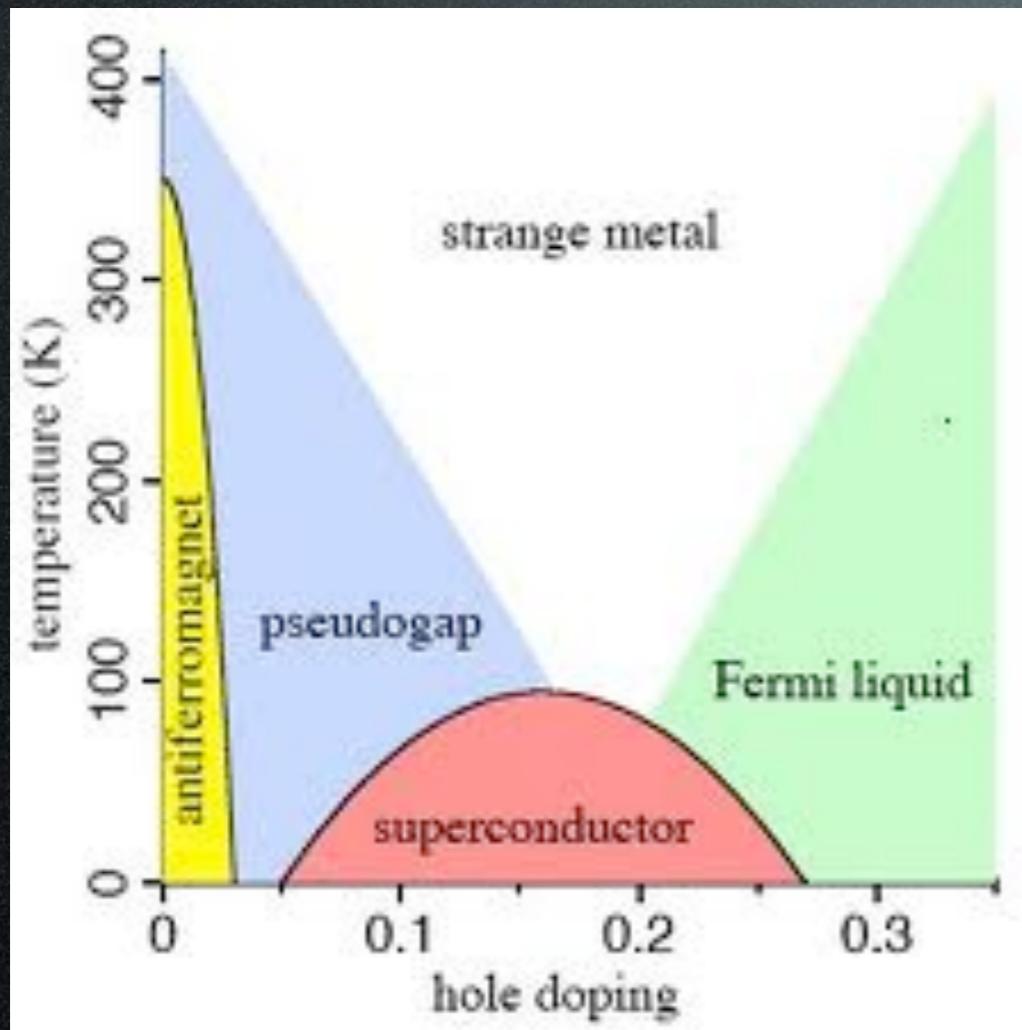
Riddles of Sphinx



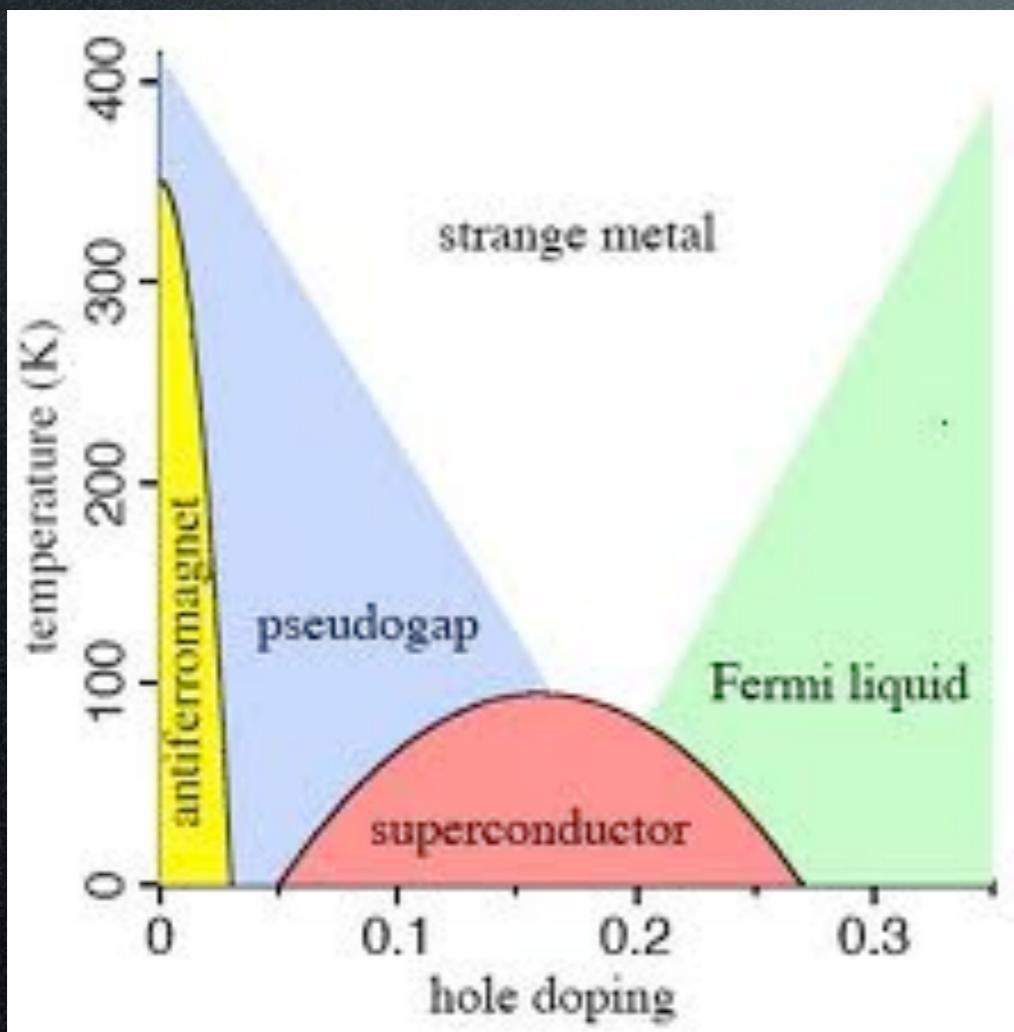
www.theoi.com



Riddles of Pseudogap

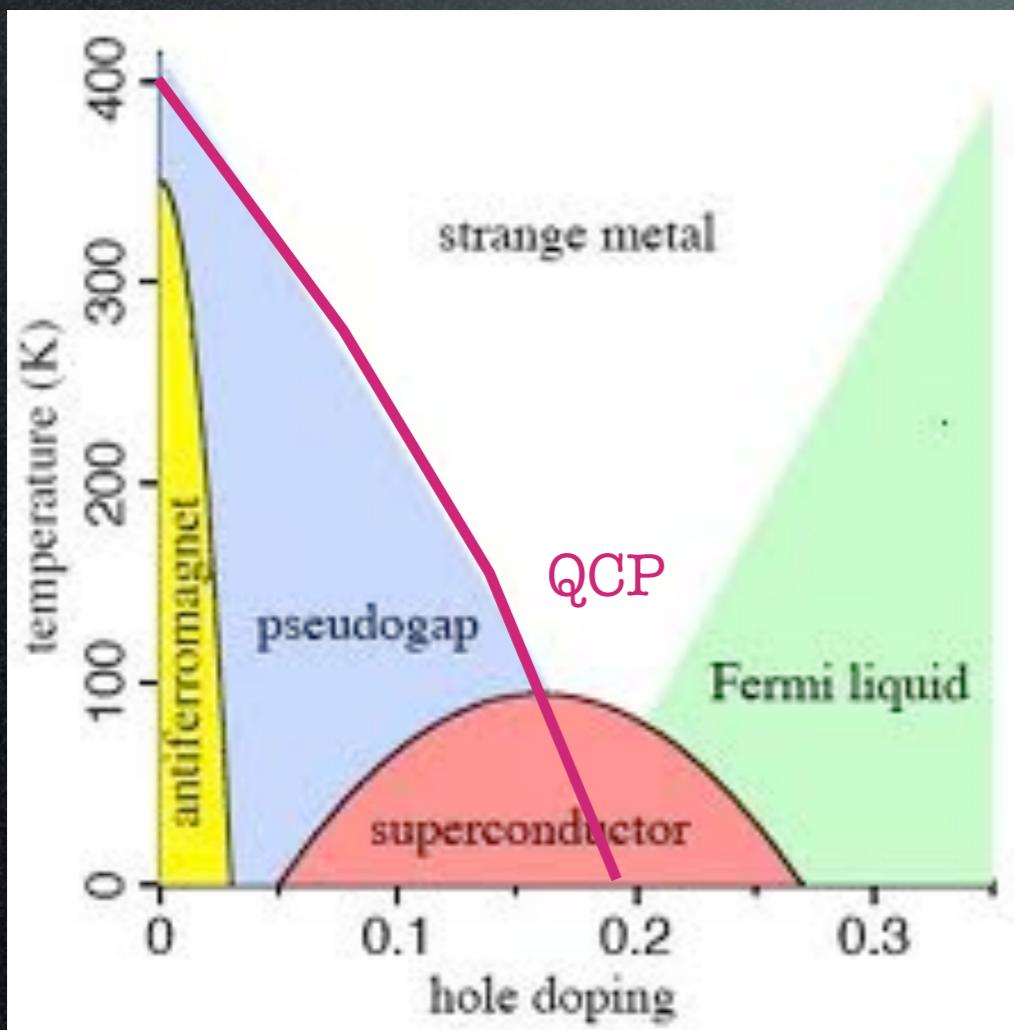


Riddles of Pseudogap



- Y. Li "Unusual magnetic order in the pseudogap region of the superconductor HgBa₂CuO₄₊₁d" Nature 455 372 2008
- Jing Xia, "Polar Kerr-Effect Measurements of YBa₂Cu₃O_{6+x} Superconductor: Evidence for Broken Symmetry near the Pseudogap Temperature" PRL 100 127002 2008
- M. J. Lawler "Intra-unit-cell electronic nematicity of the high-T_c copper-oxide pseudogap states" Nature 466 347 2010
- R. Daou "Broken rotational symmetry in the pseudogap phase of a high-T_c superconductor" Nature 463 519 2010
- S. De Almeida-Didry Evidence for intra-unit-cell magnetic order in Bi₂Sr₂CaCu₂O₈ PHYSICAL REVIEW B 86 020504(R) 2012
- Tao Wu, "Magnetic-field-induced charge-stripe order in the high-temperature superconductor YBa₂Cu₃O_y" Nature 477 191 2011
- G. Ghiringhelli, "Long-Range Incommensurate Charge Fluctuations in (Y,Nd)Ba₂Cu₃O_{6+x}" Science 337 821 2012
- J. Chang, "Direct observation of competition between superconductivity and charge density wave order in YBa₂Cu₃O_{6.67}" Nature Physics 8 871 2012

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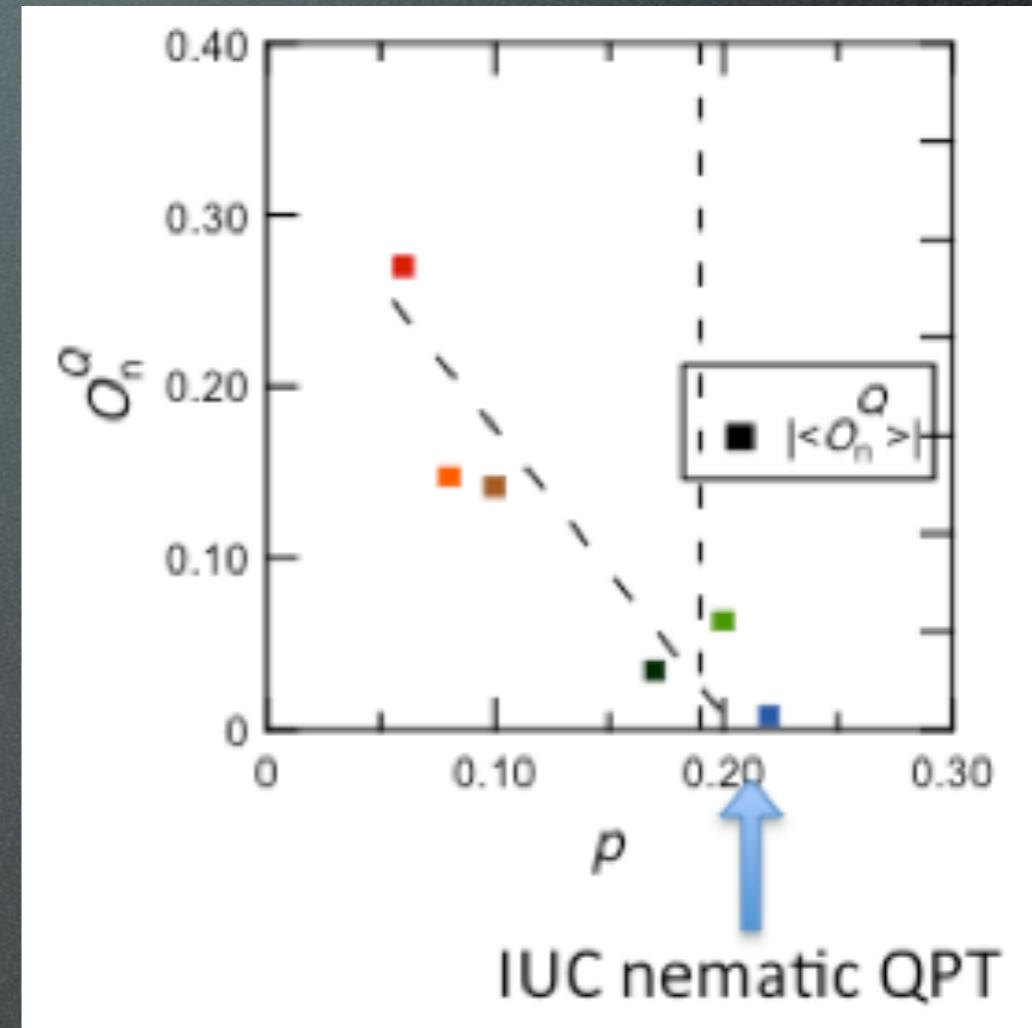
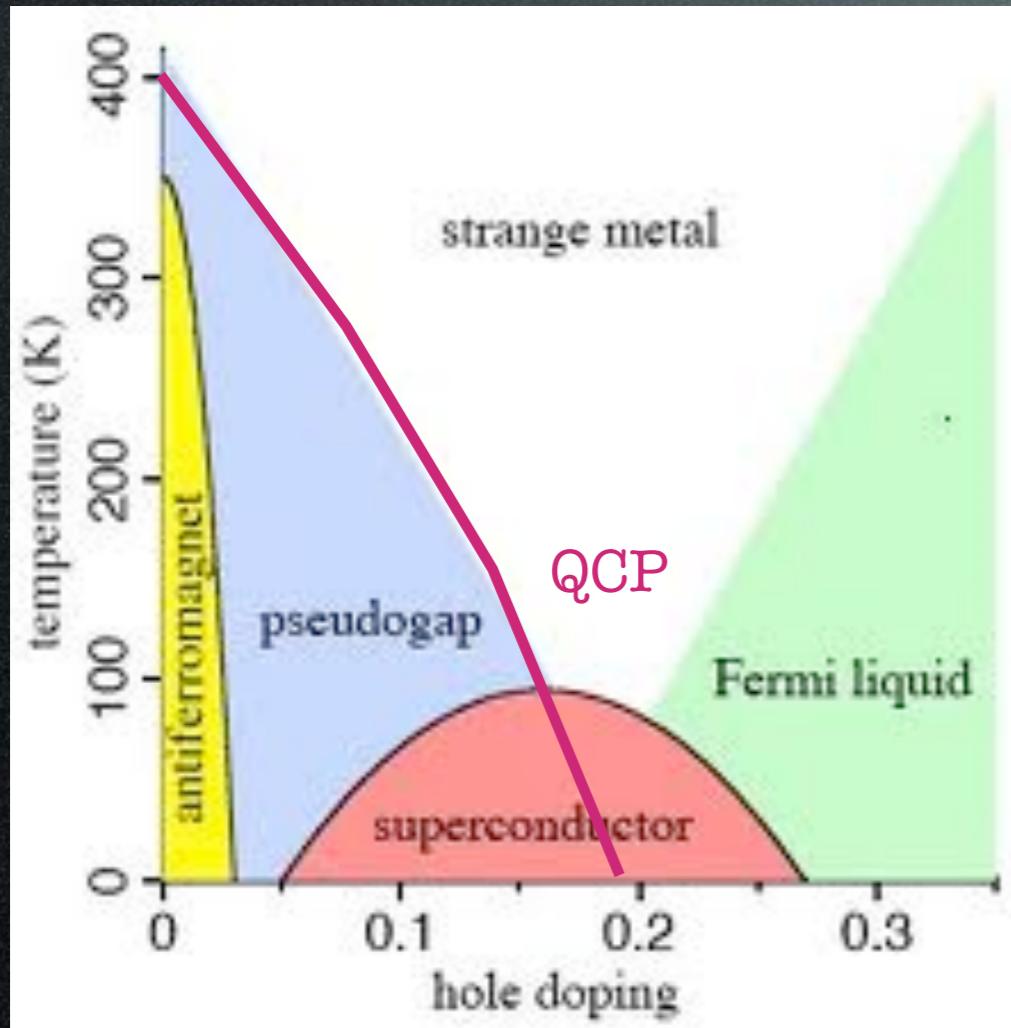
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Science 337 821 2012

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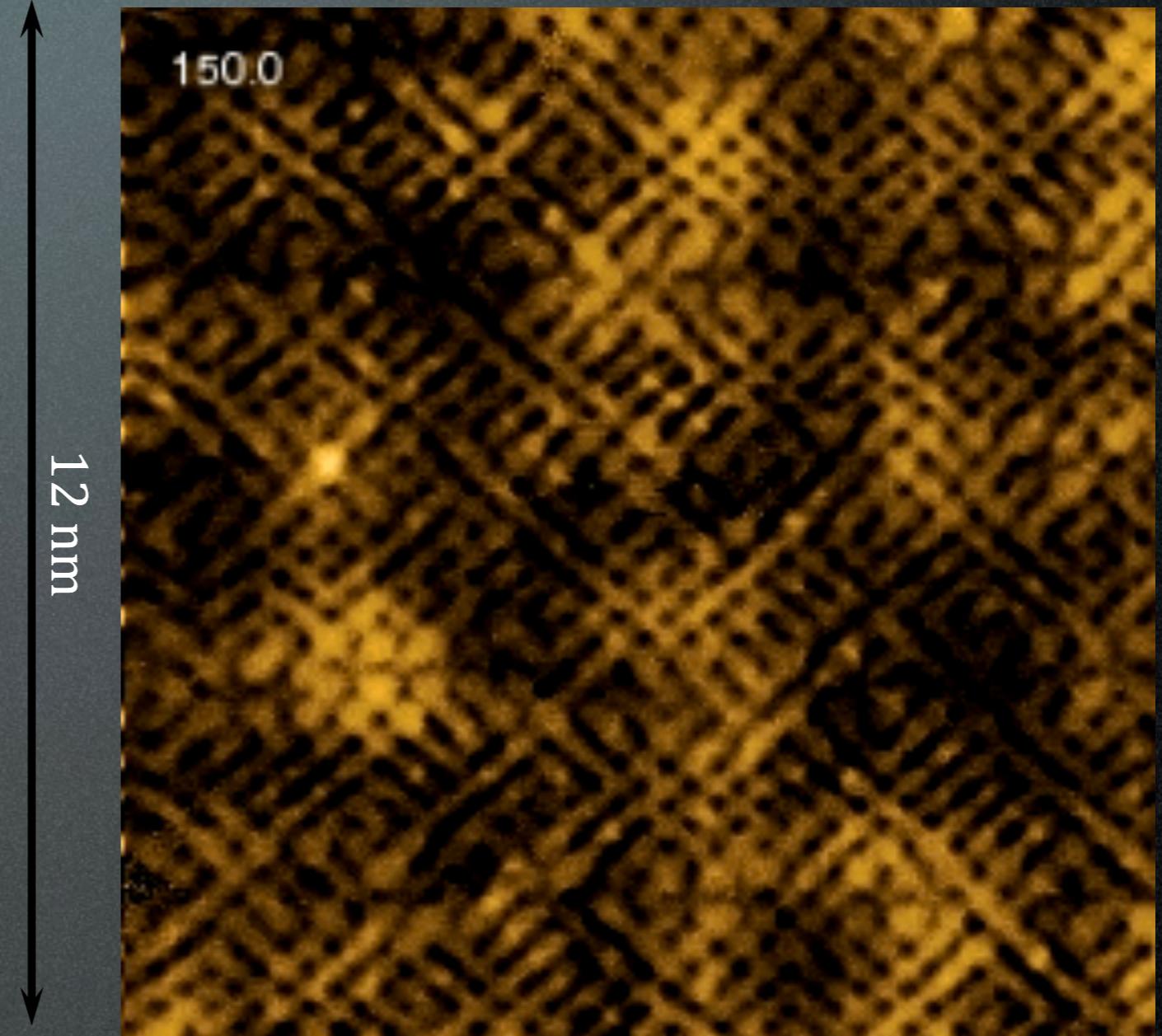
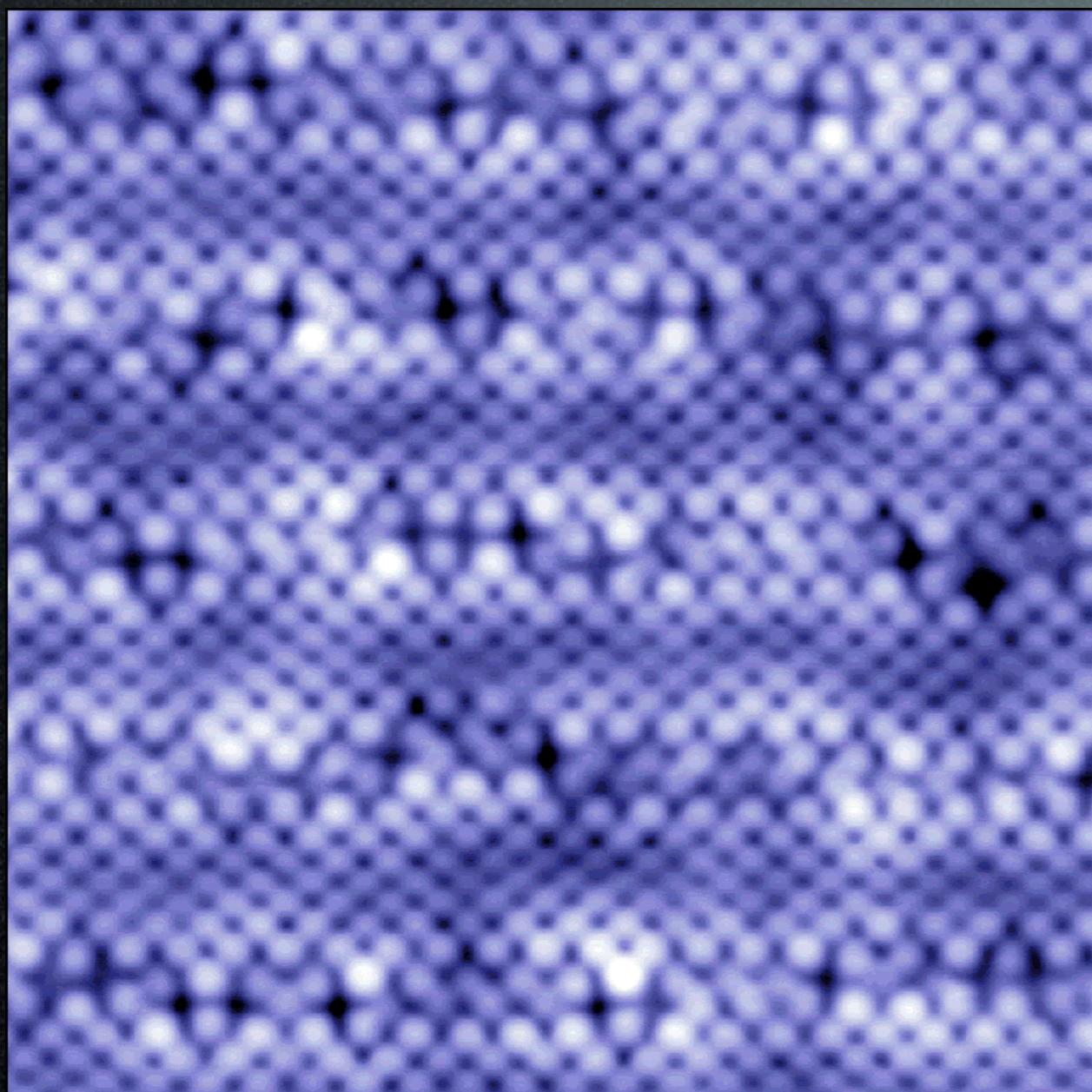
Riddles of Pseudogap



K. Fujita et al, submitted to
Science (2014)

Visualize Broken-Symmetry States

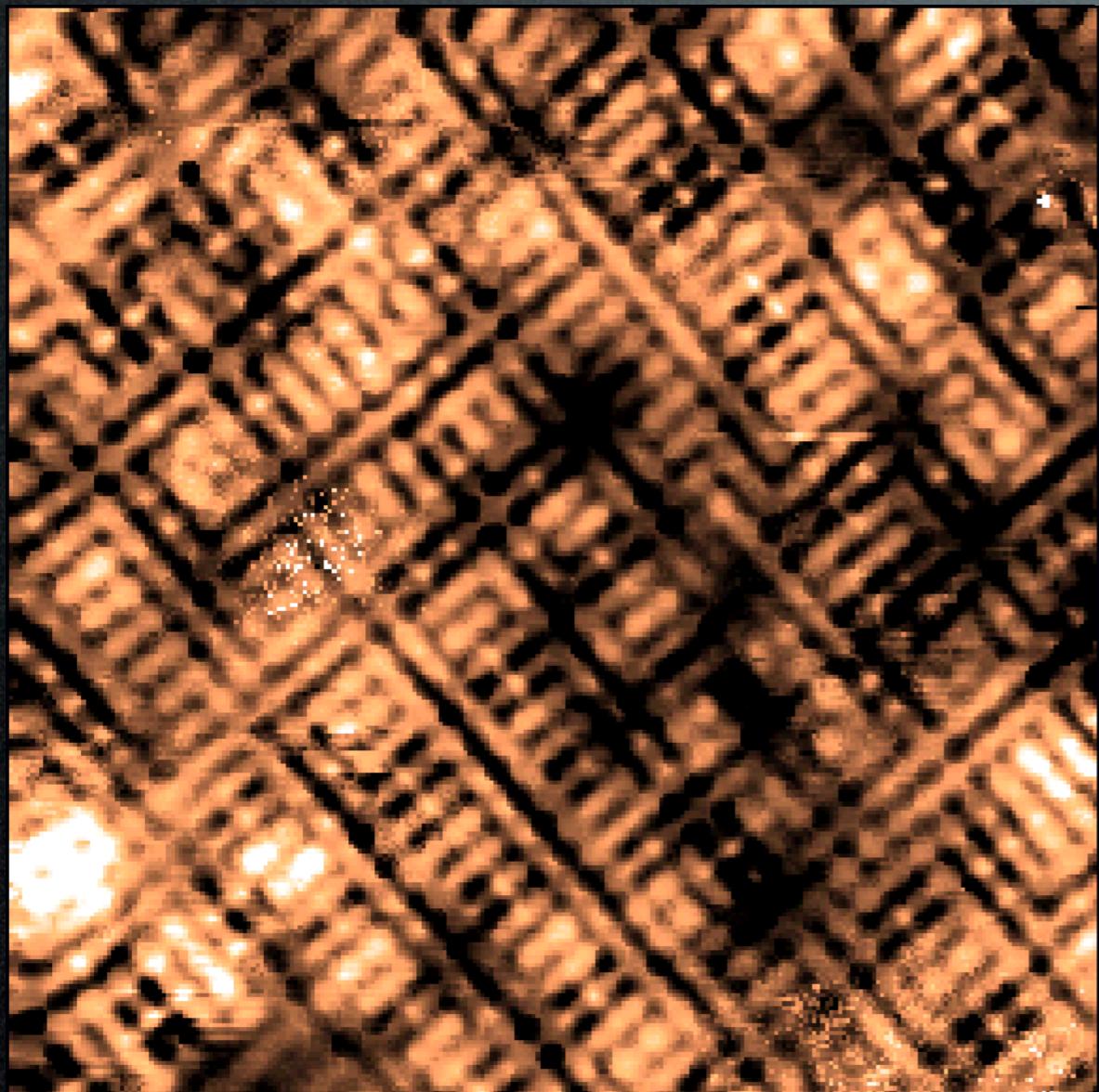
Science 315, 1380 (2007)



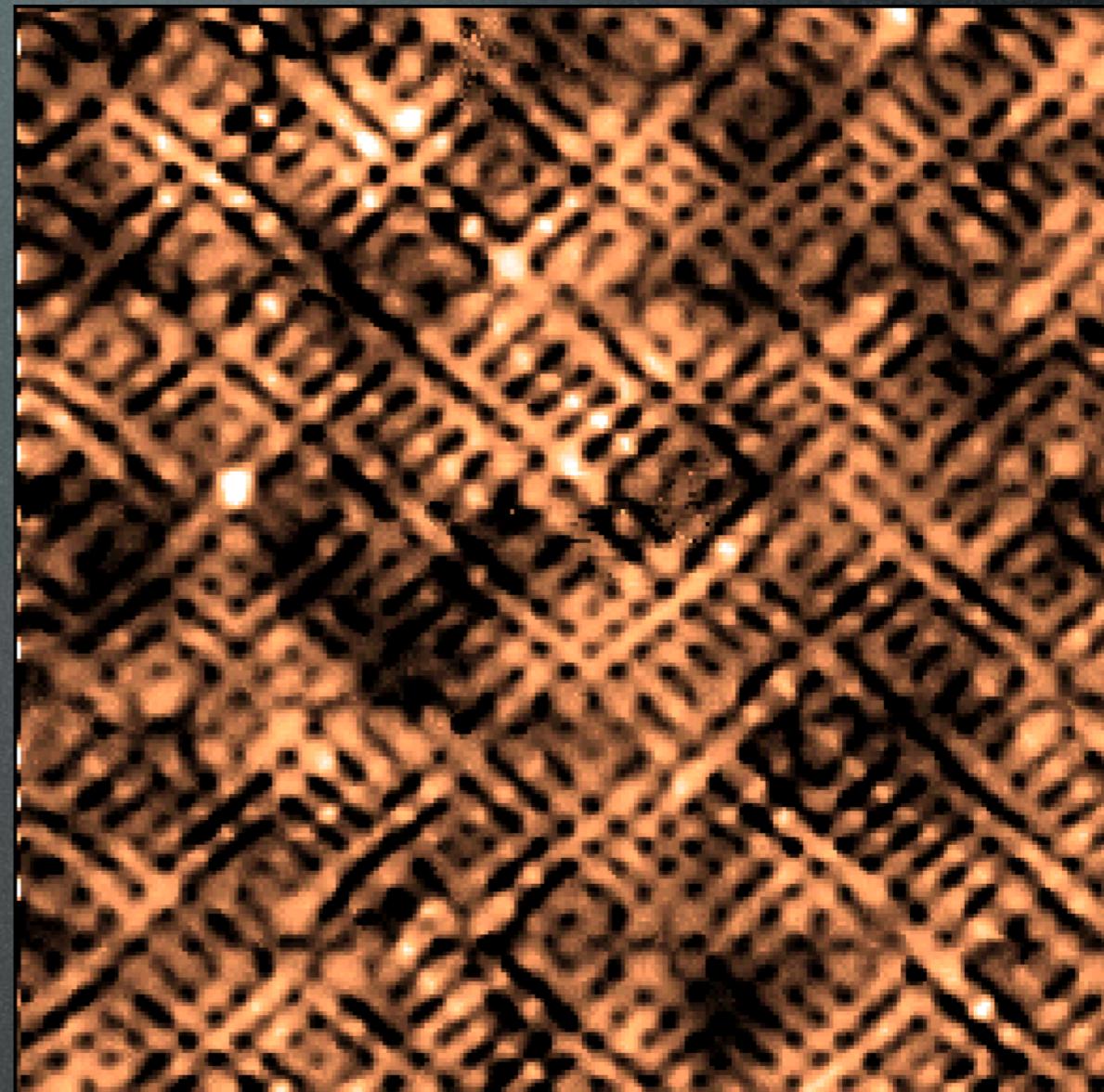
0.5 1.9

Not due to surface /crystal symmetry / dopant disorder etc

Science 315, 1380 (2007)



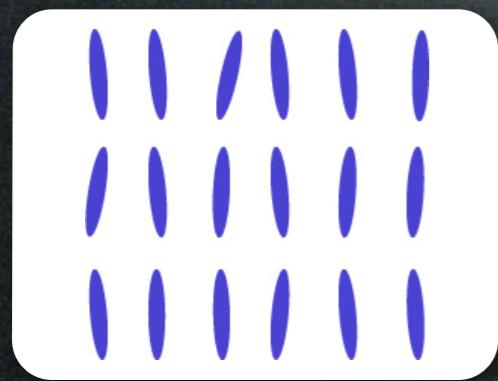
$\text{Ca}_{1.90}\text{Na}_{0.10}\text{CuO}_2\text{Cl}_2$



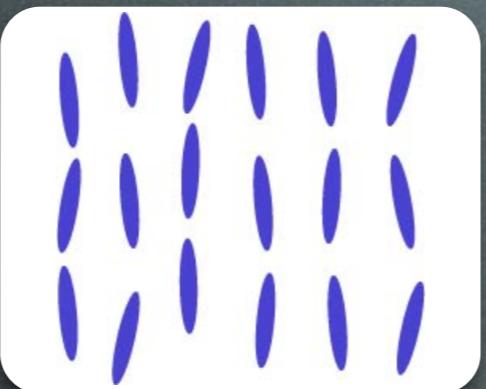
$\text{Bi}_{2.2}\text{Sr}_{1.8}\text{Ca}_{0.8}\text{Dy}_{0.2}\text{Cu}_2\text{O}_y$

Symmetry Based Perspective

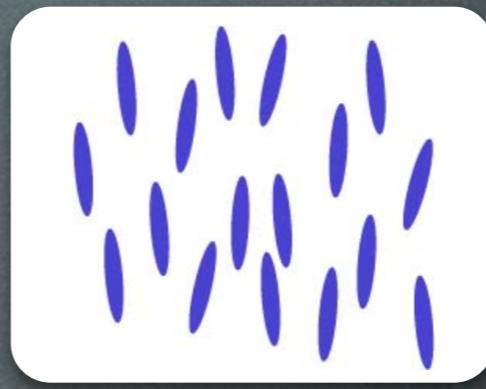
Analogy different phases of rod-like polymers



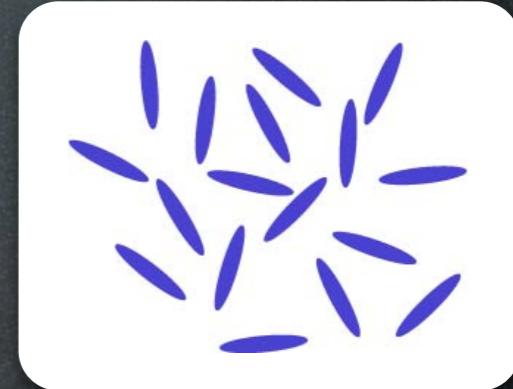
Crystal



Smectic



Nematic

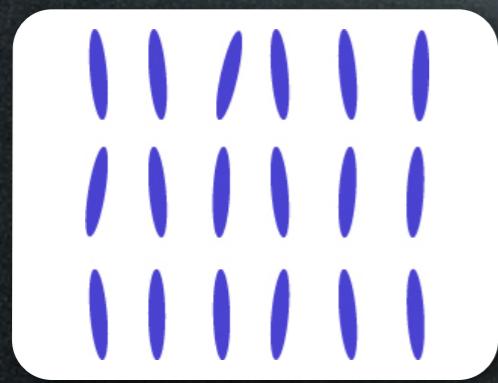


Liquid

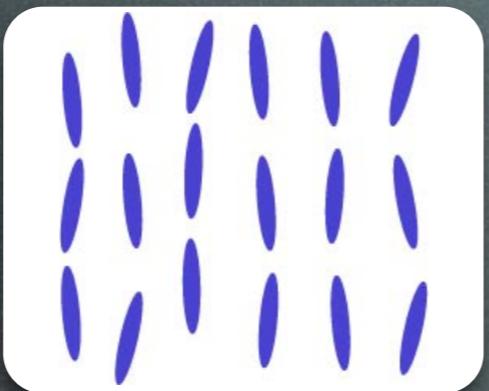


Symmetry Based Perspective

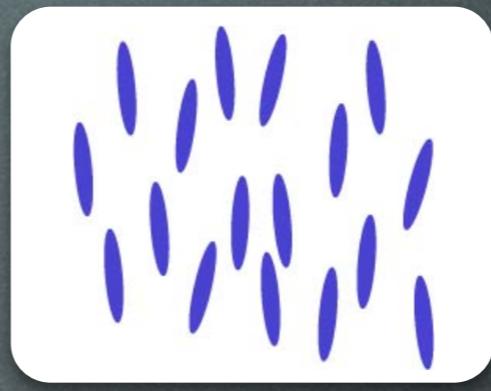
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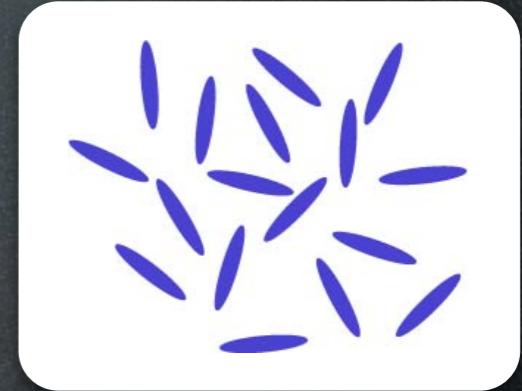
Crystal



Smectic



Nematic



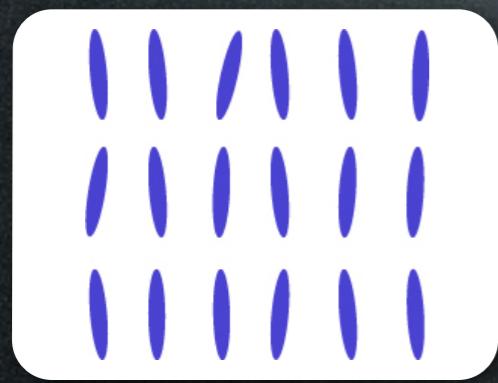
Liquid



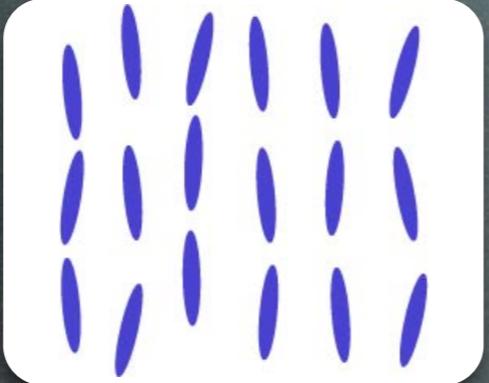
$$\hat{T}_a, \hat{T}_b, \hat{R}$$

Symmetry Based Perspective

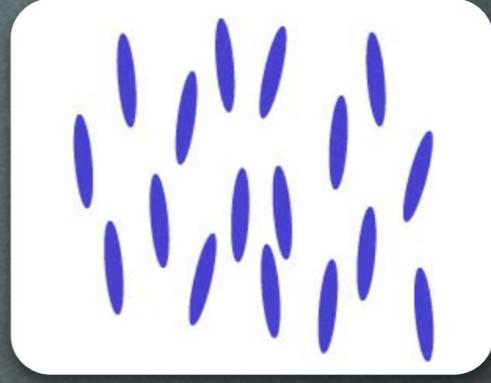
Analogy different phases of rod-like polymers



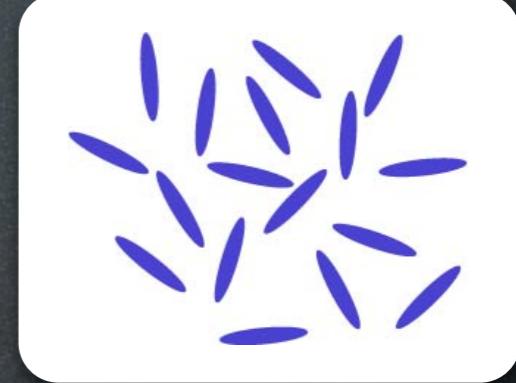
Crystal



Smectic



Nematic



Liquid

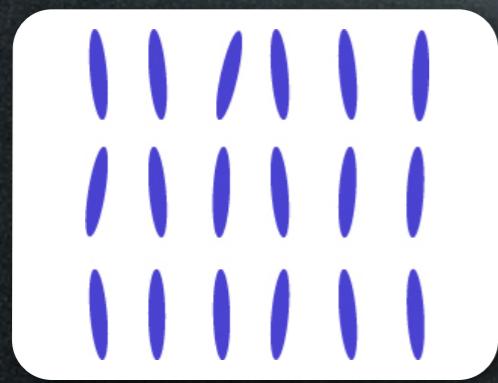


$\hat{T}_a, \hat{T}_b, \hat{R}$

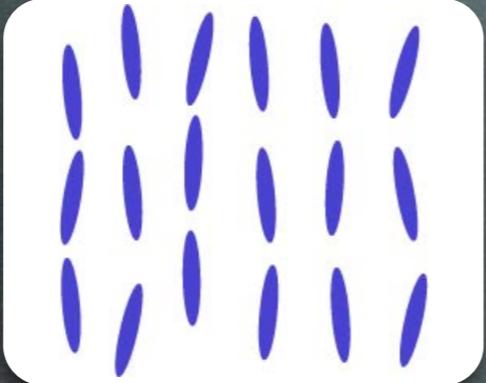
\hat{T}_a, \hat{R}

Symmetry Based Perspective

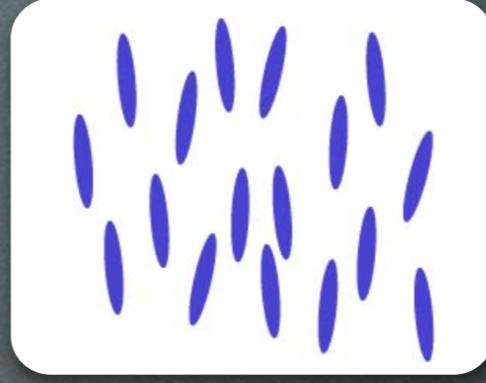
Analogy different phases of rod-like polymers



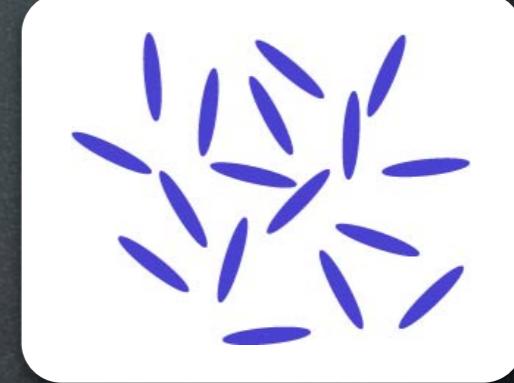
Crystal



Smectic



Nematic



Liquid

T



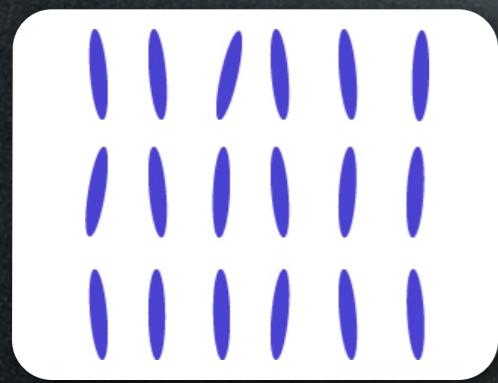
$\hat{T}_a, \hat{T}_b, \hat{R}$

\hat{T}_a, \hat{R}

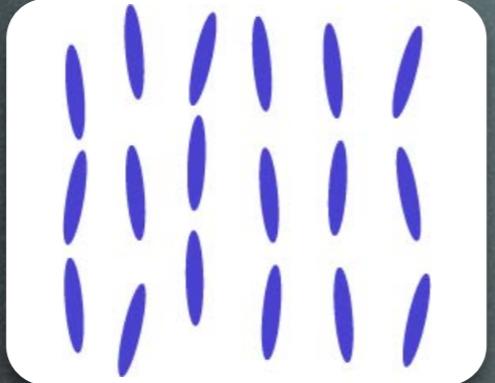
\hat{R}

Symmetry Based Perspective: ELC

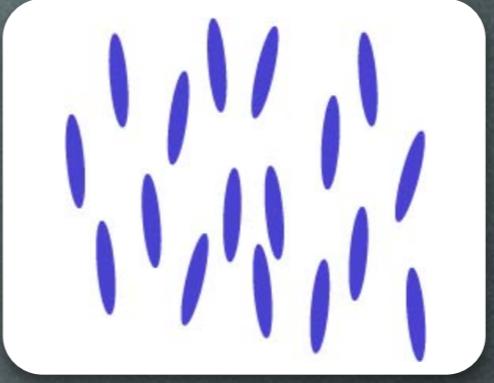
Analogy different phases of rod-like polymers



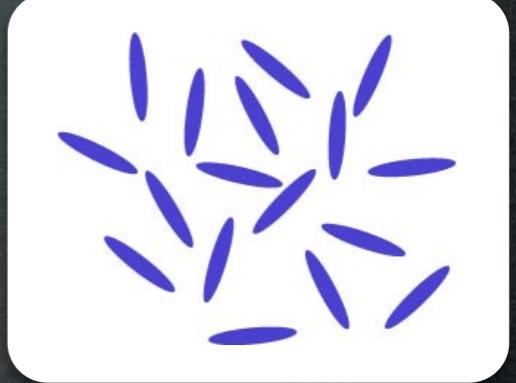
Crystal



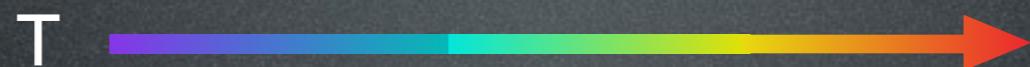
Smectic



Nematic



Liquid



$$\hat{T}_a, \hat{T}_b, \hat{R}$$

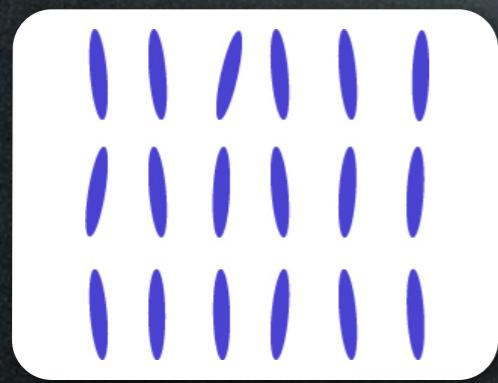
$$\hat{T}_a, \hat{R}$$

$$\hat{R}$$

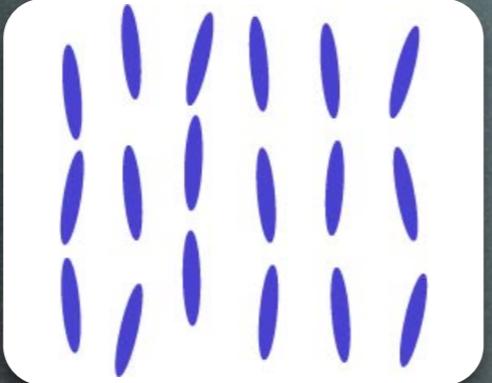
Electronic
Analogue
?

Symmetry Based Perspective: ELC

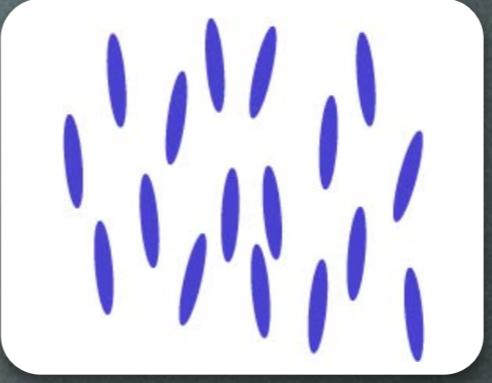
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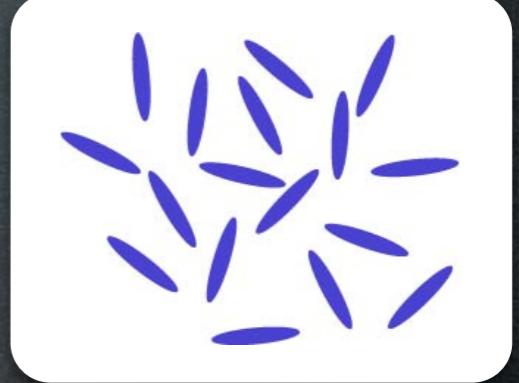
Crystal



Smectic



Nematic



Liquid

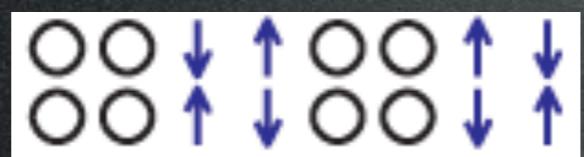


$\hat{T}_a, \hat{T}_b, \hat{R}$

\hat{T}_a, \hat{R}

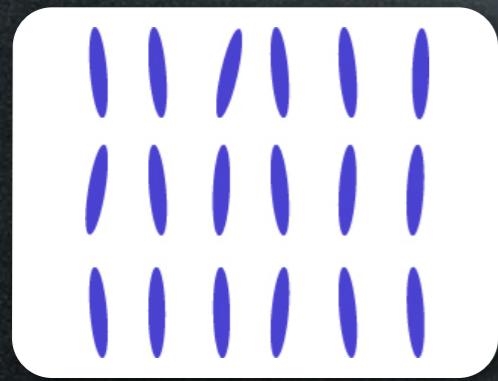
\hat{R}

Electronic
Analogue
?

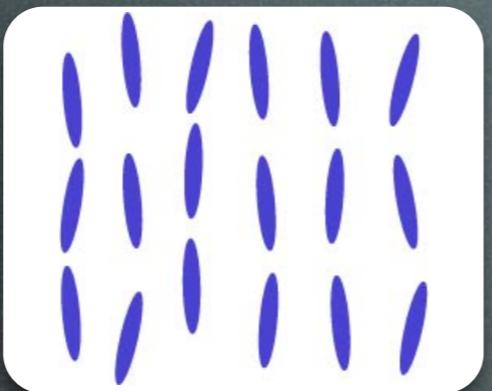


Symmetry Based Perspective: ELC

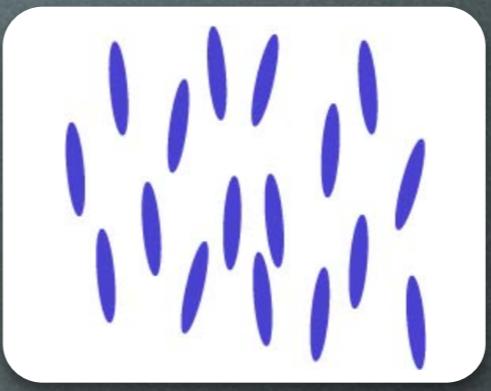
Analogy different phases of rod-like polymers



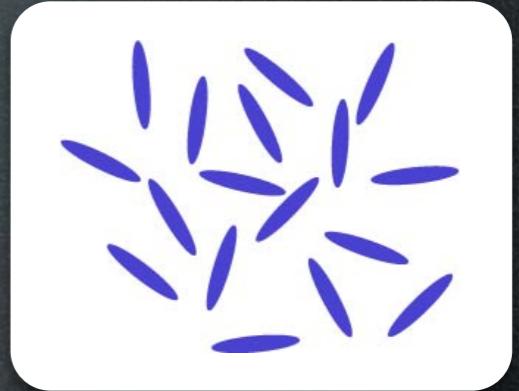
Crystal



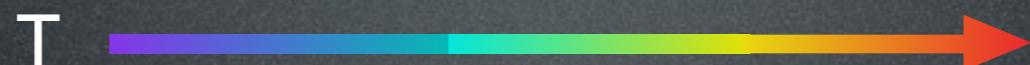
Smectic



Nematic



Liquid

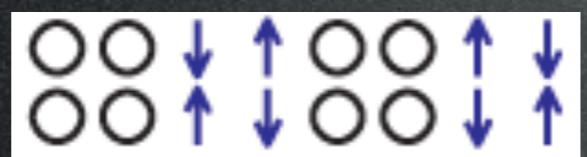


$\hat{T}_a, \hat{T}_b, \hat{R}$

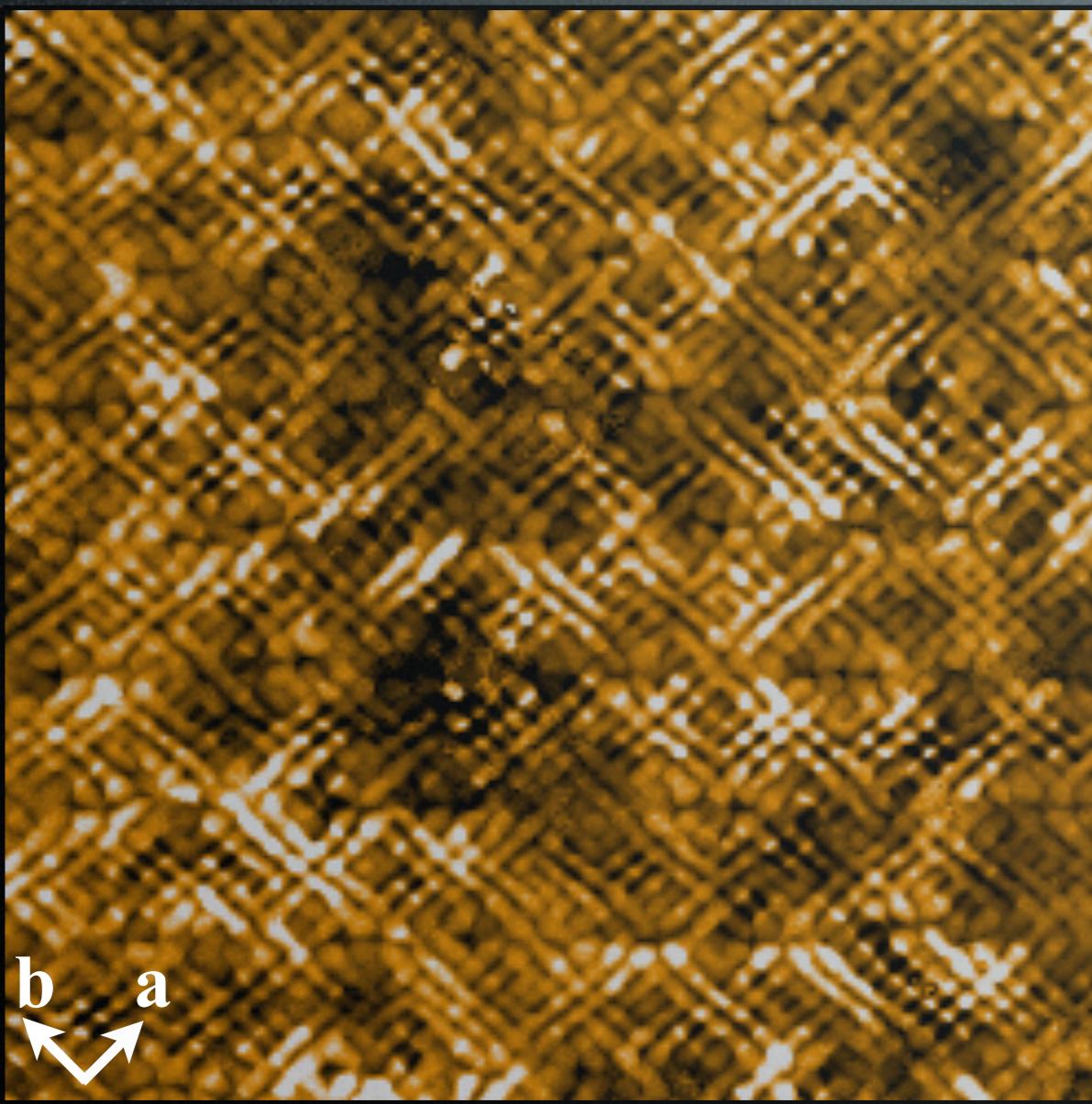
\hat{T}_a, \hat{R}

\hat{R}

Electronic
Analogue
?



?

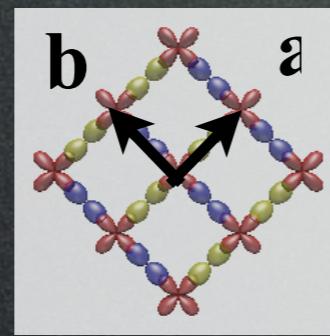


b
a

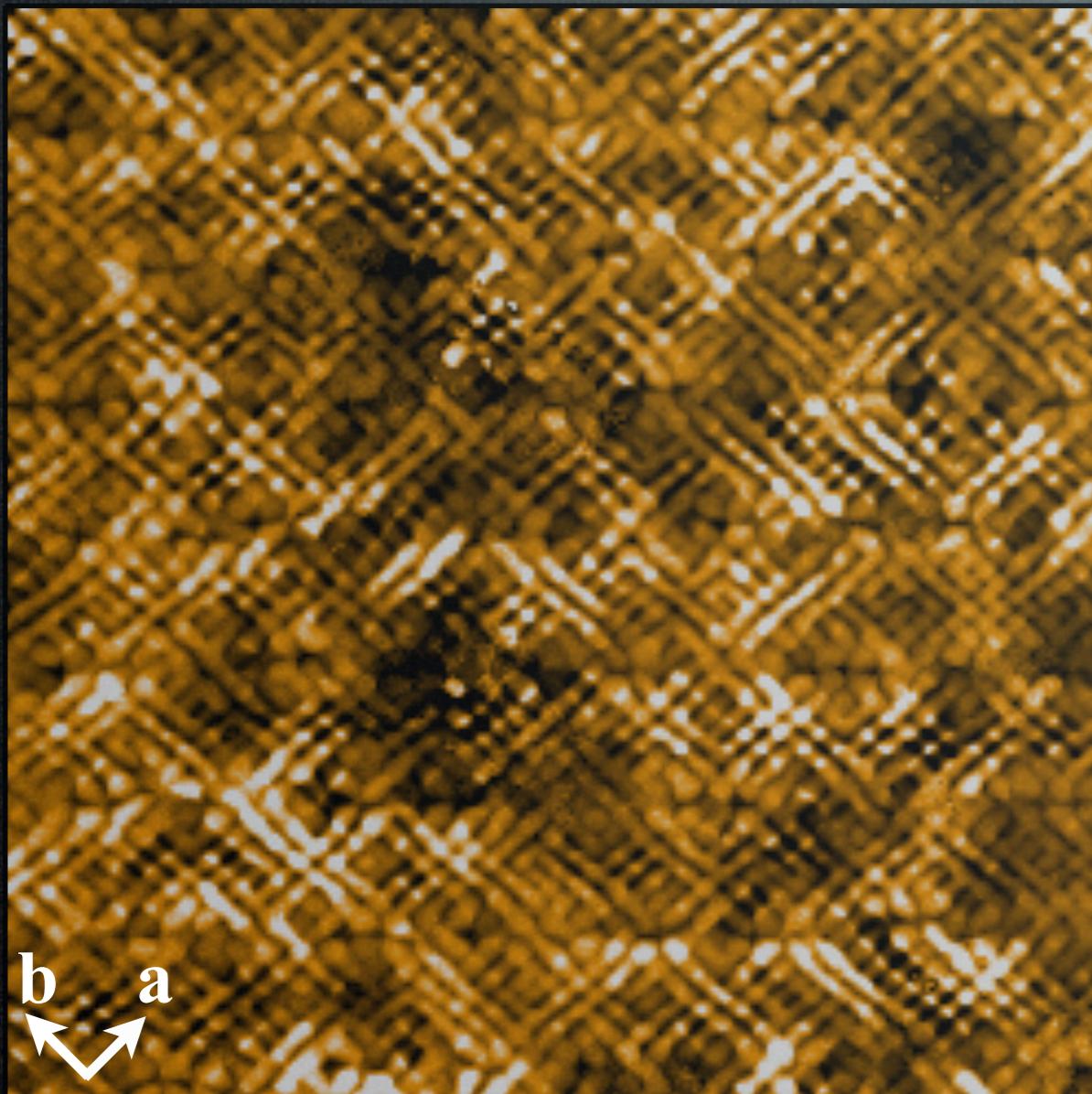
2nm

$Z(r, e=1)$

Position space



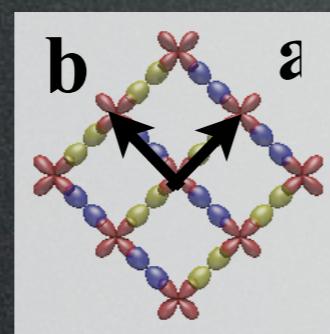
Separate Broken Symmetries?: Use distinct Fourier Components



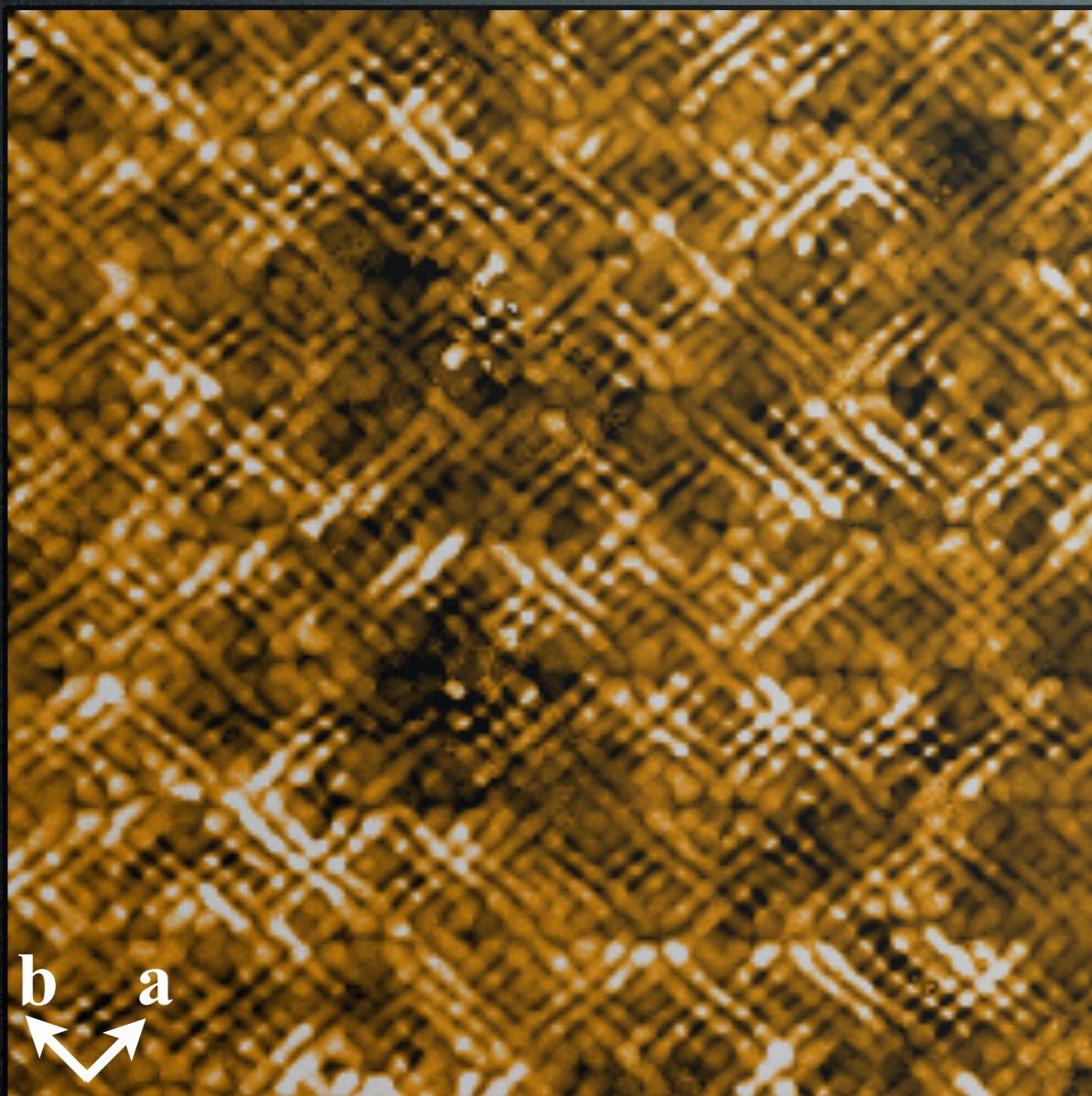
2nm

$Z(r, e=1)$

Position space

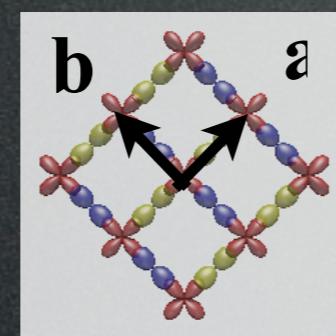


Separate Broken Symmetries?: Use distinct Fourier Components

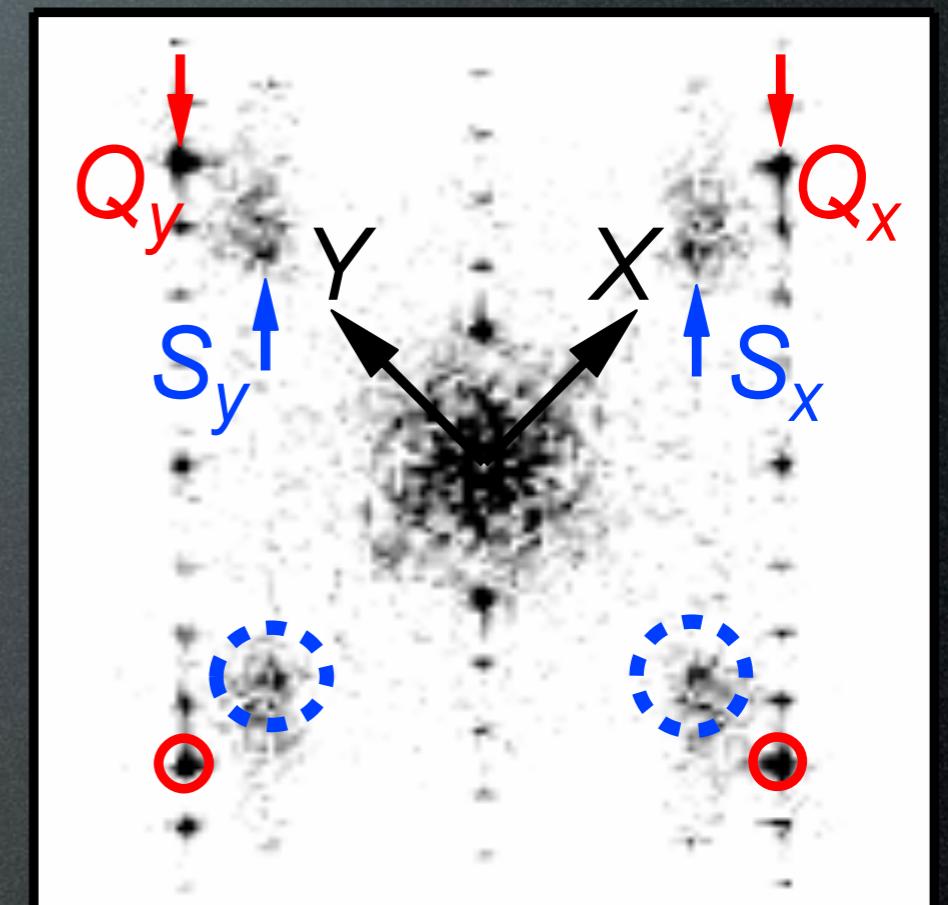


$Z(r, e=1)$

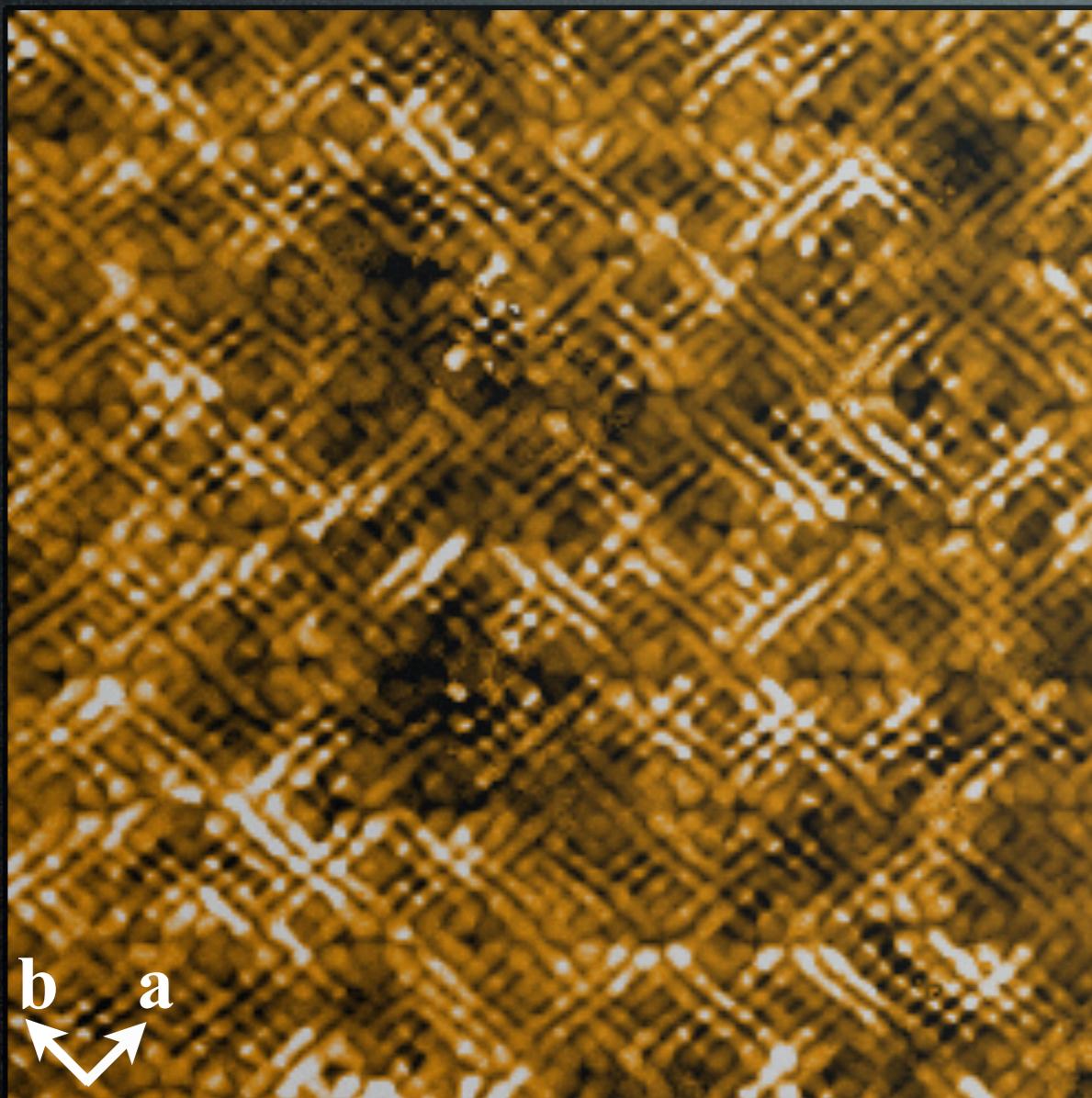
Position space



Fourier space



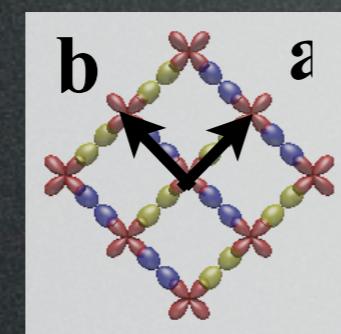
Separate Broken Symmetries?: Use distinct Fourier Components



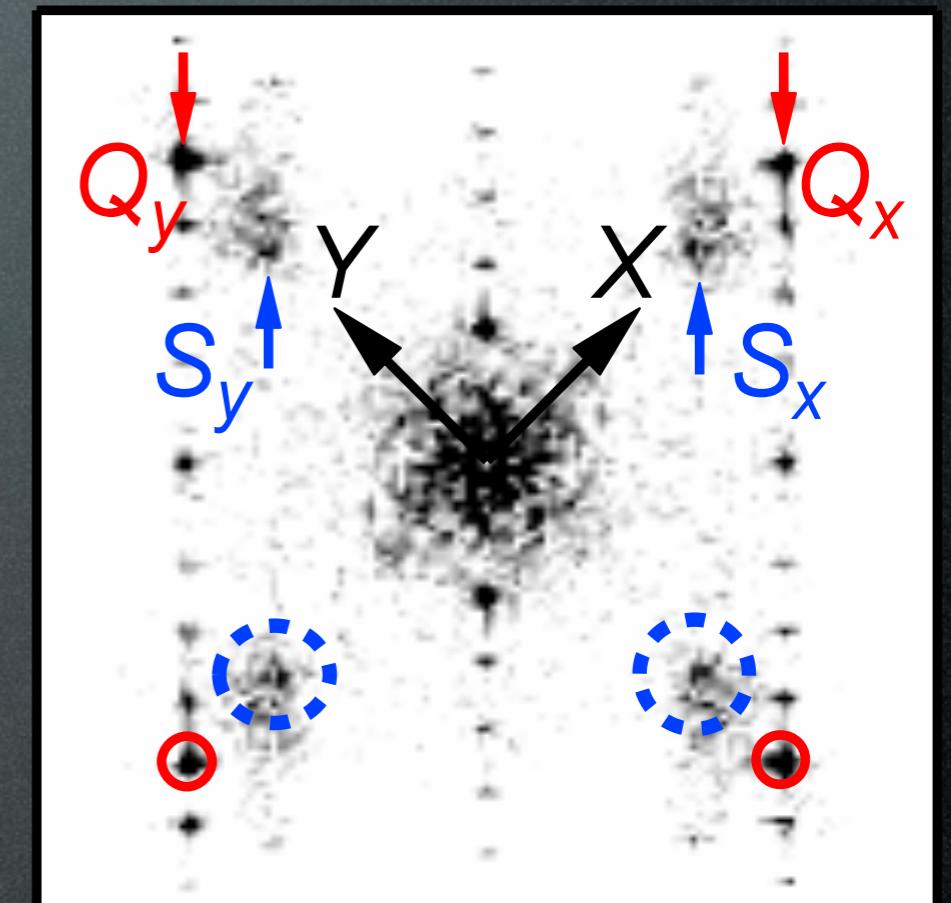
2nm

Position space

$Z(r, e=1)$



Fourier space



IUC order: Q_x & Q_y ?

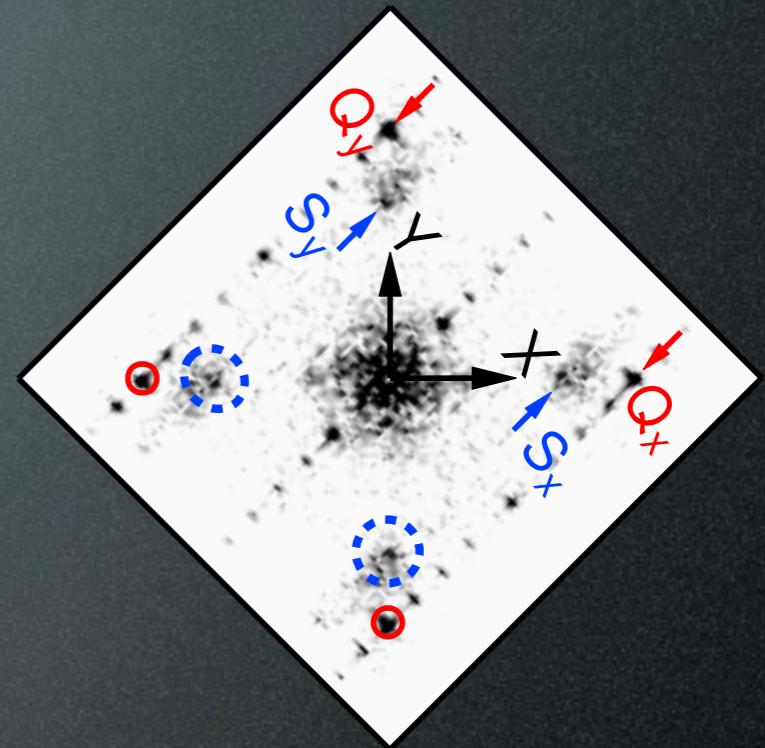
\hat{T}_a, \hat{T}_b breaking:
 S_x & S_y ?

\longleftrightarrow \longleftrightarrow

Q_x VS Q_y

- For any local map $M(\vec{r})$
- Bragg peak

$$\tilde{M}(\vec{Q}_x) = \frac{1}{\sqrt{N}} \sum_{\vec{R}, \vec{d}} M(\vec{R} + \vec{d}) e^{-i \vec{Q}_x \cdot \vec{d}}$$
$$\vec{Q}_x = (2\pi/a, 0)$$

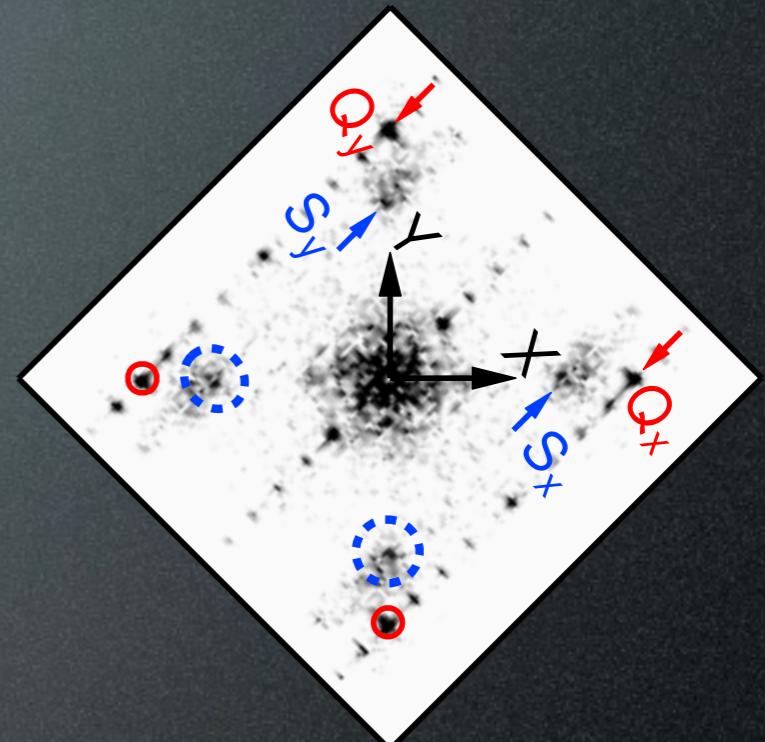


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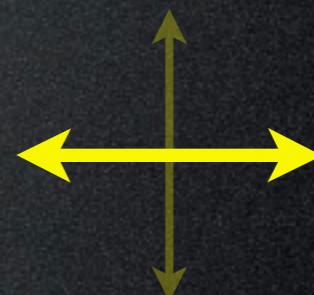


- Nematic OP

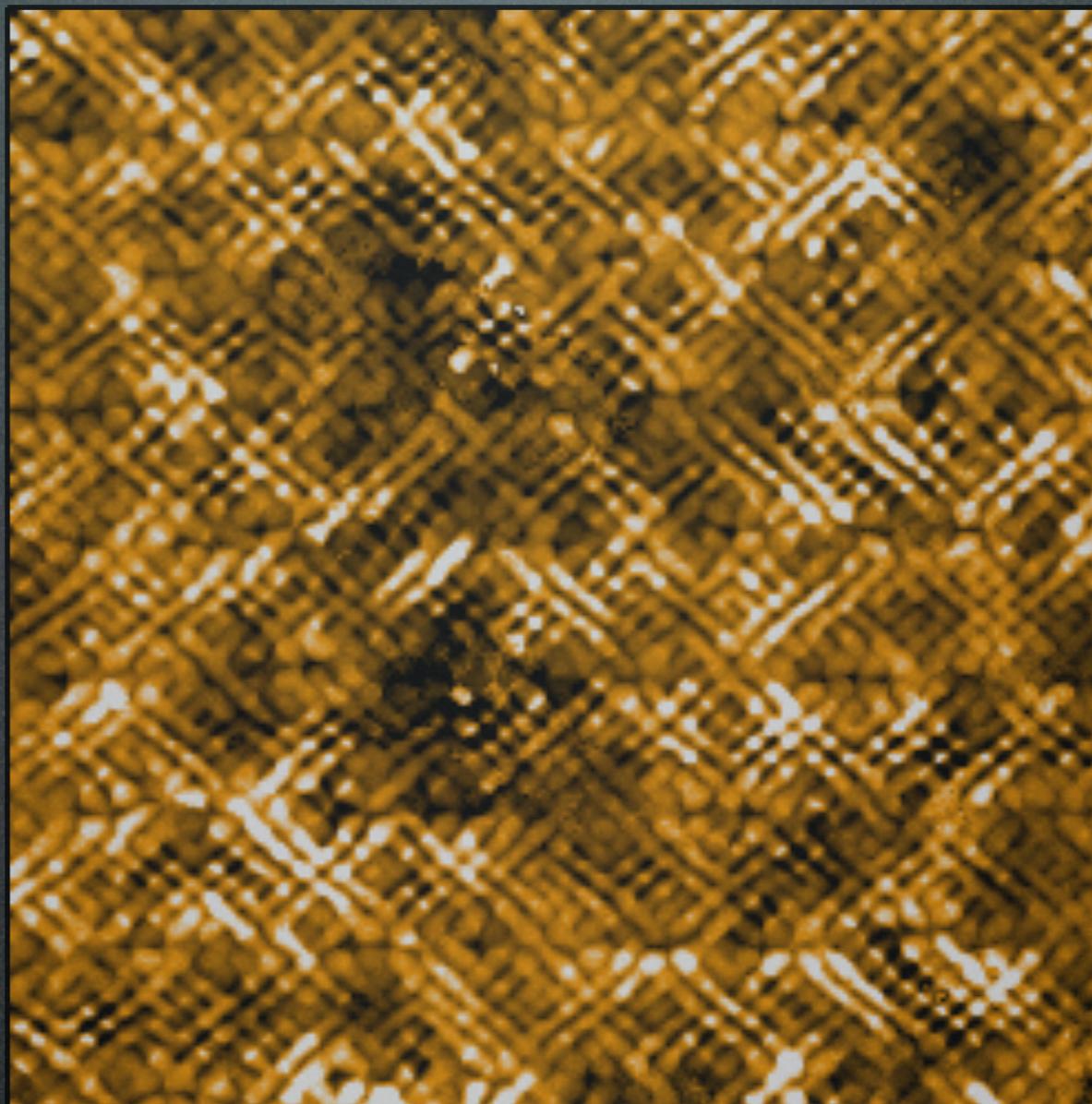
$$\begin{aligned} \mathcal{O}_N[M] &= \frac{1}{2} [\tilde{M}(\vec{Q}_y) - \tilde{M}(\vec{Q}_x) + \tilde{M}(-\vec{Q}_y) - \tilde{M}(-\vec{Q}_x)] \\ &= \text{Re}\tilde{M}(\vec{Q}_y) - \text{Re}\tilde{M}(\vec{Q}_x) \end{aligned}$$

→ Measures C₄ breaking

→ Preserves lattice translation

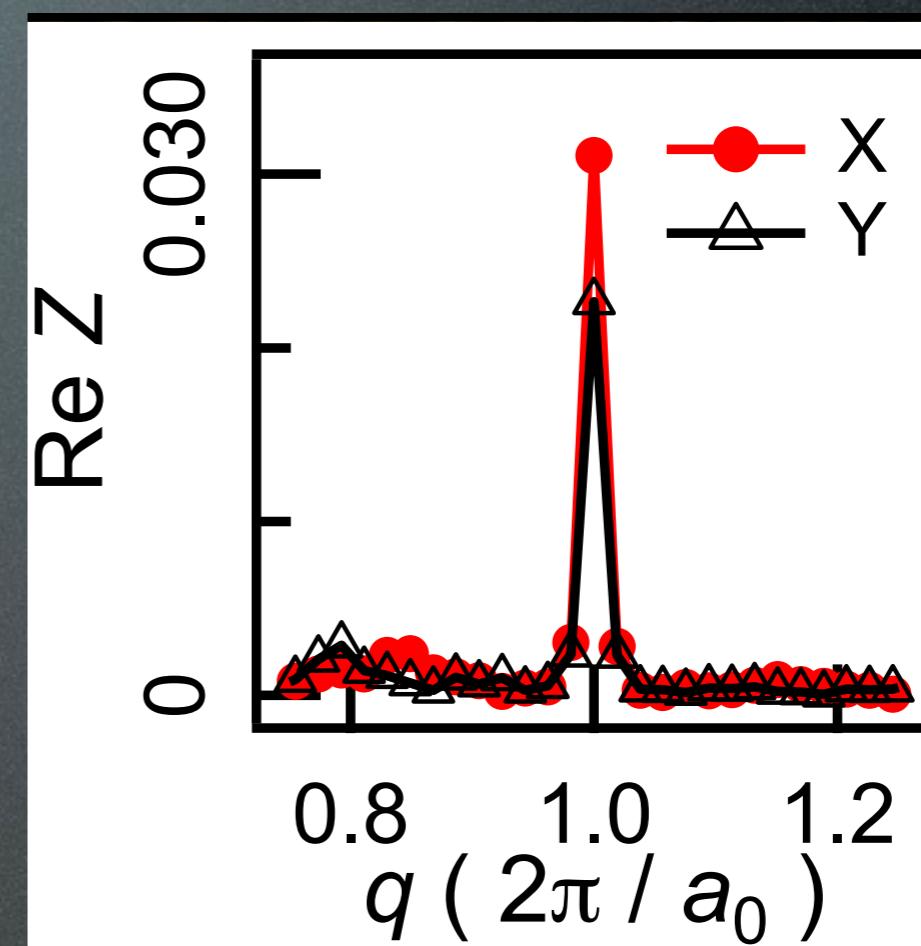
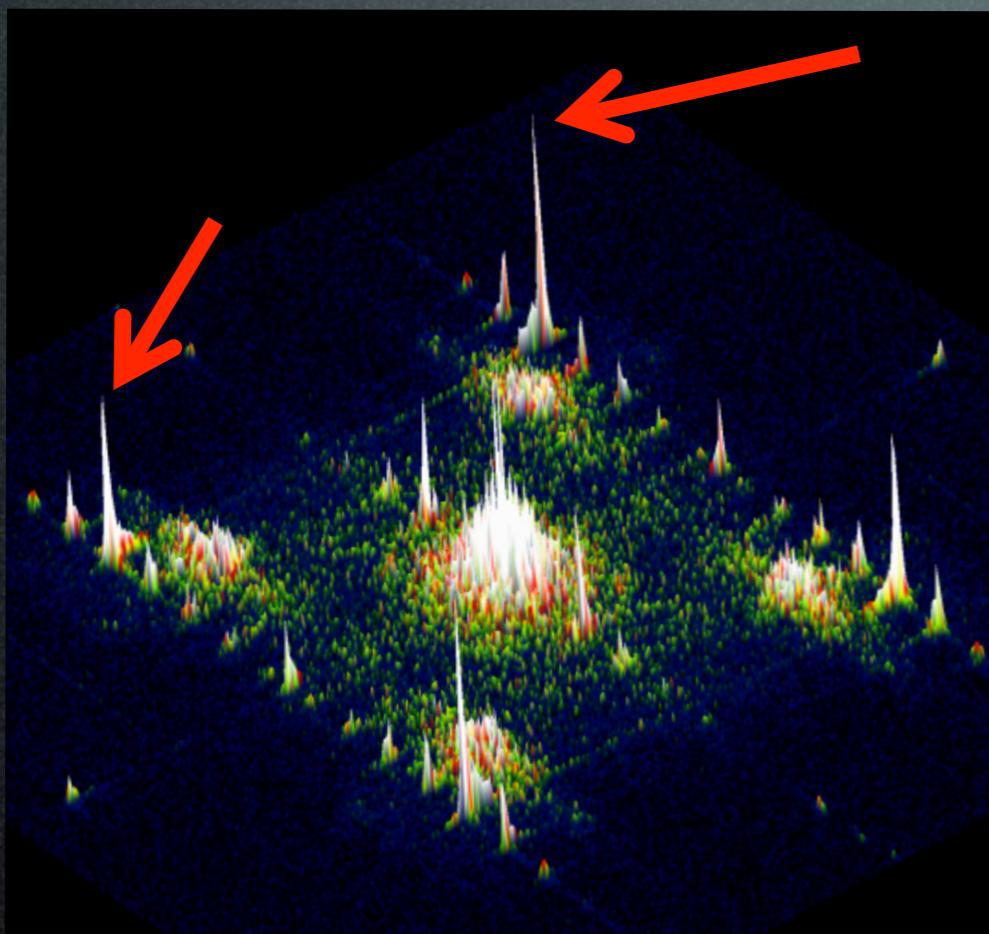


Bragg Peaks



IUC Nematic in BSCCO

Bragg Peaks



IUC Nematic in BSCCO

\mathcal{O}_N intra-unit-cell structure

\mathcal{O}_N intra-unit-cell structure

$$\tilde{Z}(\vec{Q}_x) = \bar{Z}_{\text{Cu}} - \bar{Z}_{\text{O}_x} + \bar{Z}_{\text{O}_y}, \tilde{Z}(\vec{Q}_y) = \bar{Z}_{\text{Cu}} + \bar{Z}_{\text{O}_x} - \bar{Z}_{\text{O}_y}$$

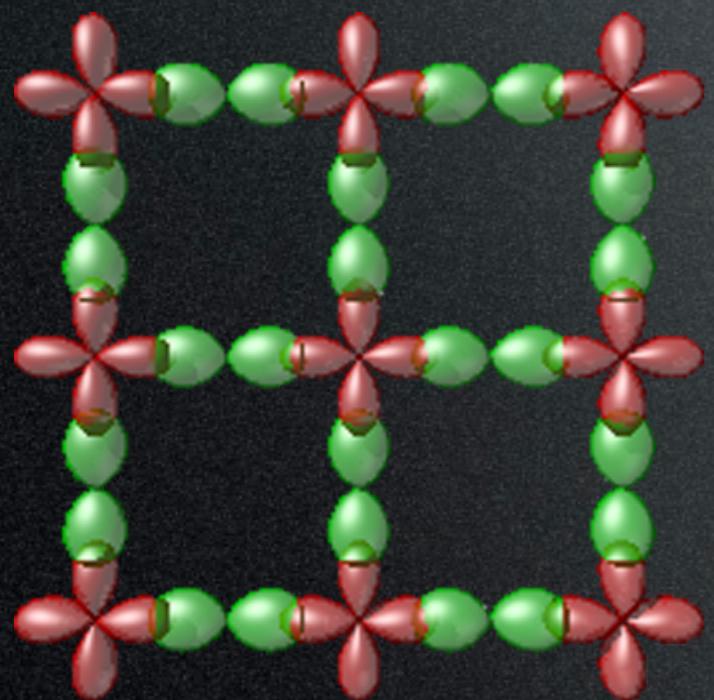
$$\mathcal{O}_N \propto (\bar{Z}_{\text{O}_x} - \bar{Z}_{\text{O}_y}) \quad \text{M.J. Lawler et al, Nature 2010}$$

\mathcal{O}_N intra-unit-cell structure

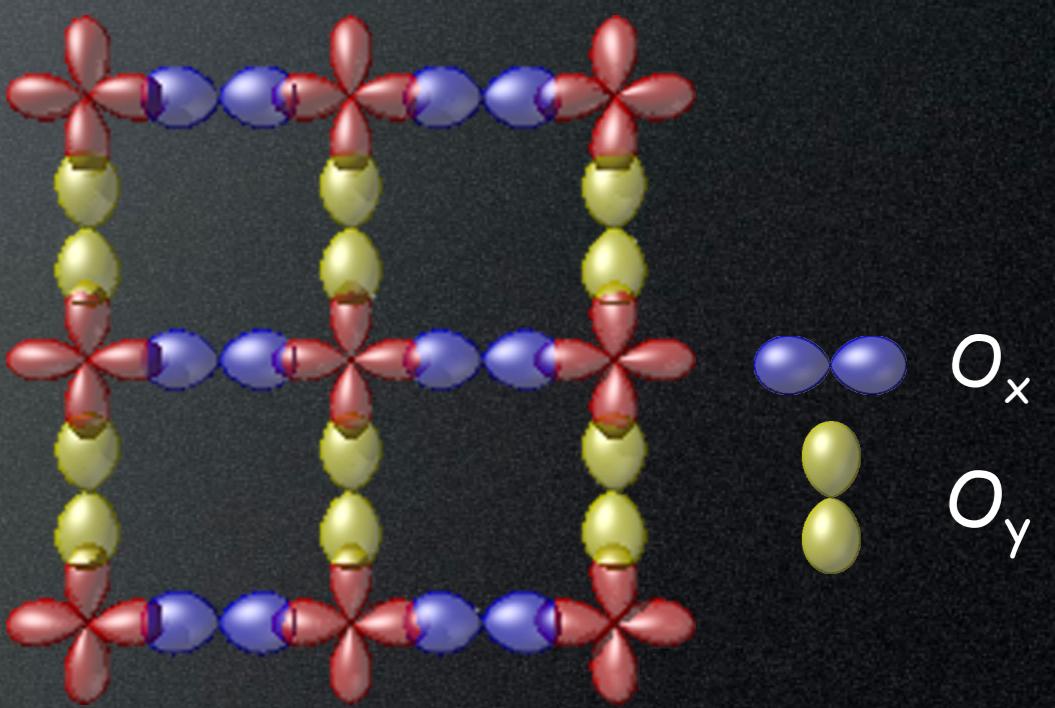
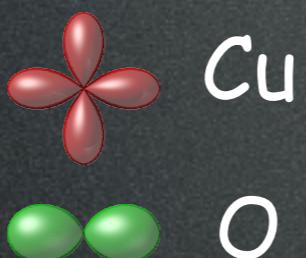
$$\tilde{Z}(\vec{Q}_x) = \bar{Z}_{\text{Cu}} - \bar{Z}_{O_x} + \bar{Z}_{O_y}, \tilde{Z}(\vec{Q}_y) = \bar{Z}_{\text{Cu}} + \bar{Z}_{O_x} - \bar{Z}_{O_y}$$

$$\mathcal{O}_N \propto (\bar{Z}_{O_x} - \bar{Z}_{O_y}) \quad \text{M.J. Lawler et al, Nature 2010}$$

→ Intra-unitcell pattern including O sites



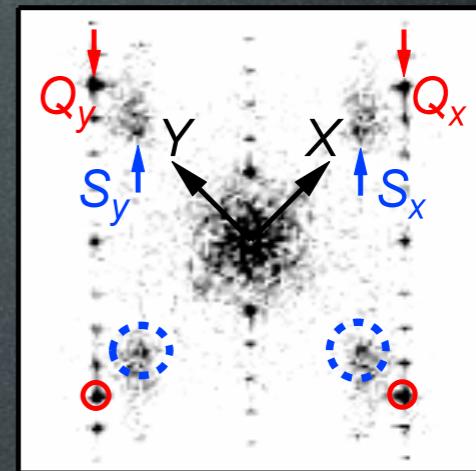
CuO₂ plane



Intra unitcell Nematic:
 $C_4 \rightleftharpoons C_2$

Local version of Nematic OP $\mathcal{O}_N(\vec{x})$

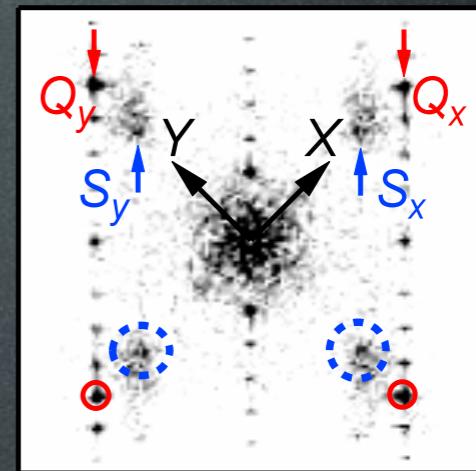
- How strongly do each point \vec{x} contribute to a Q space peak $\tilde{M}(\vec{Q})$?



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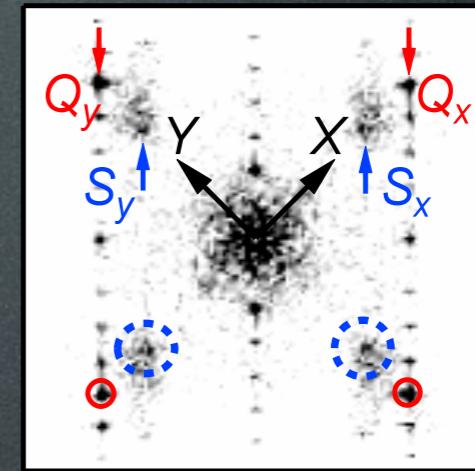
$$\tilde{M}(\vec{Q}, \vec{x}) = \text{low pass}_{\Lambda} \left[M(\vec{x}) e^{i \vec{Q} \cdot \vec{x}} \right]$$



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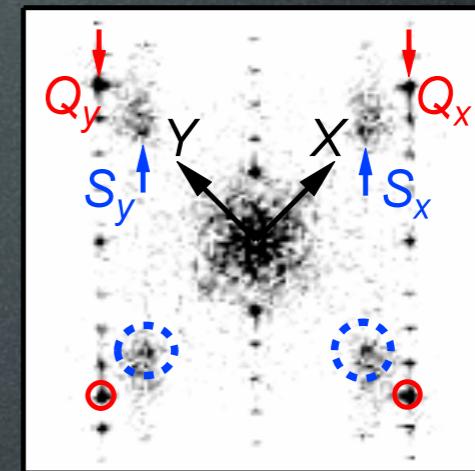
- Local order parameter:

$$\mathcal{O}_N[M](\vec{x}) = \frac{1}{2} [\tilde{M}(\vec{Q}_y, \vec{y}) - \tilde{M}(\vec{Q}_x, \vec{x}) + \tilde{M}(-\vec{Q}_y, \vec{x}) - \tilde{M}(-\vec{Q}_x, \vec{x})]$$

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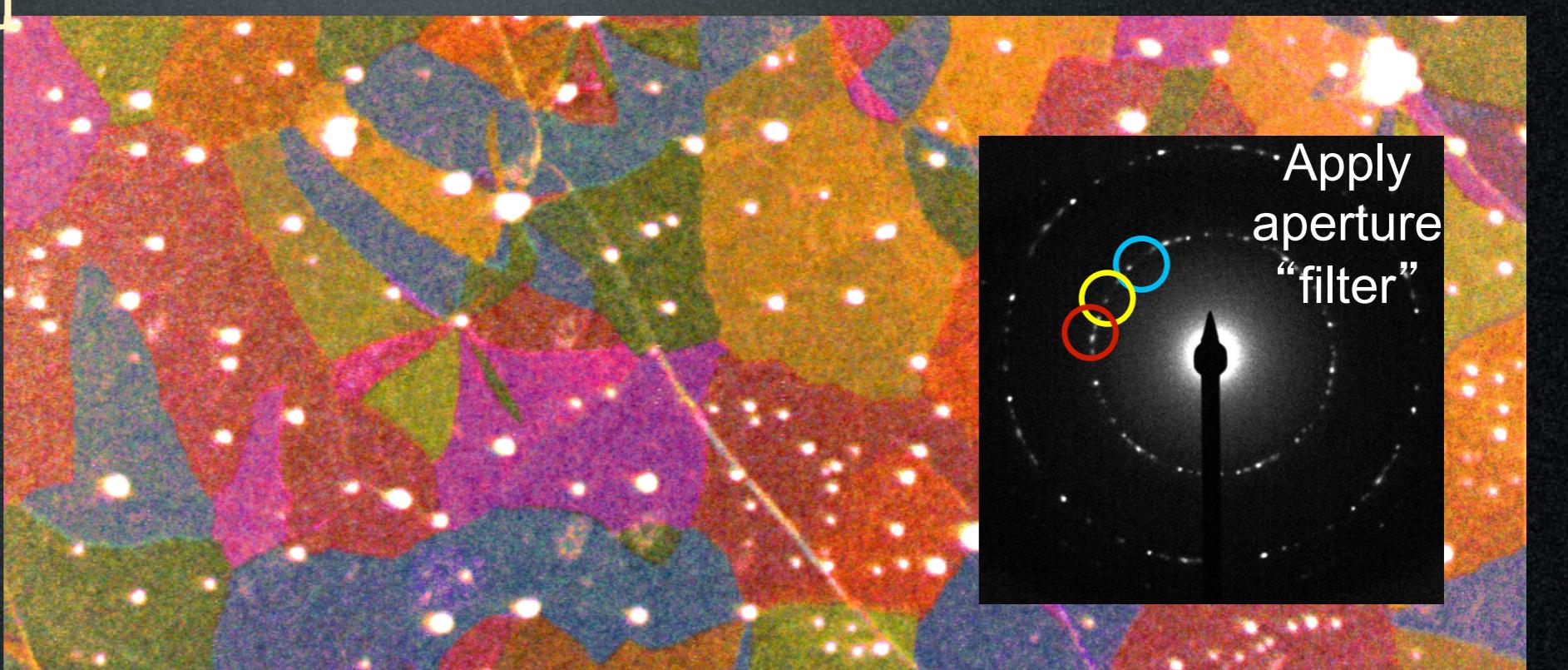
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- ala TEM on graphene
[Huang et al,
Nature 2011]

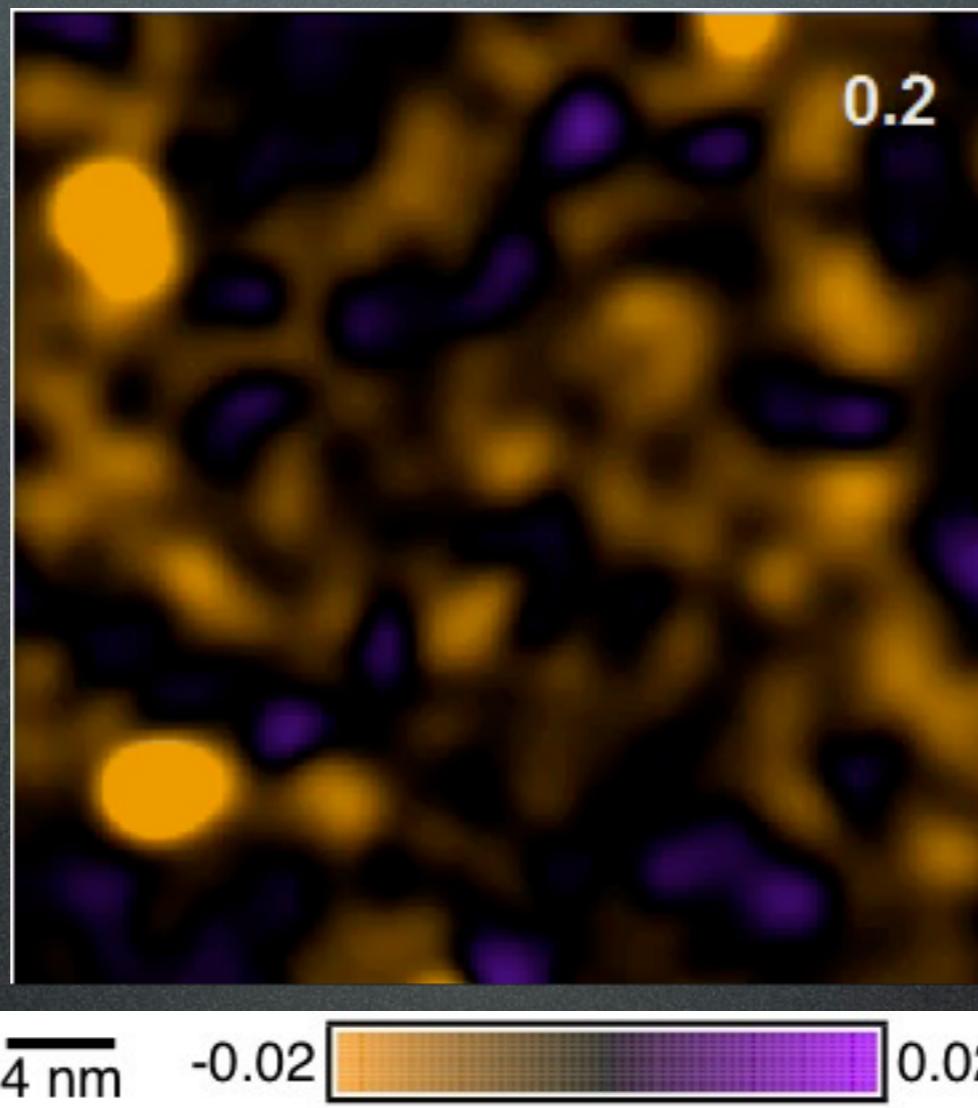
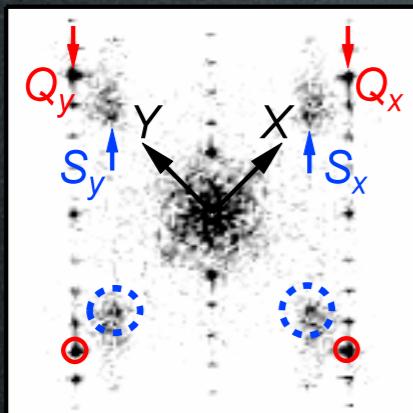


$\vec{Q} = 0$ Nematic Order

- Shift Q_x, Q_y to origin



- Low pass filter (long distance physics)

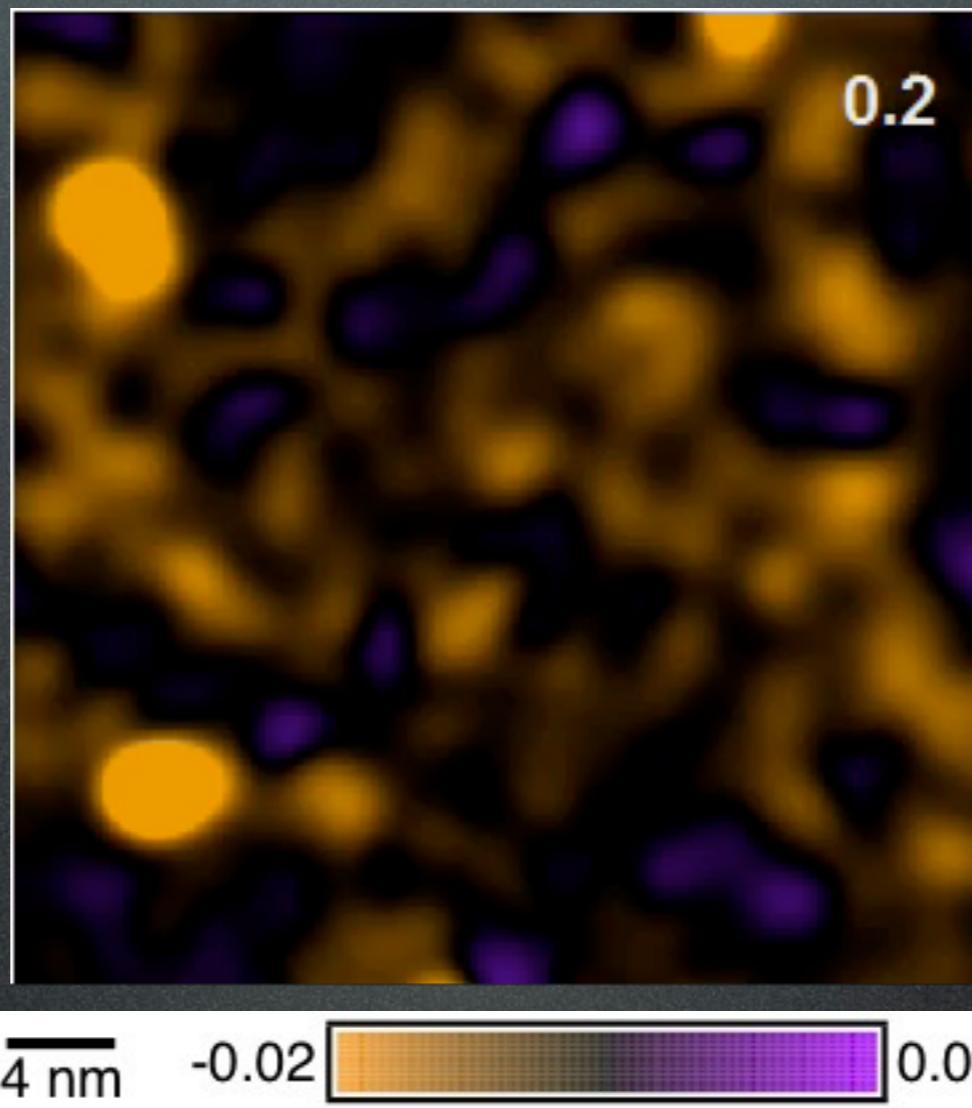
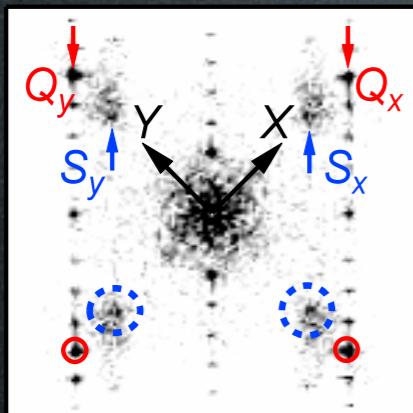


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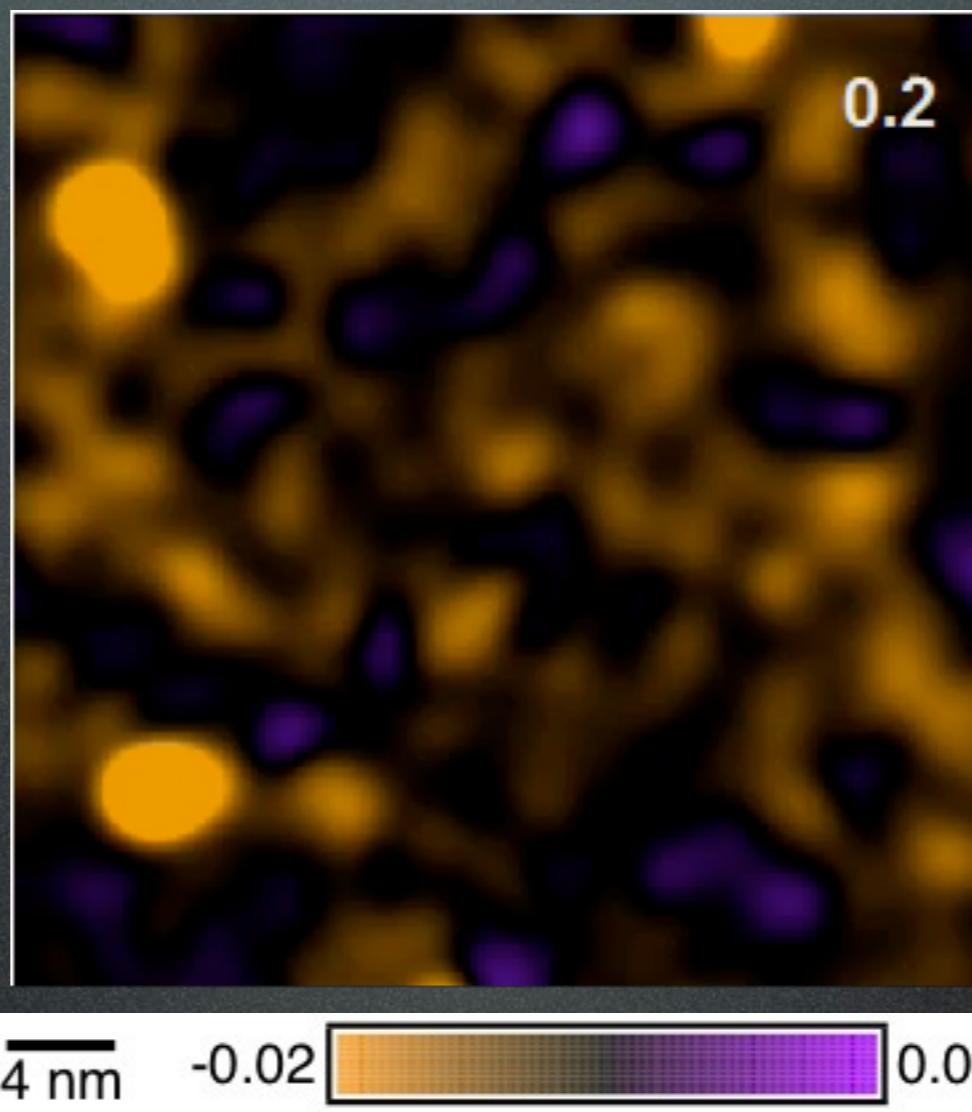
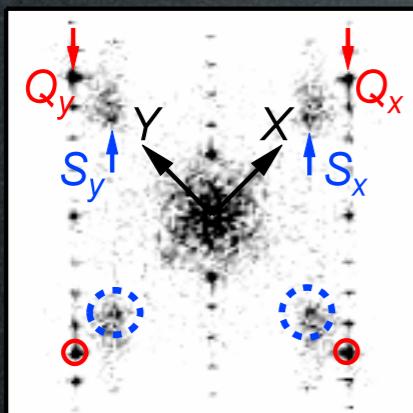


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Orders near pseudogap energy scale

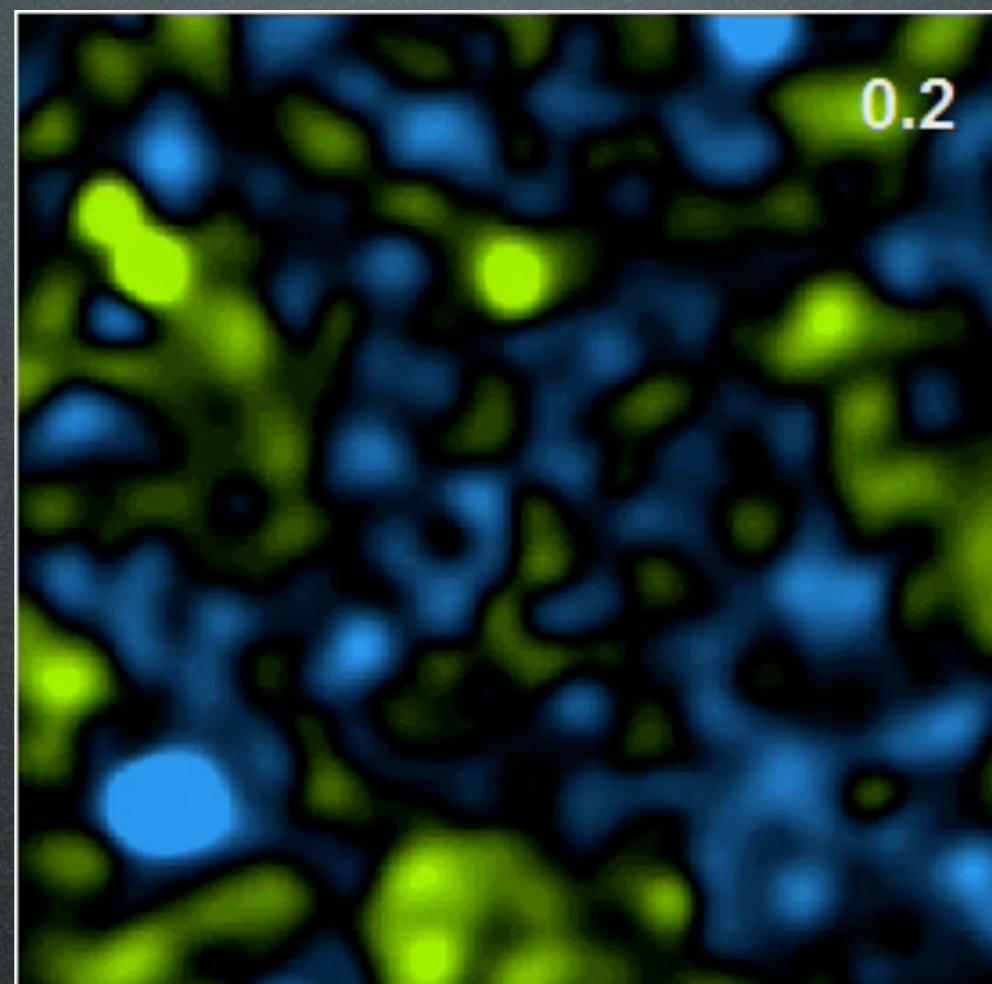
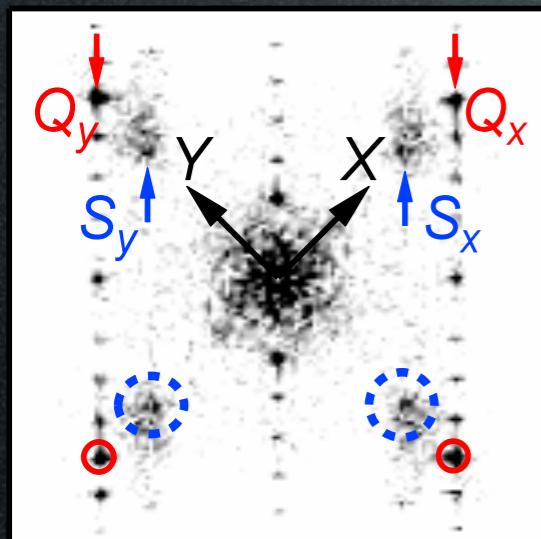
Lawler, Fujita et al, Nature 2010

$\vec{Q} \neq 0$ Smectic domains

- Shift S_x, S_y to origin (“tune to the channel”)



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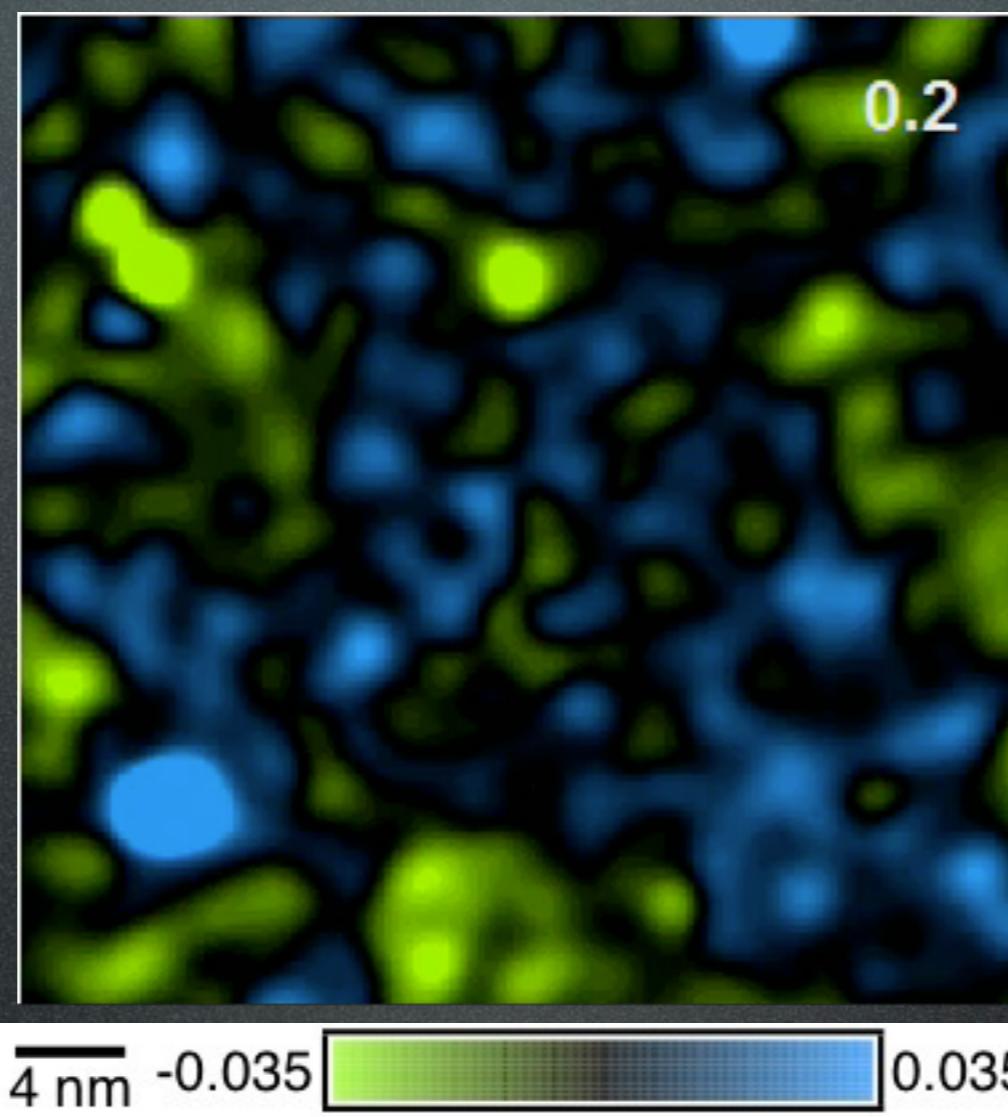
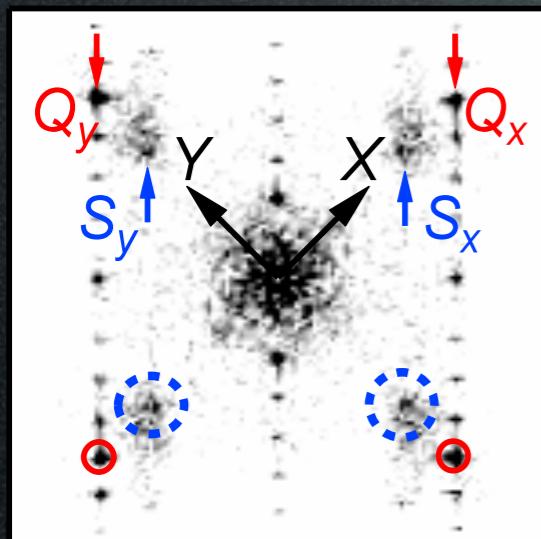
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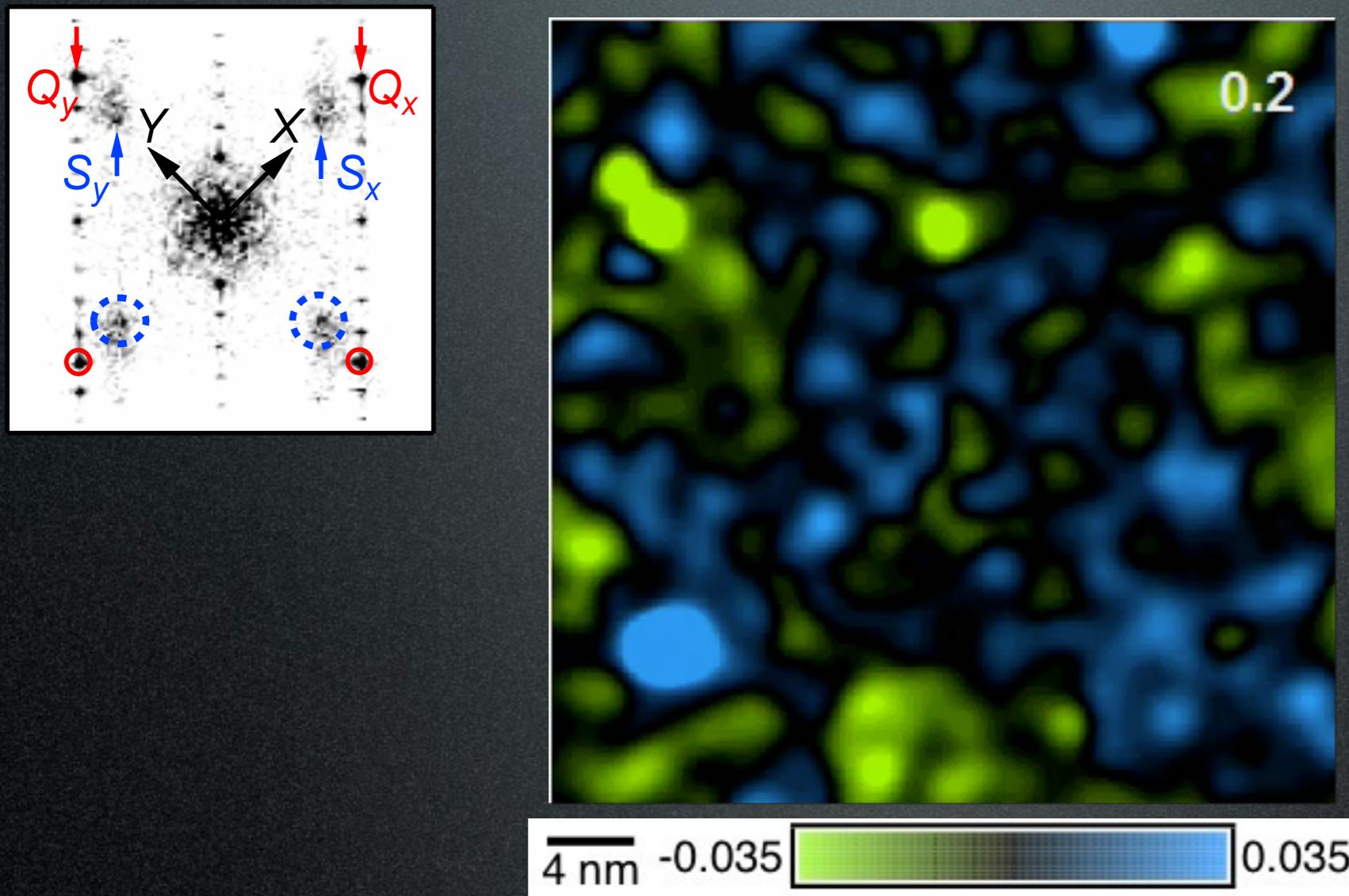
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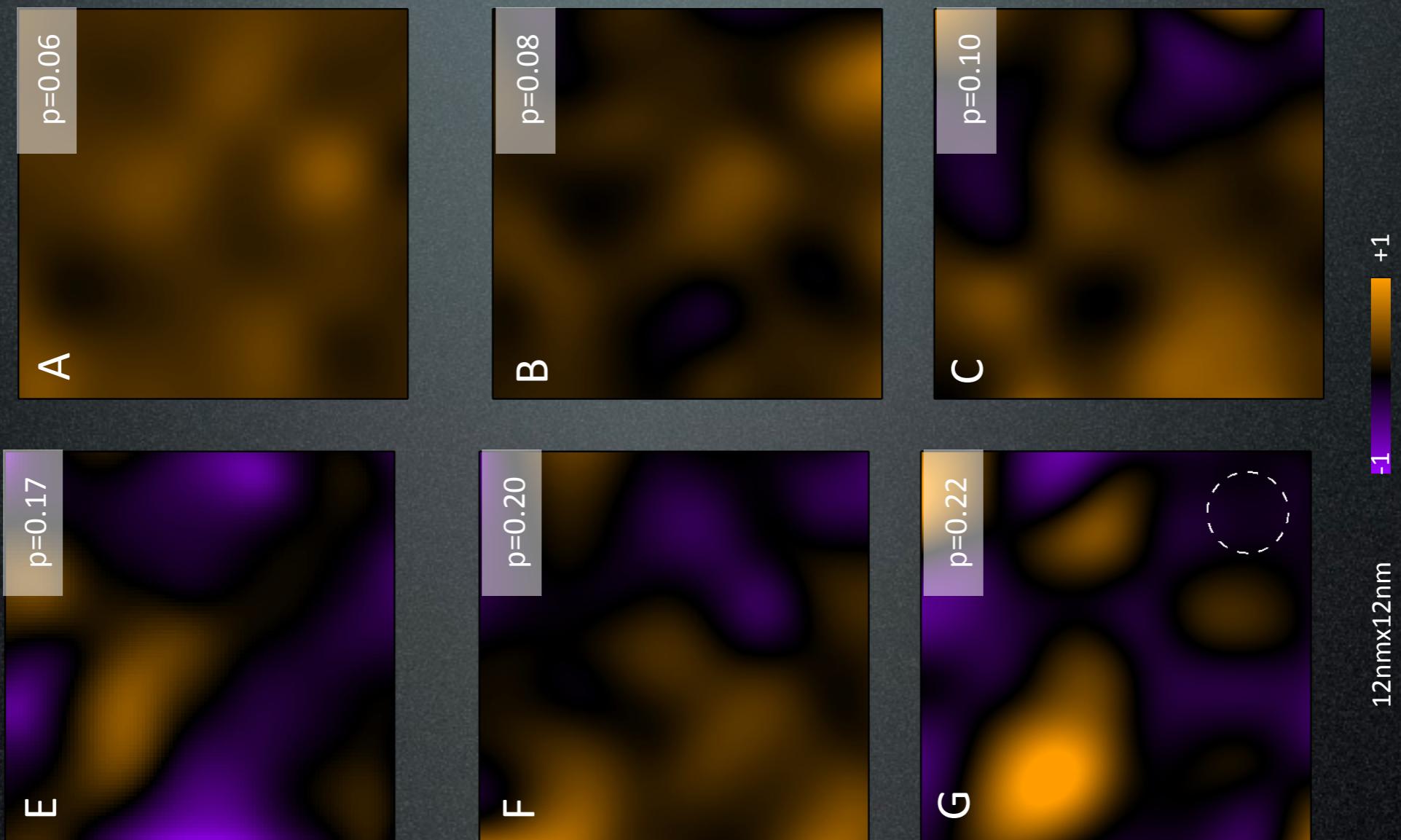
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Severely fluctuating in space at all energies

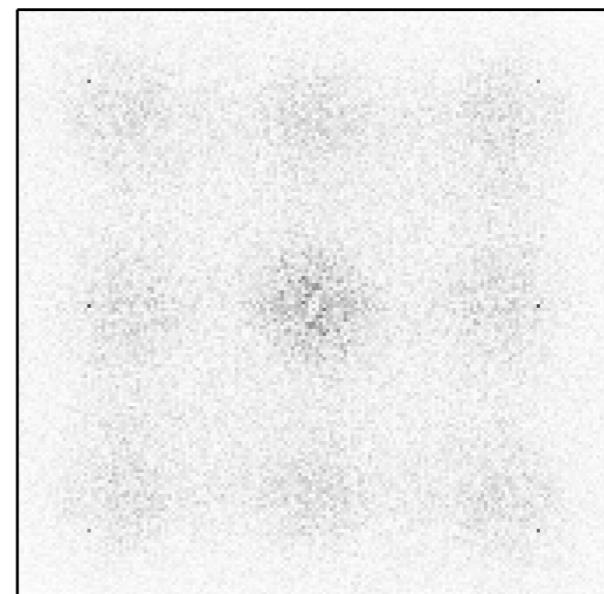
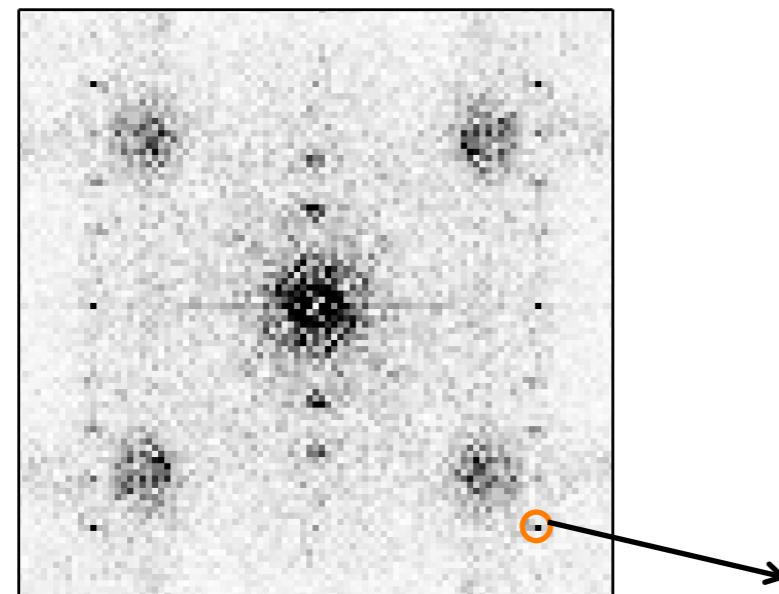
:Consistent with previous studies

Howald et al (2003) Kohsaka et al (2008) Robertson et. al. (2006) Del Meastro et. al. (2006)

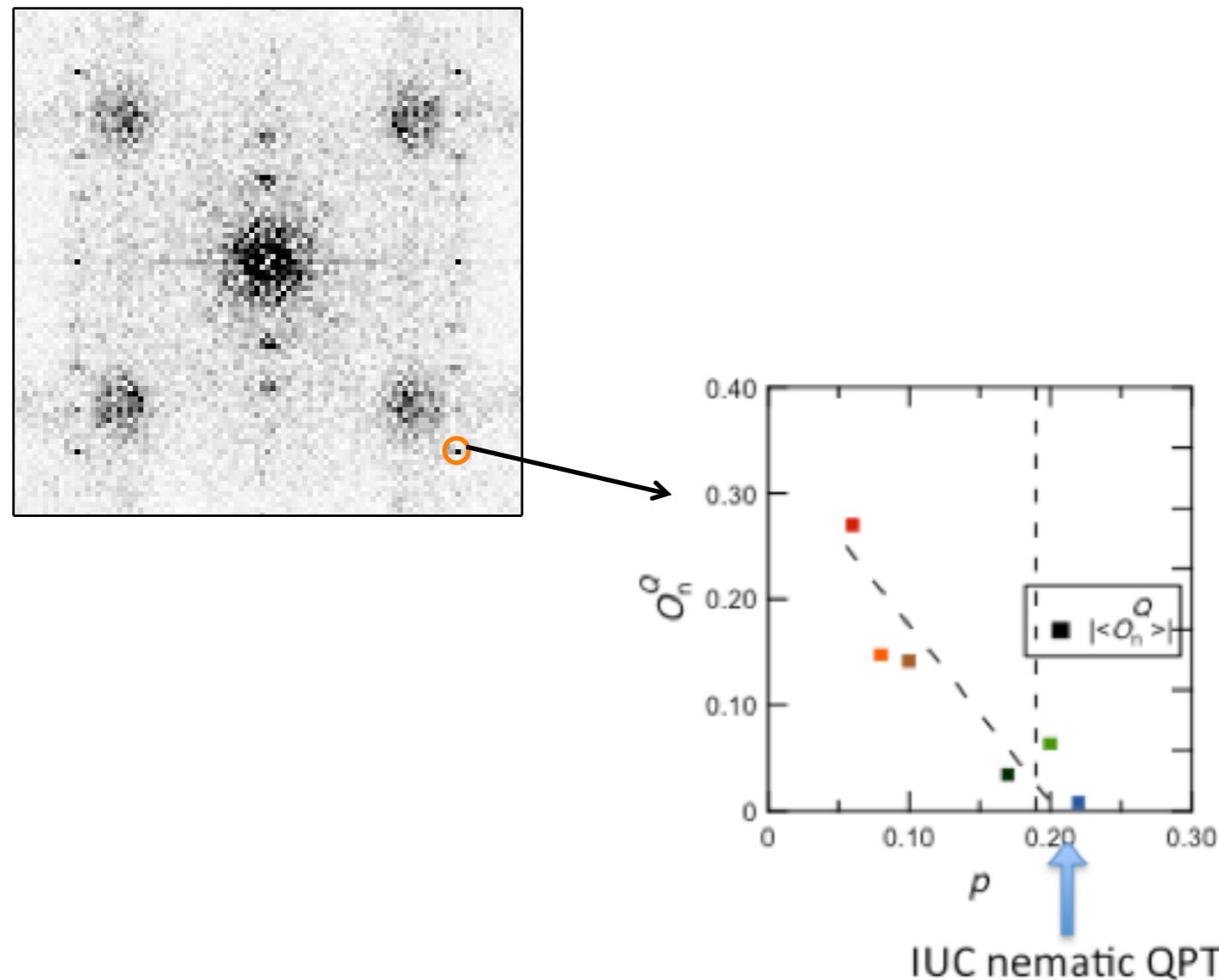
DOPING DEPENDENCE OF Q=0 SYMMETRY BREAKING



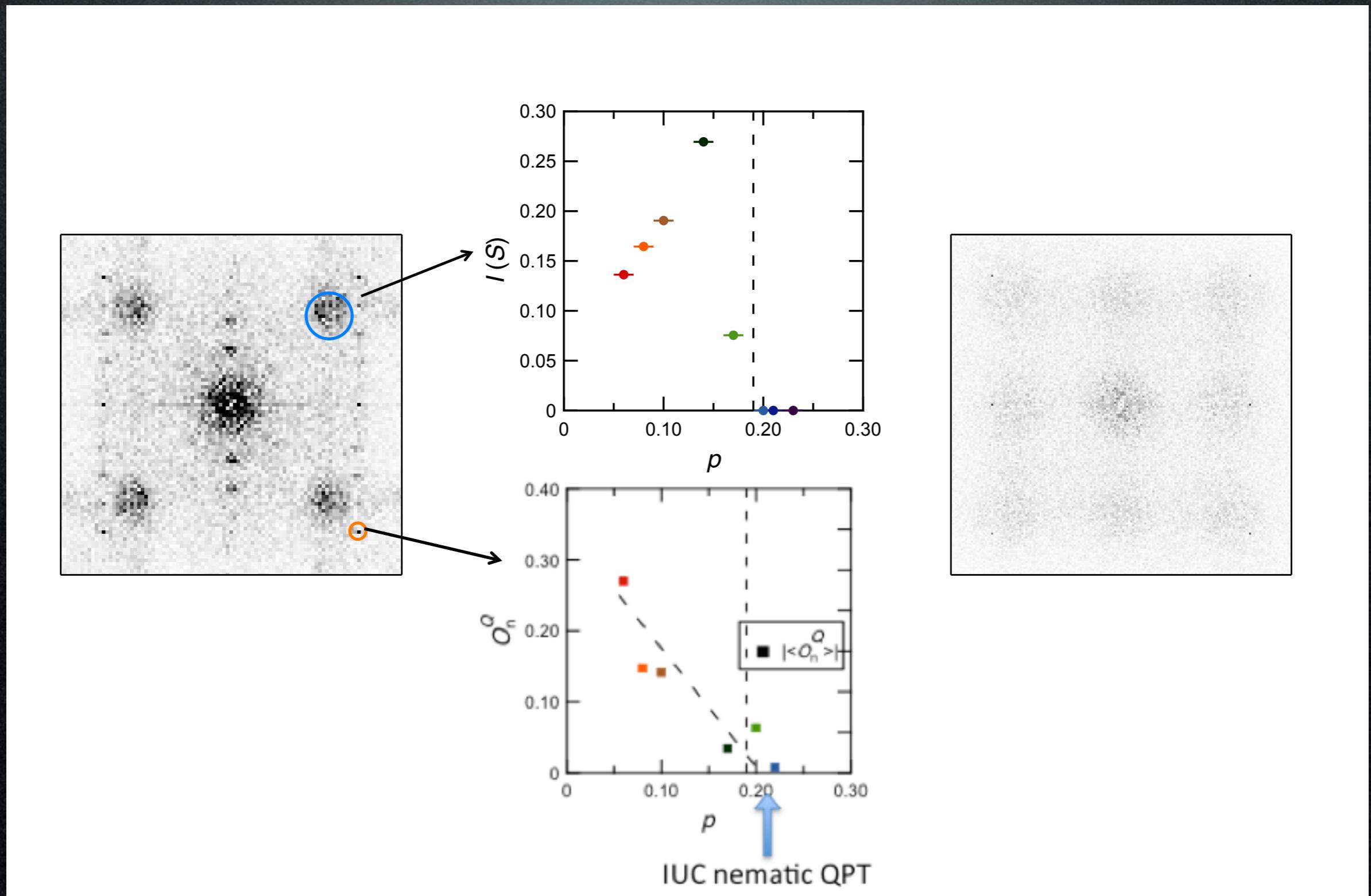
Doping Dependence of Q=0 IUC Nematic



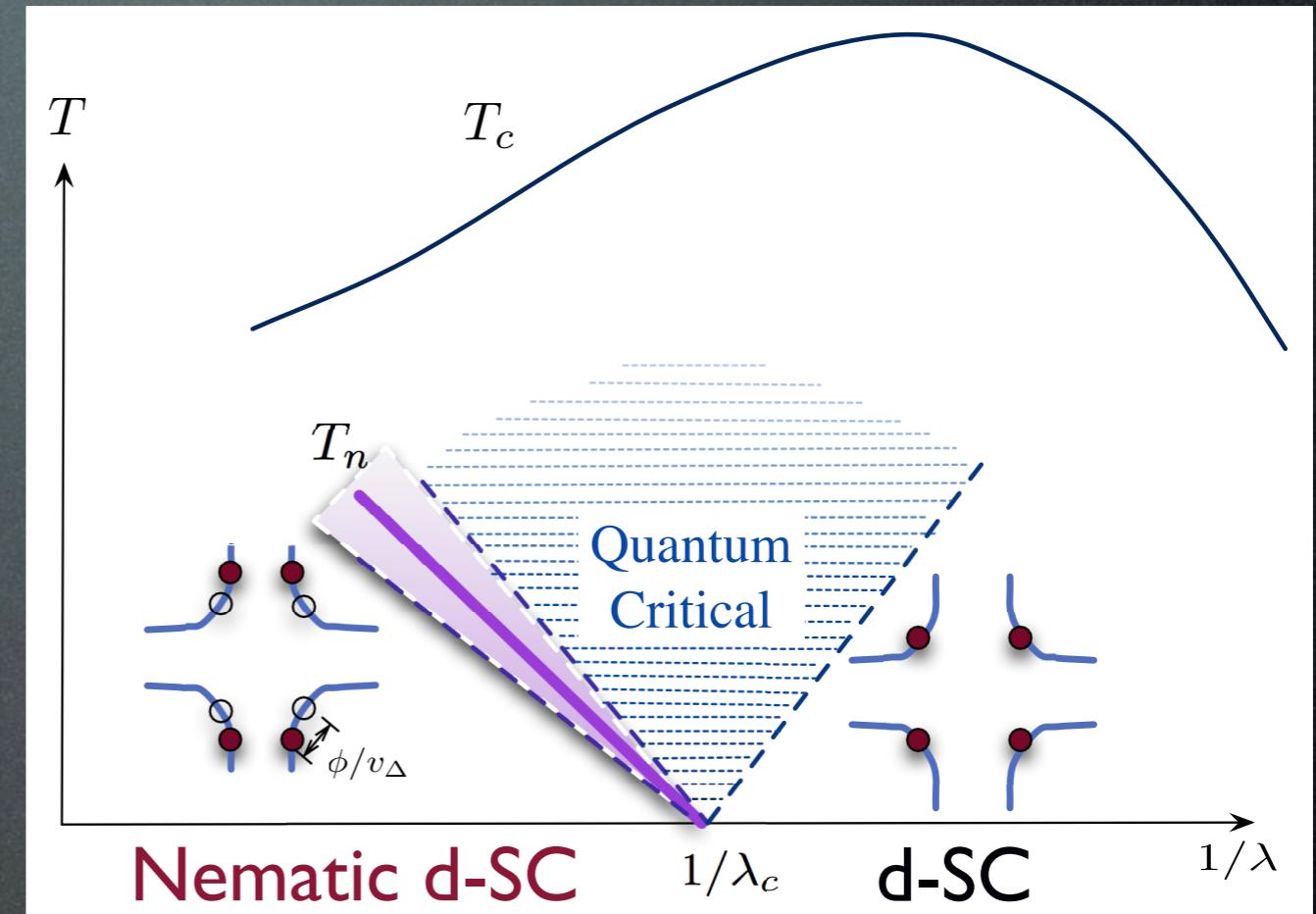
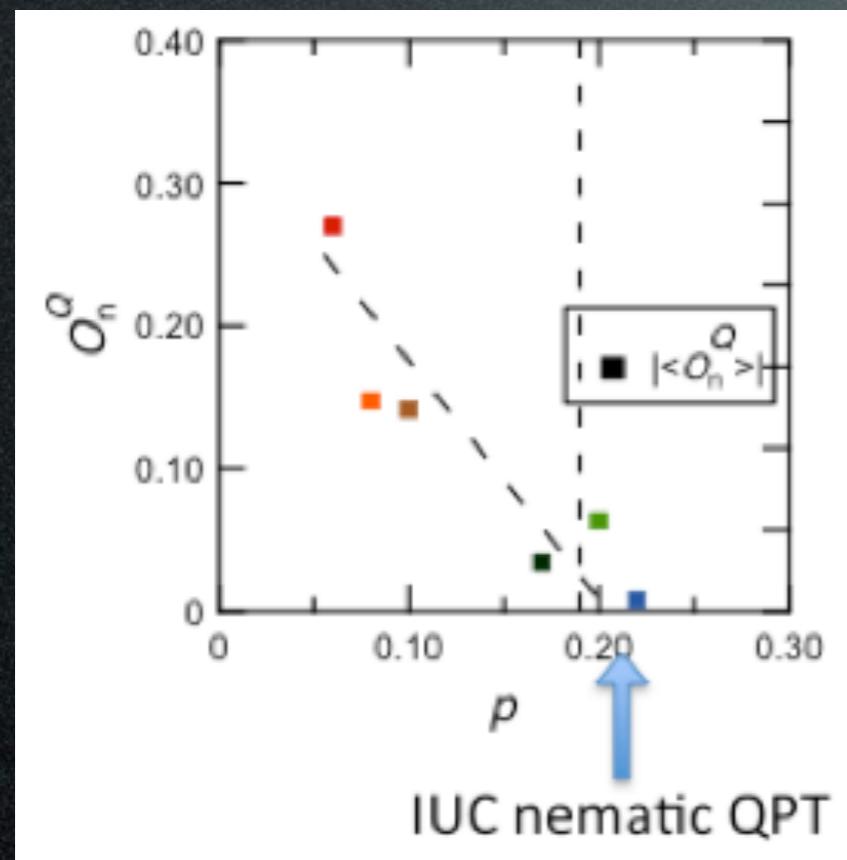
Doping Dependence of Q=0 IUC Nematic



Doping Dependence of $Q=0$ and $Q \neq 0$ Symmetry Breaking

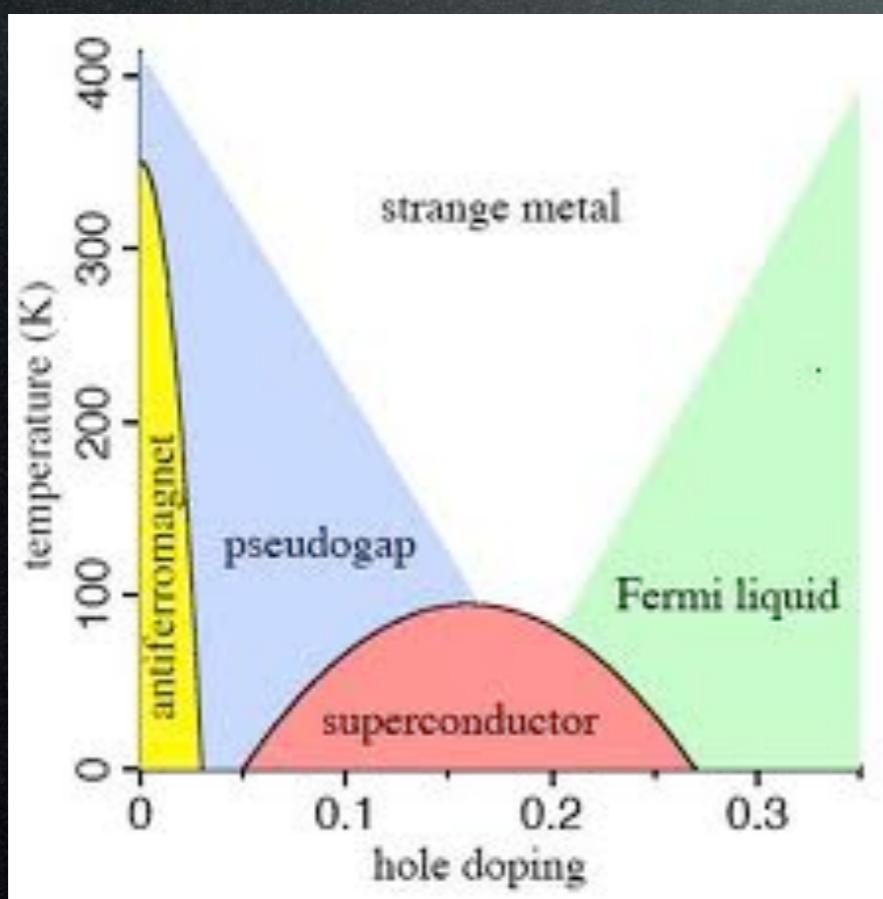


Earlier study of Nematic quantum criticality



Kim et. al., PRB 77, 184514 (2008)

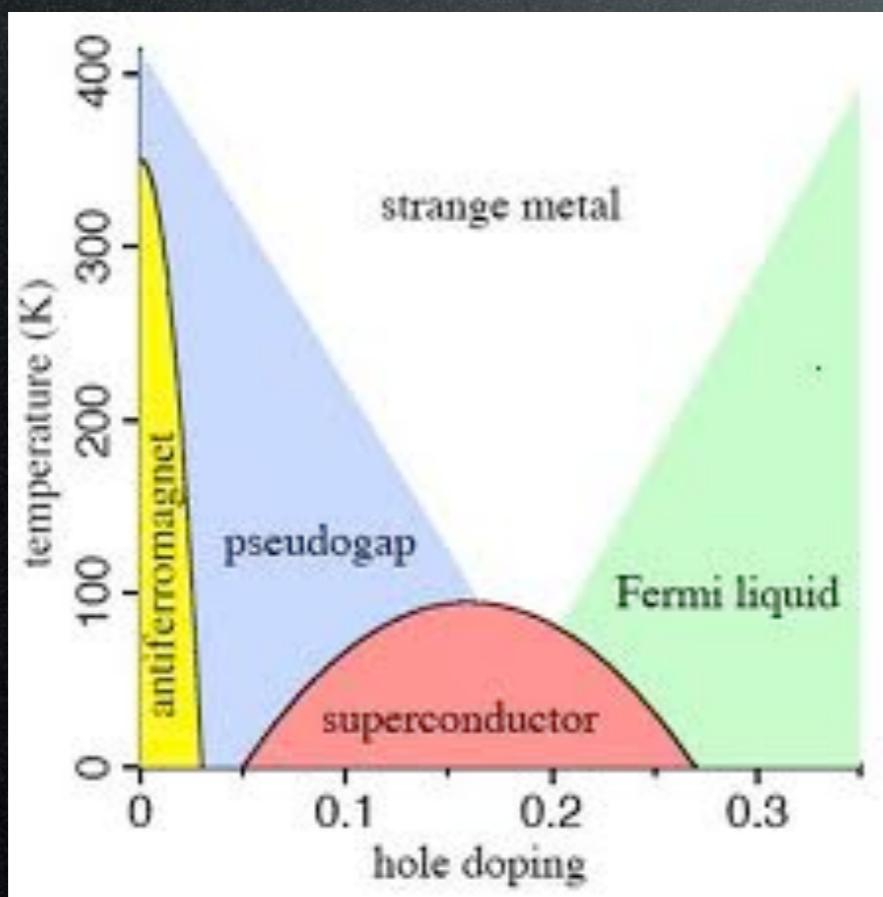
The Phase Diagram, summary



Lawler et al, Nature 2010
Fujita et al, Science 2014

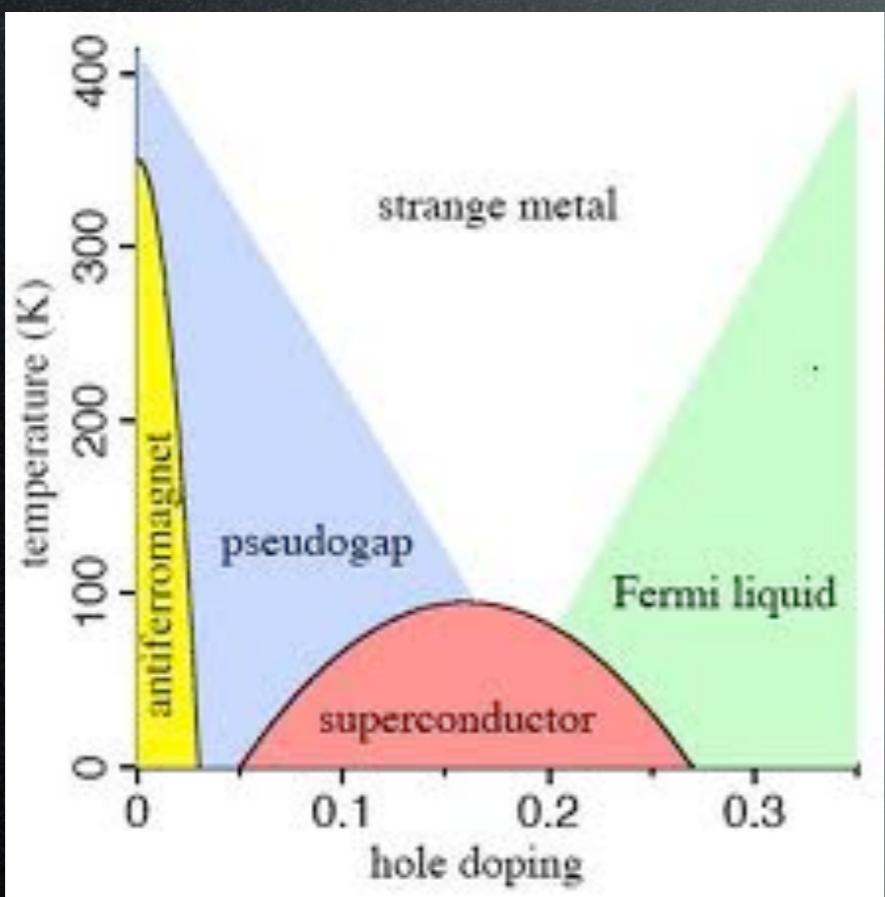
The Phase Diagram, summary

- Long-range IUC symmetry breaking in STM data of pseudogap states

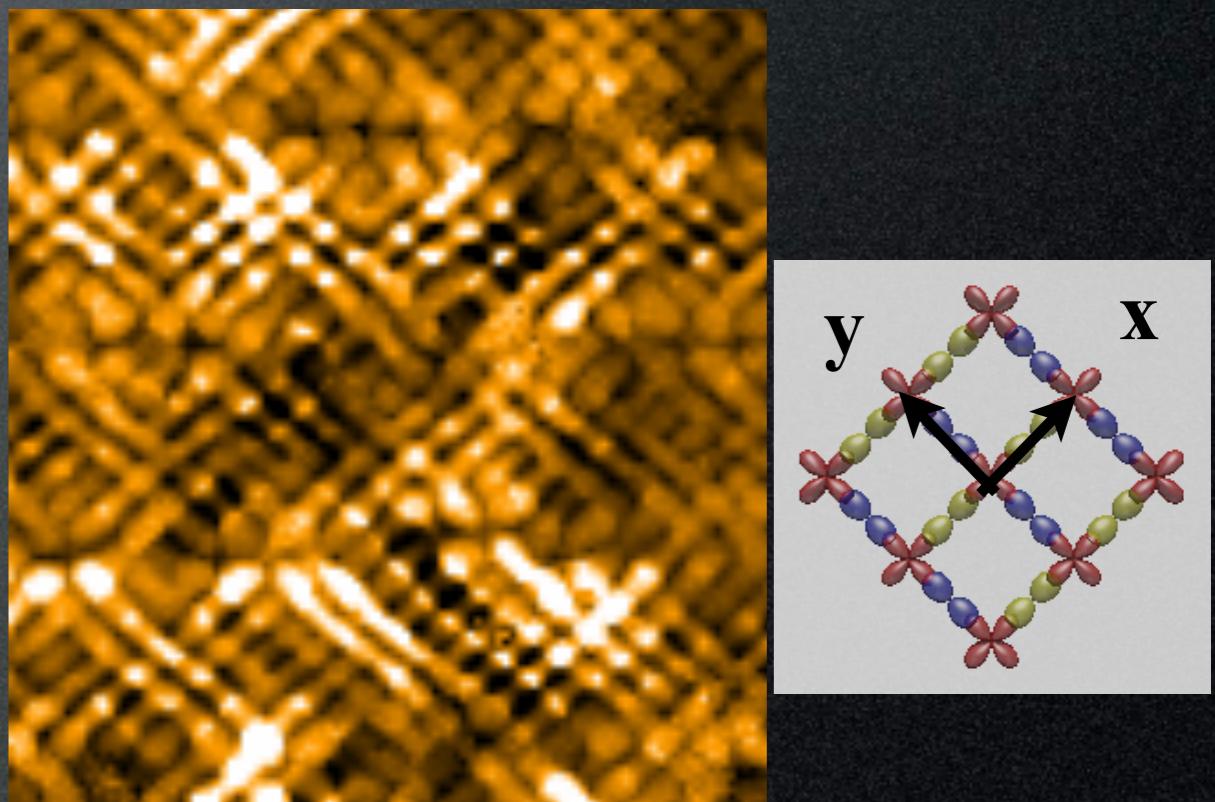


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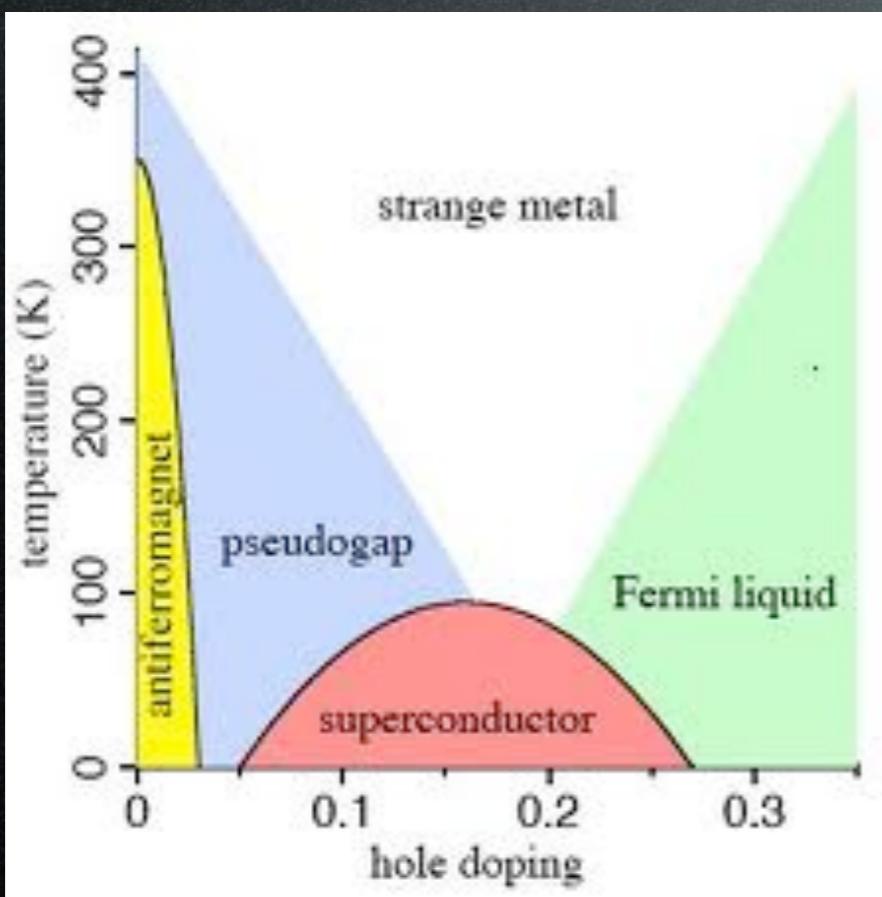
$$\mathcal{O}_N[M] \propto \bar{M}_{O_x} - \bar{M}_{O_y}$$



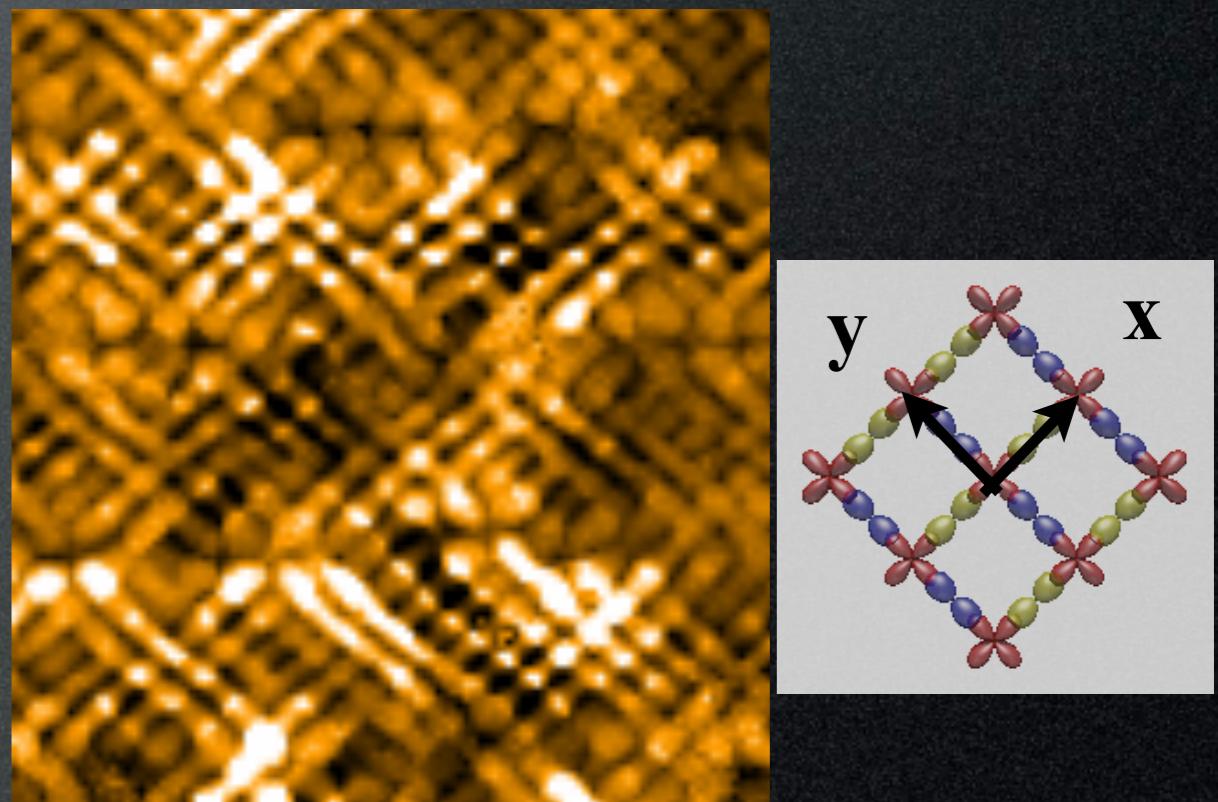
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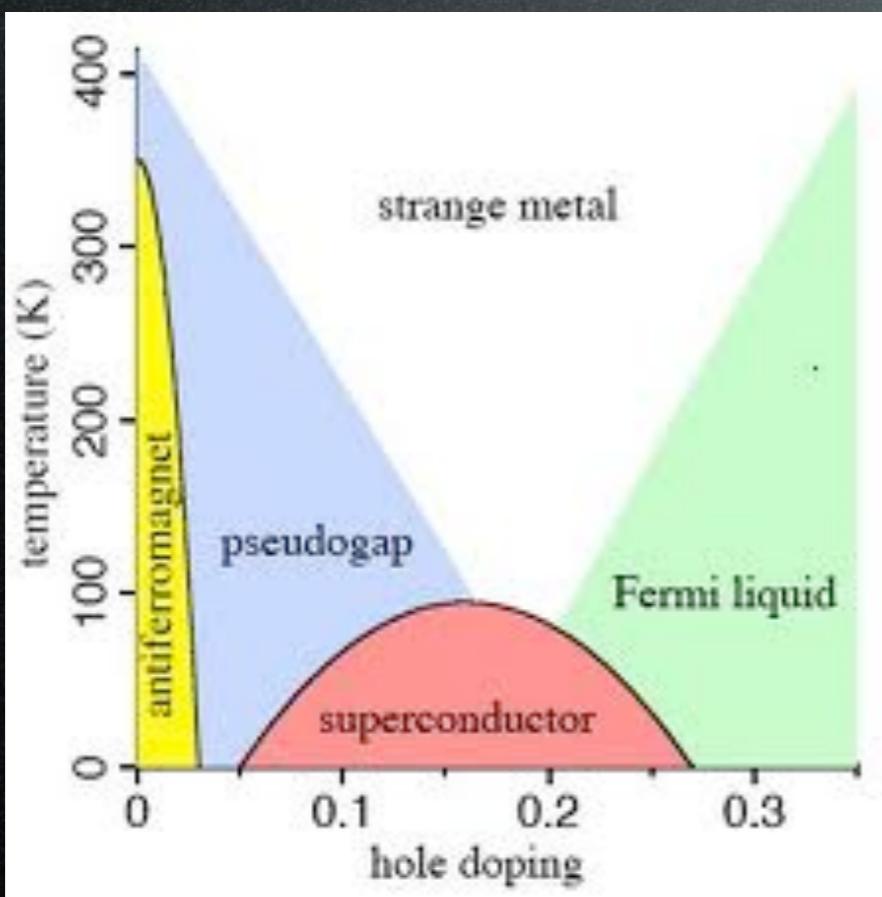


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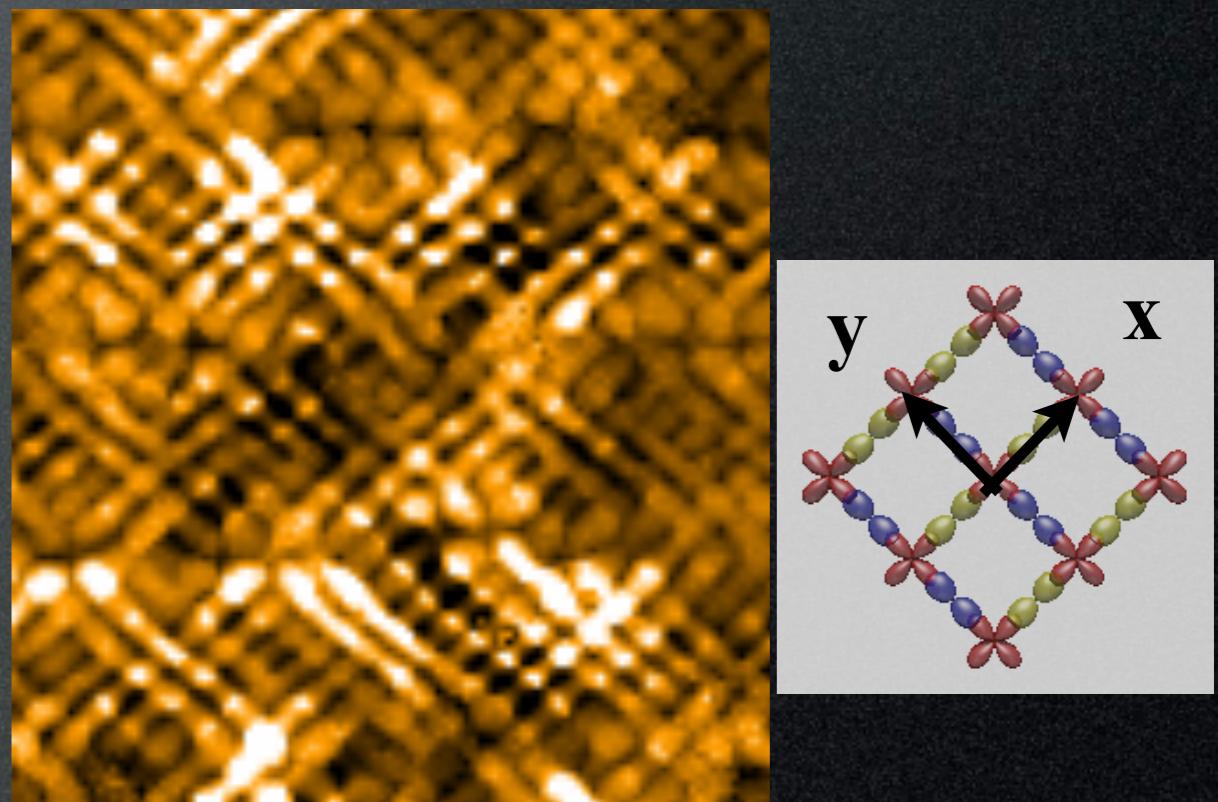
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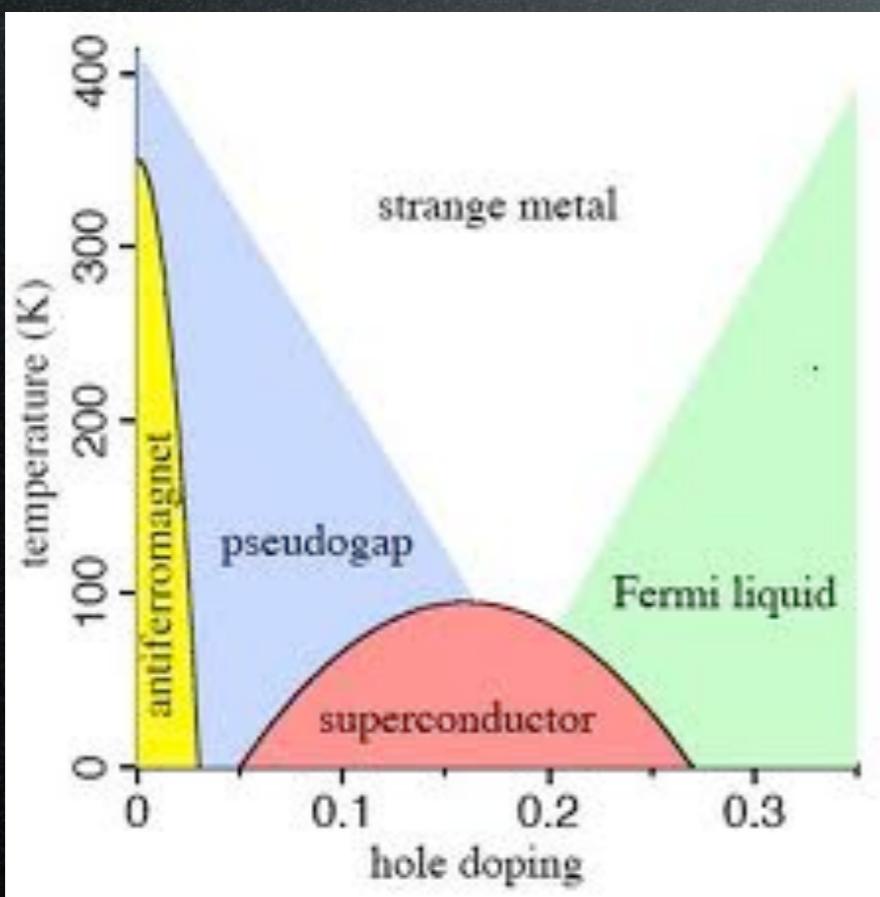


Lawler et al, Nature 2010
Fujita et al, Science 2014

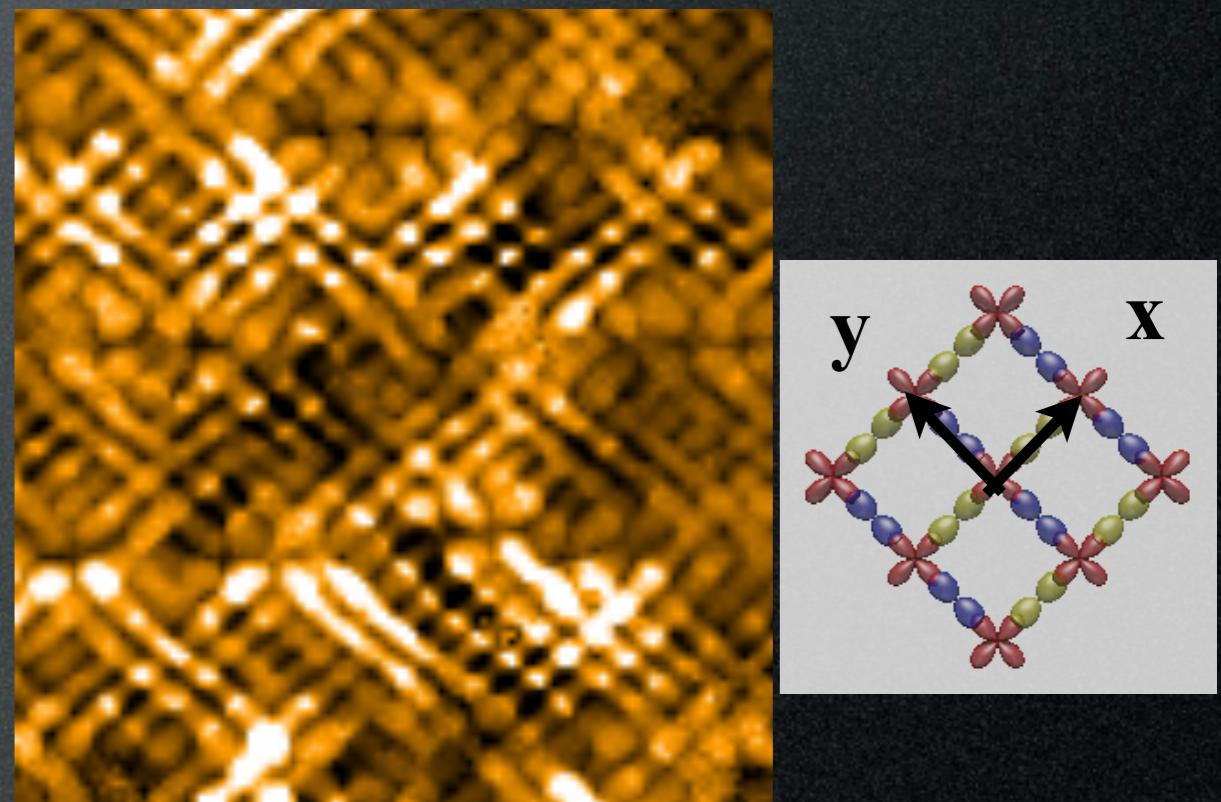
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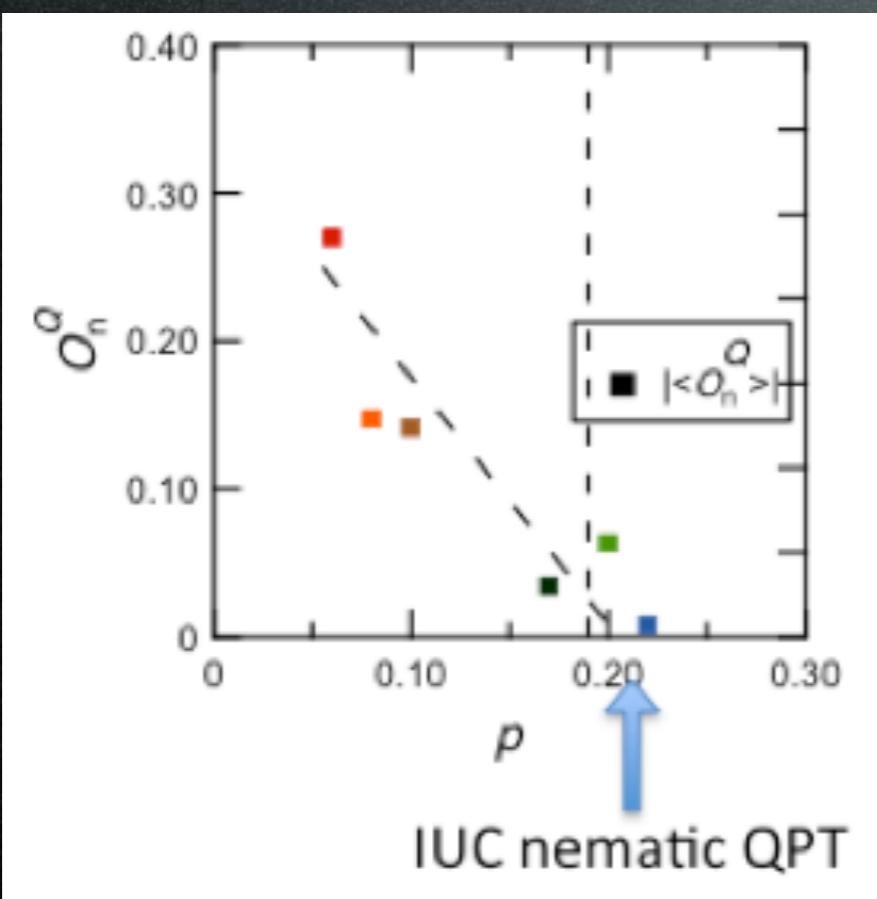


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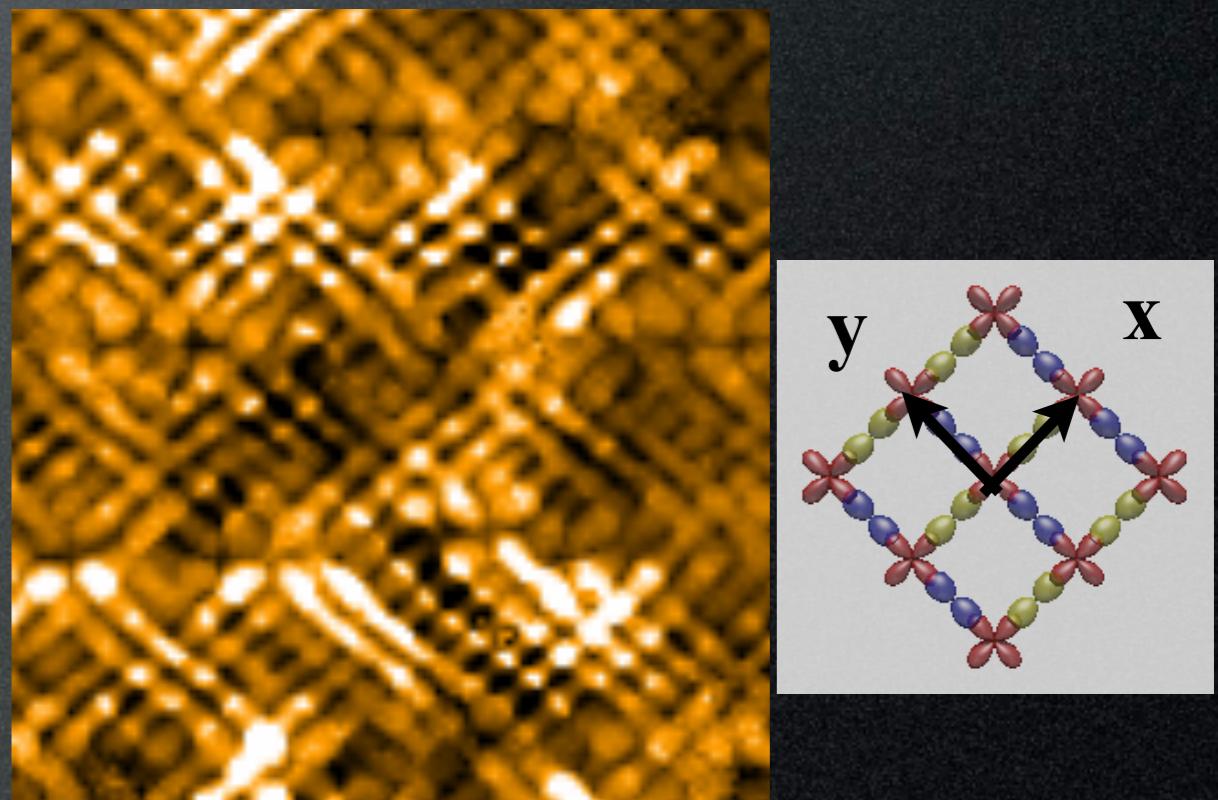
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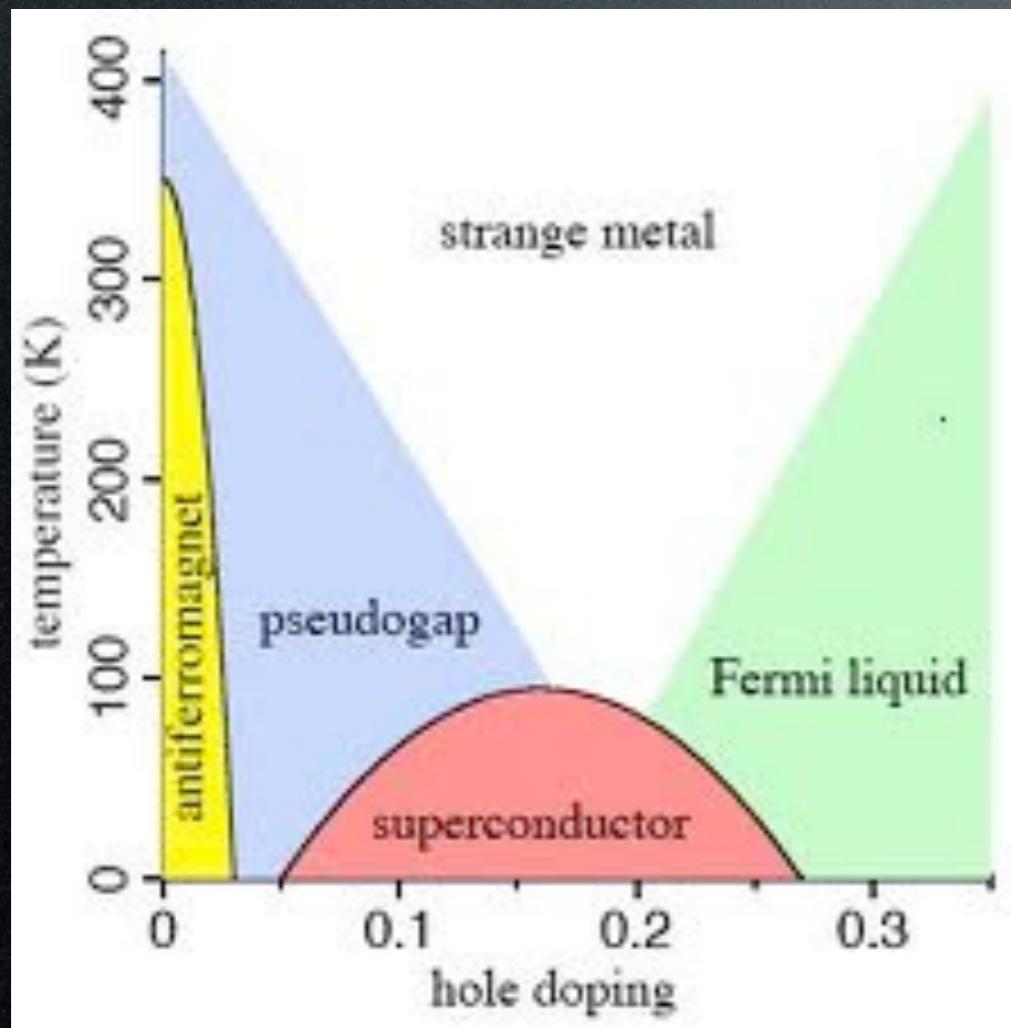
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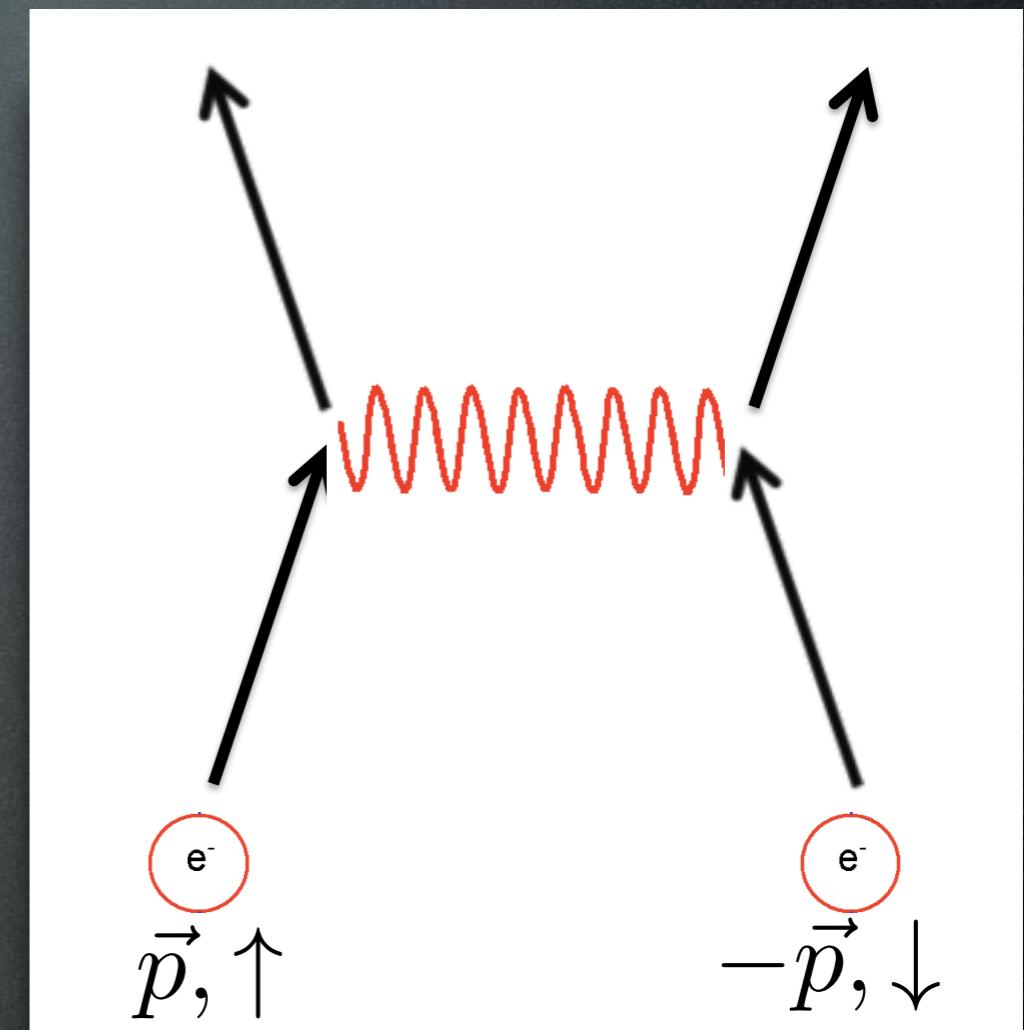
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Key Questions in High- T_c Superconductivity:

The Phase Diagram?

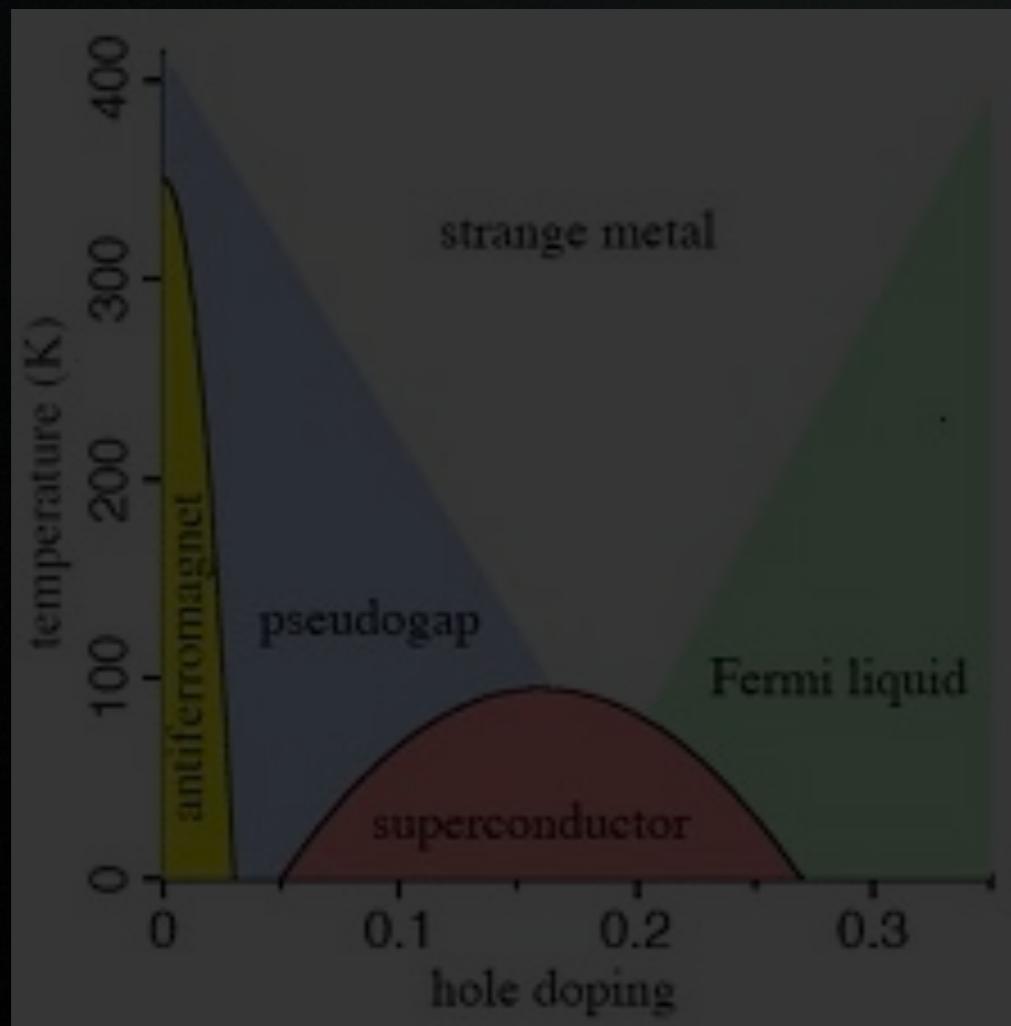


The Mechanism?

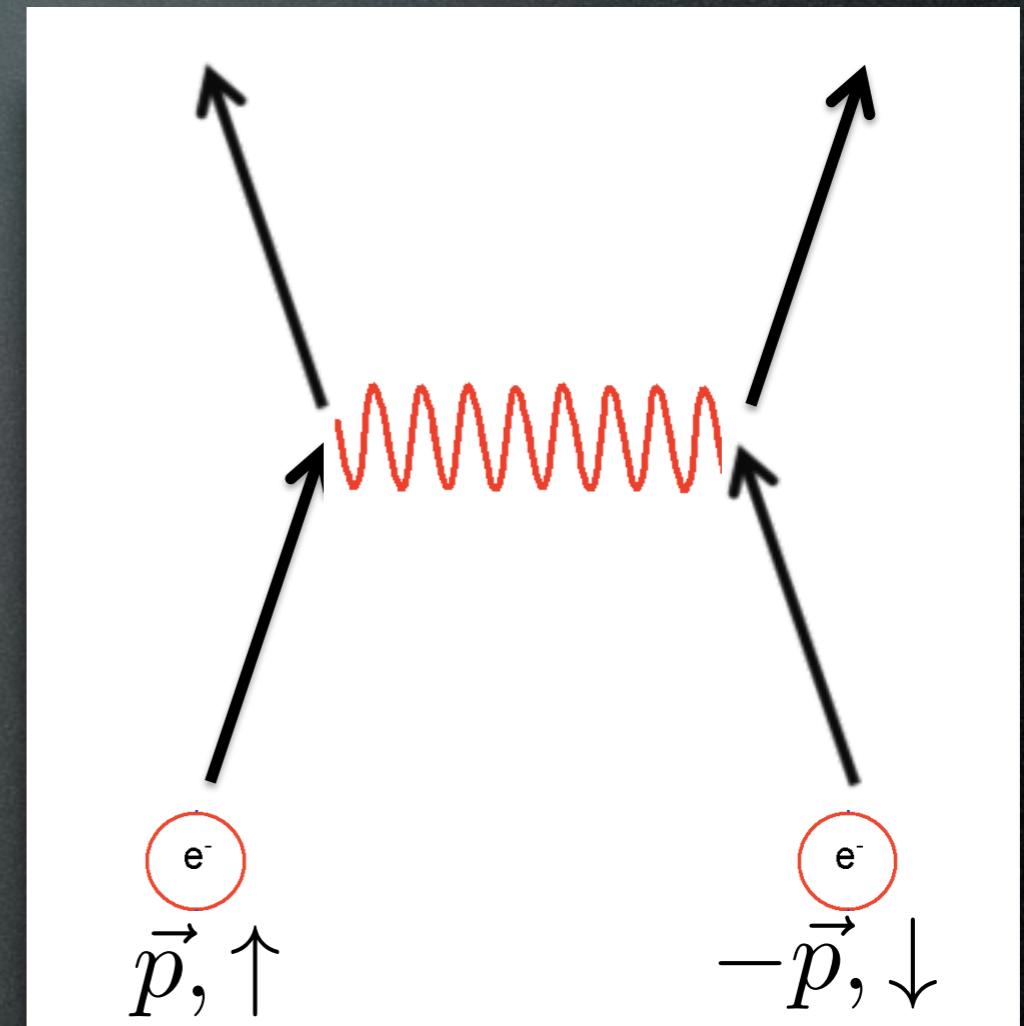


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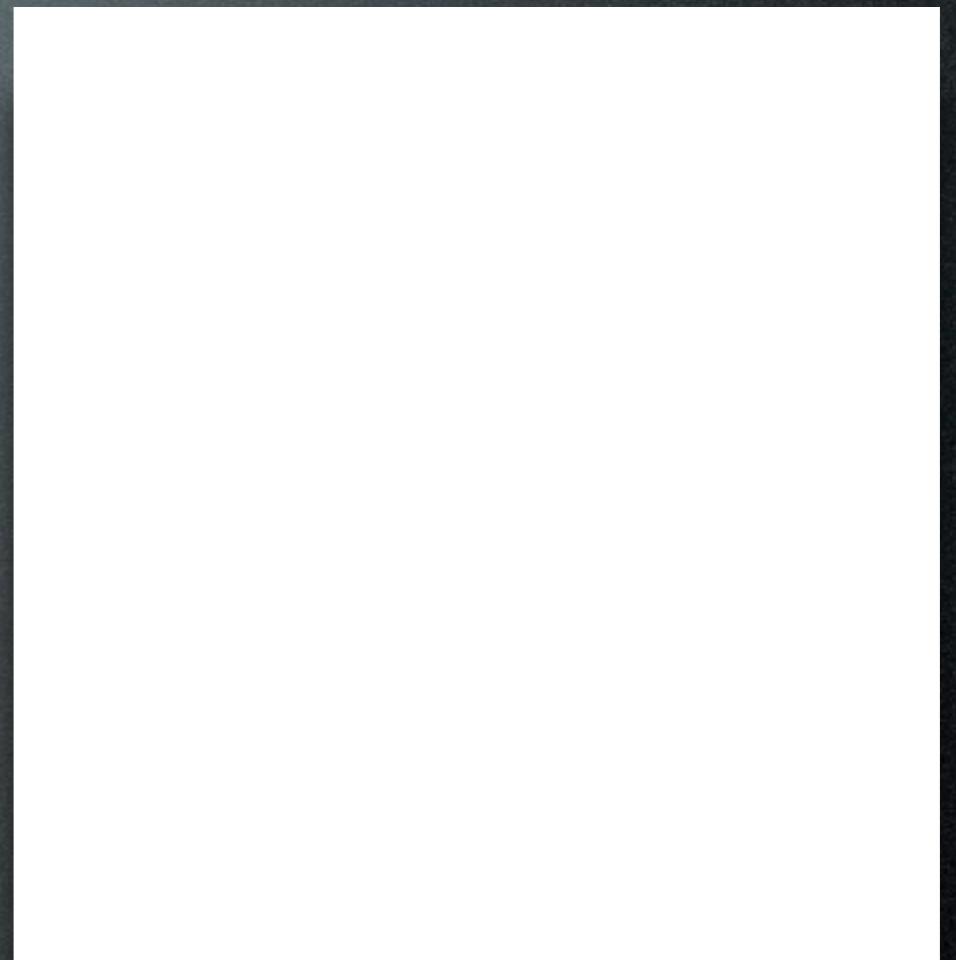
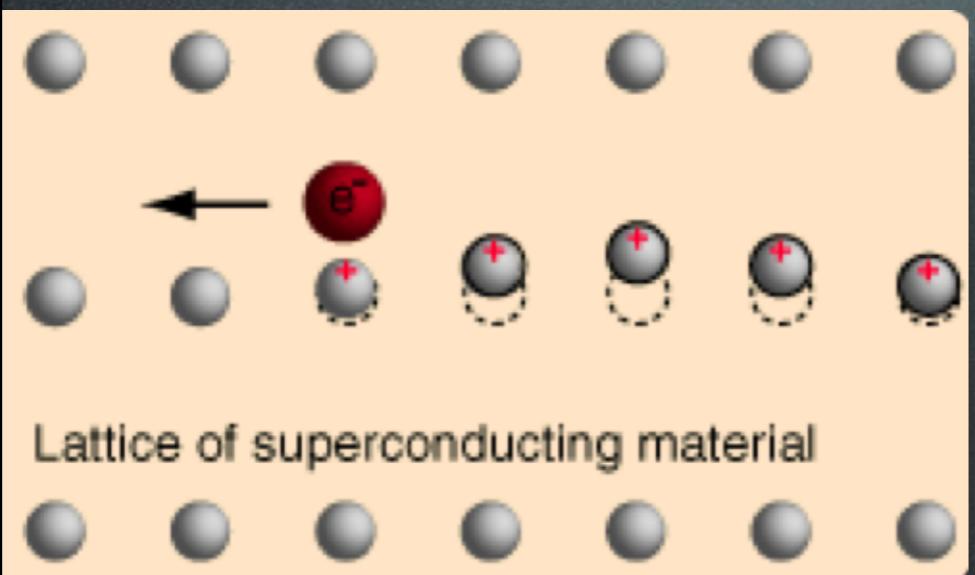
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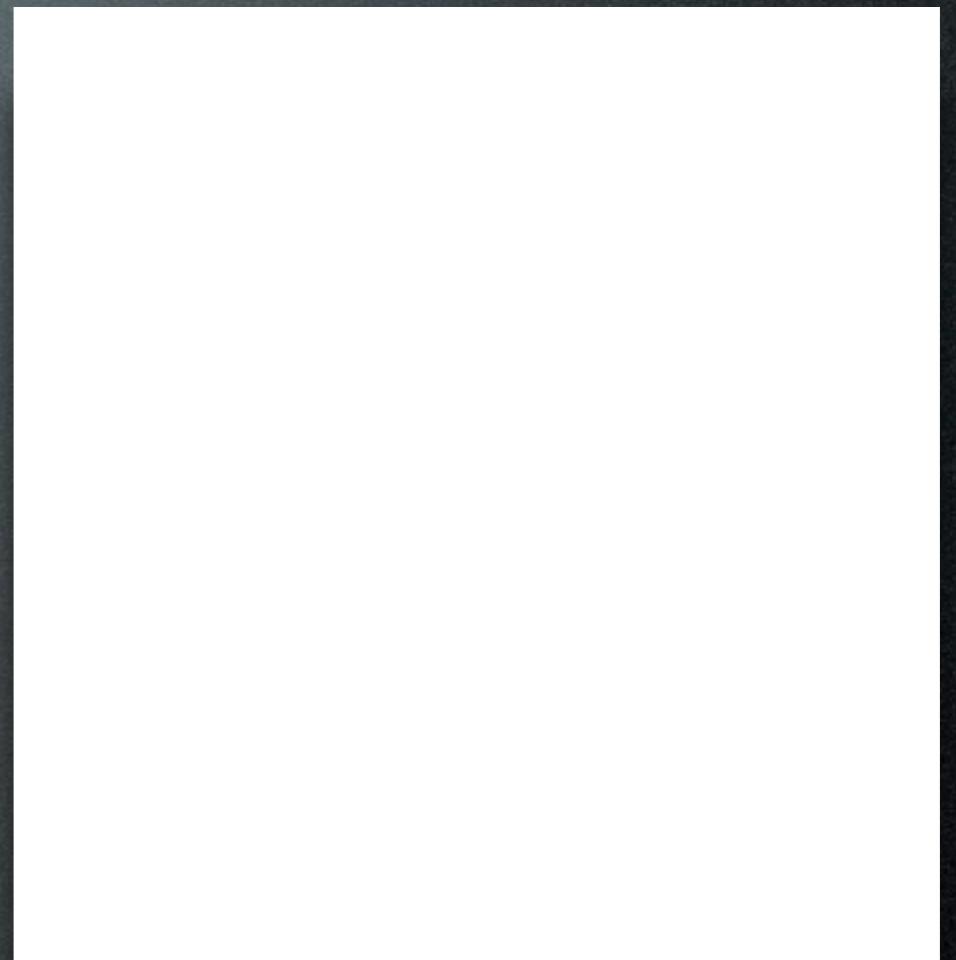
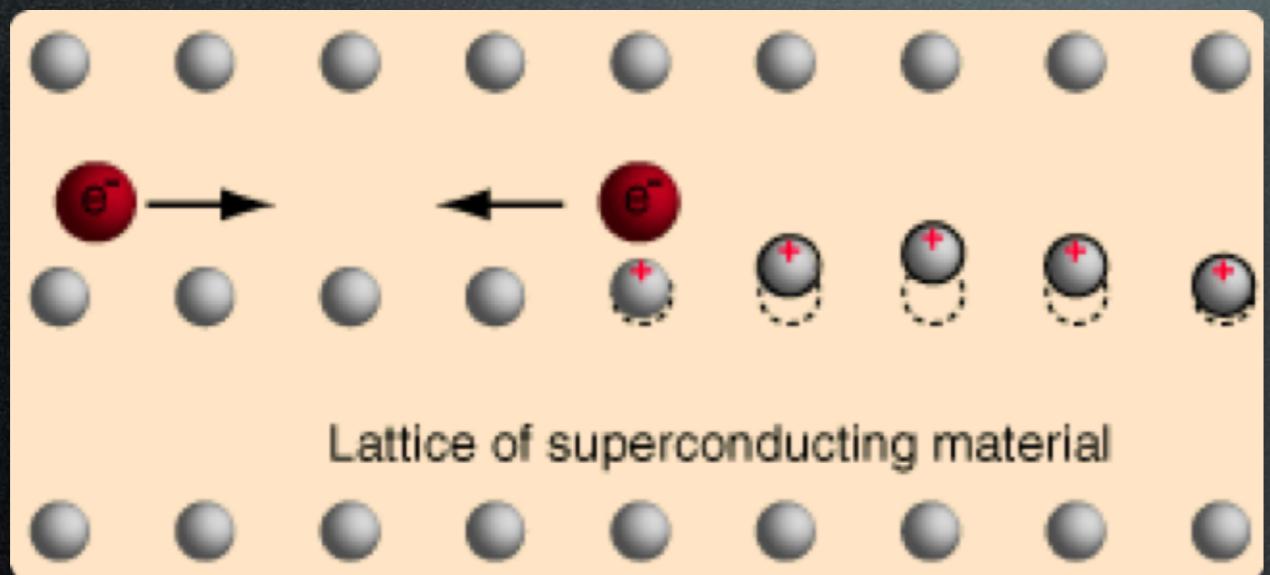
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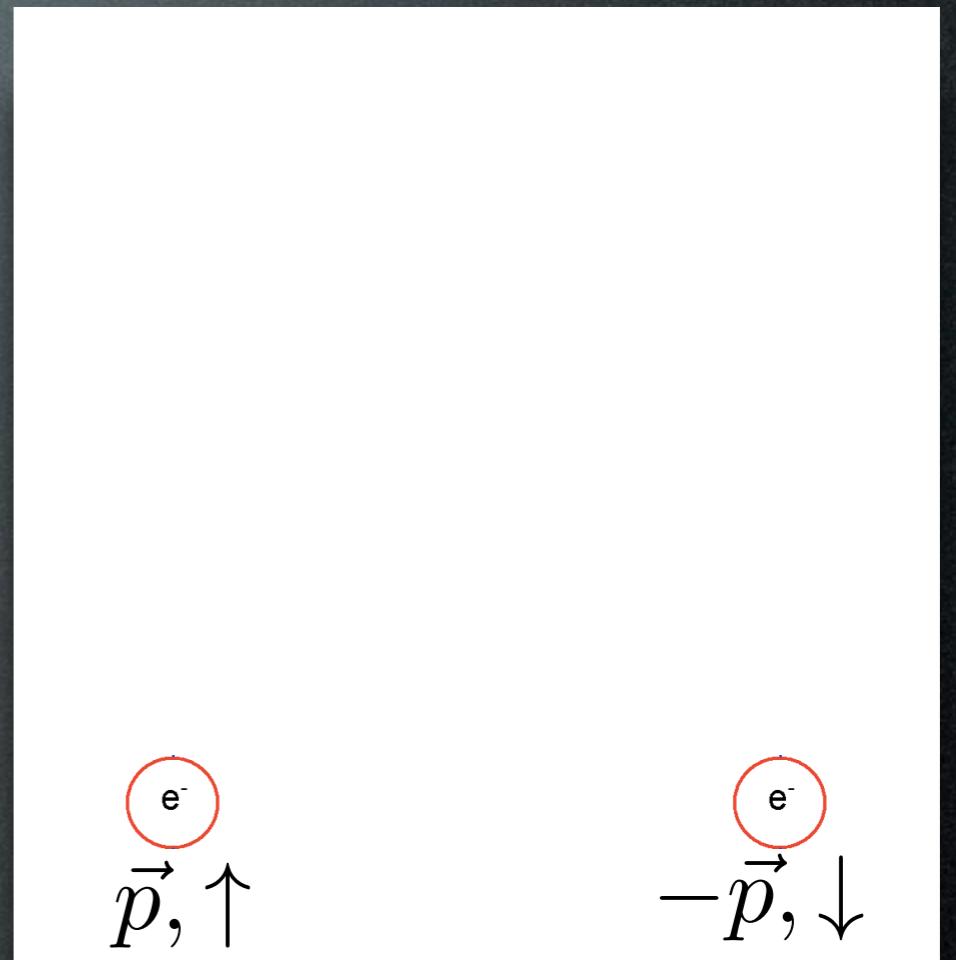
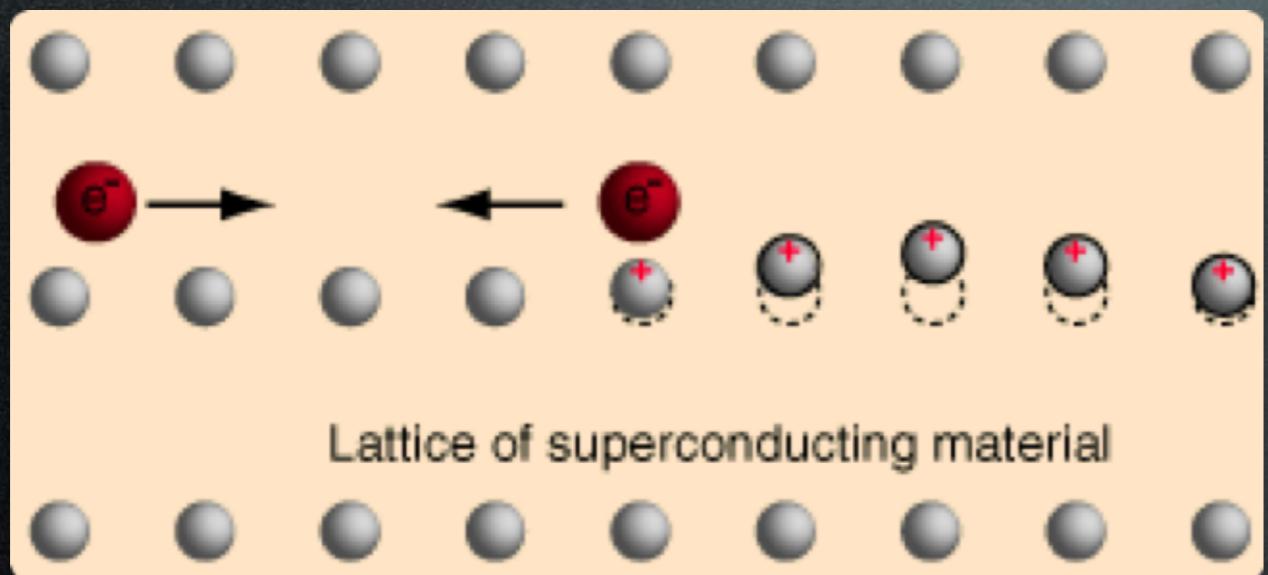
Electron-phonon coupling in BCS-SC?



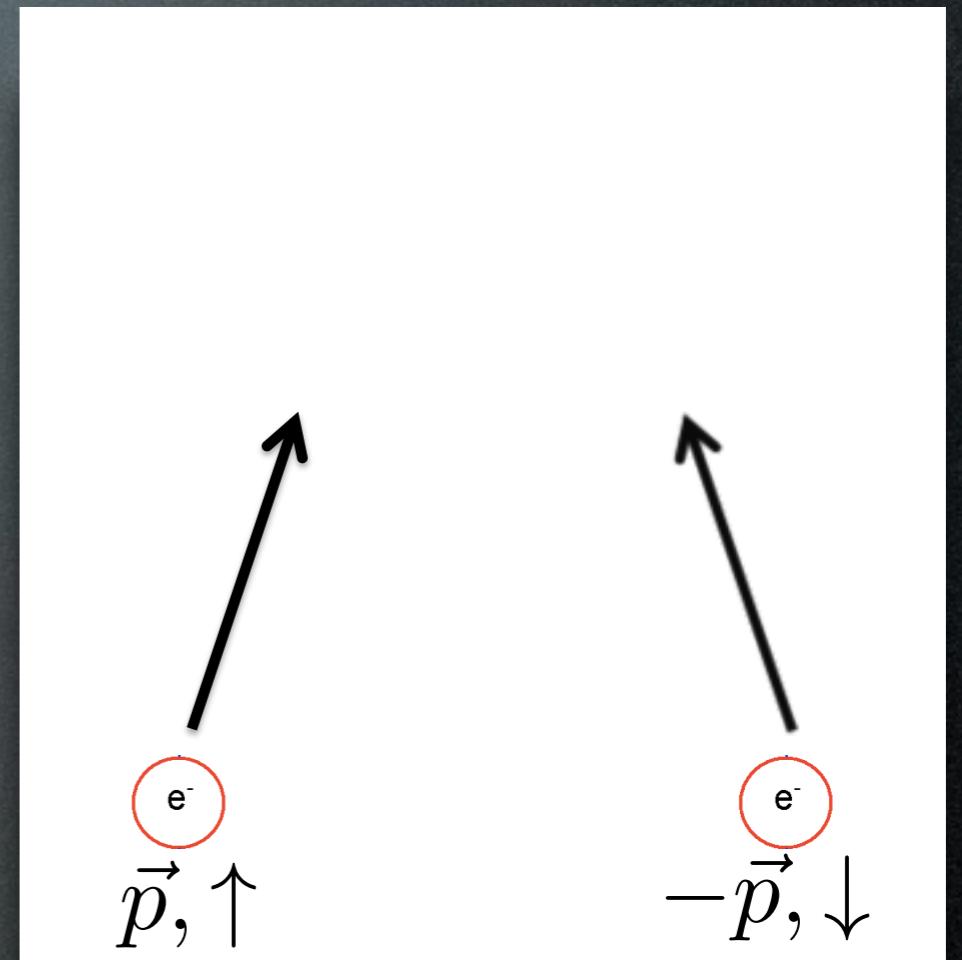
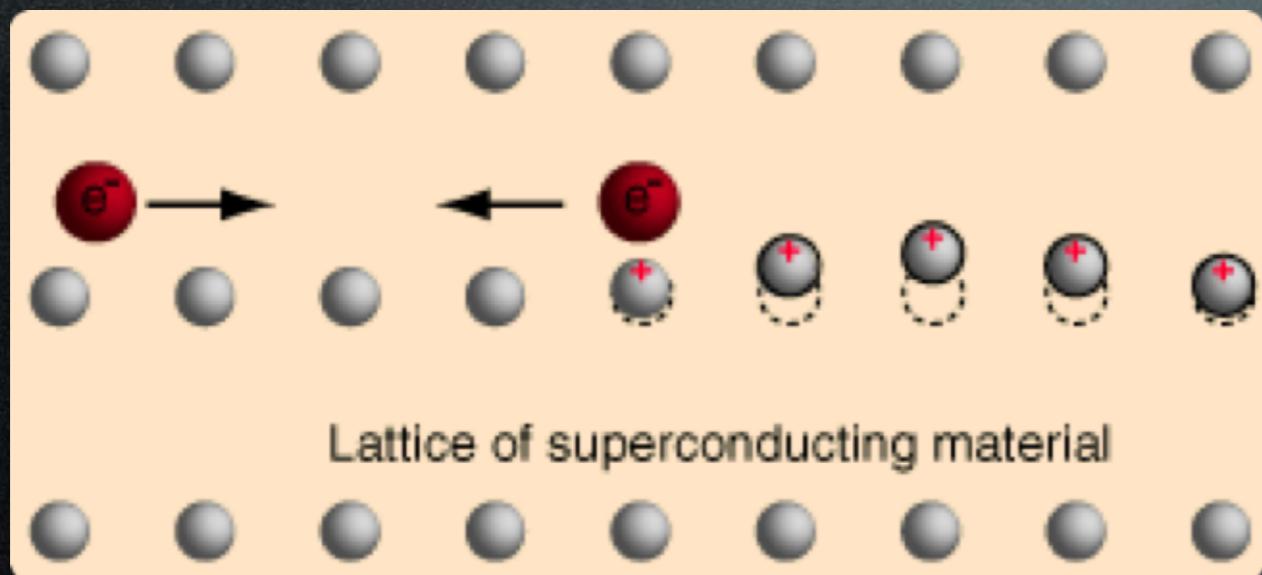
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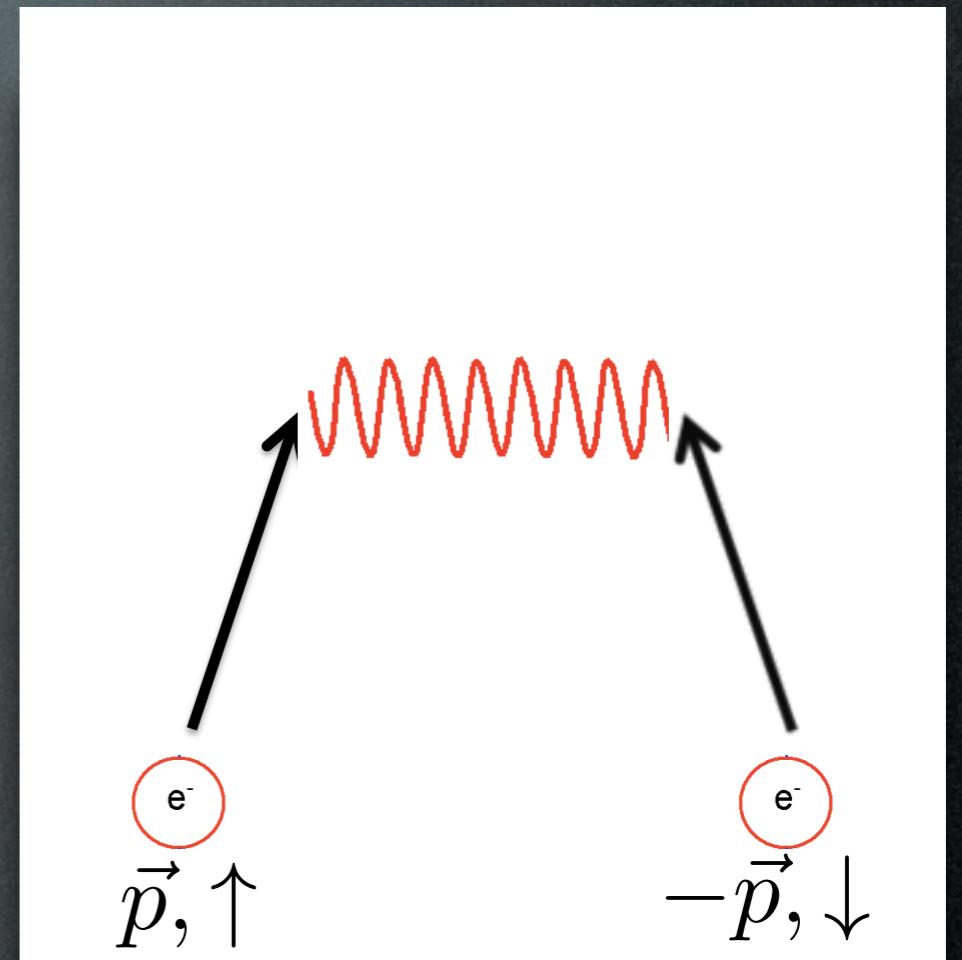
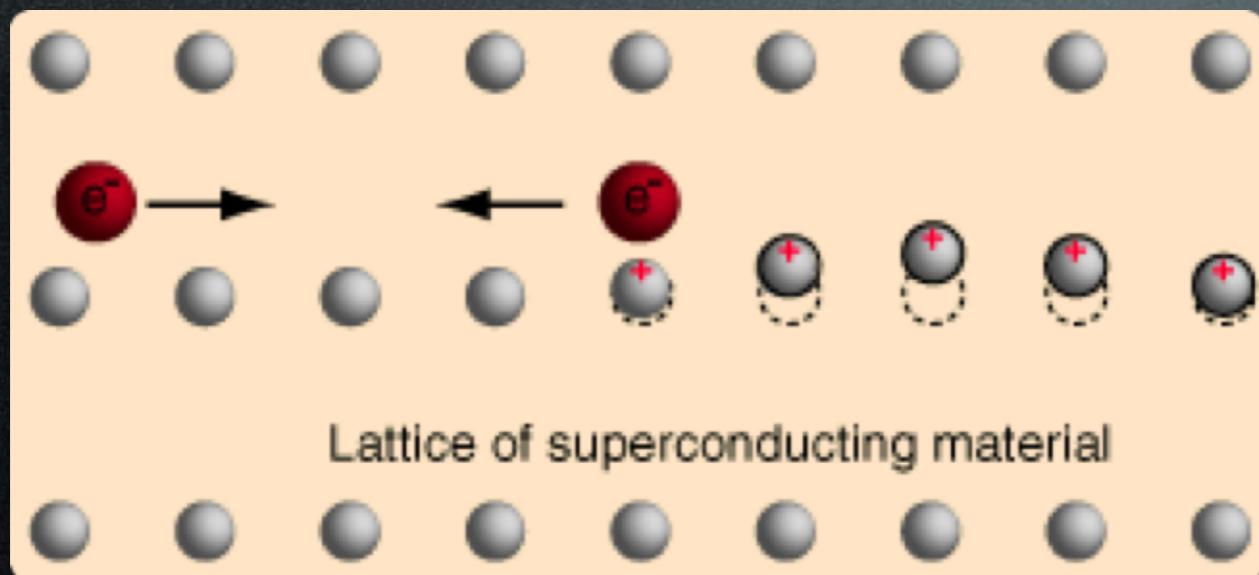
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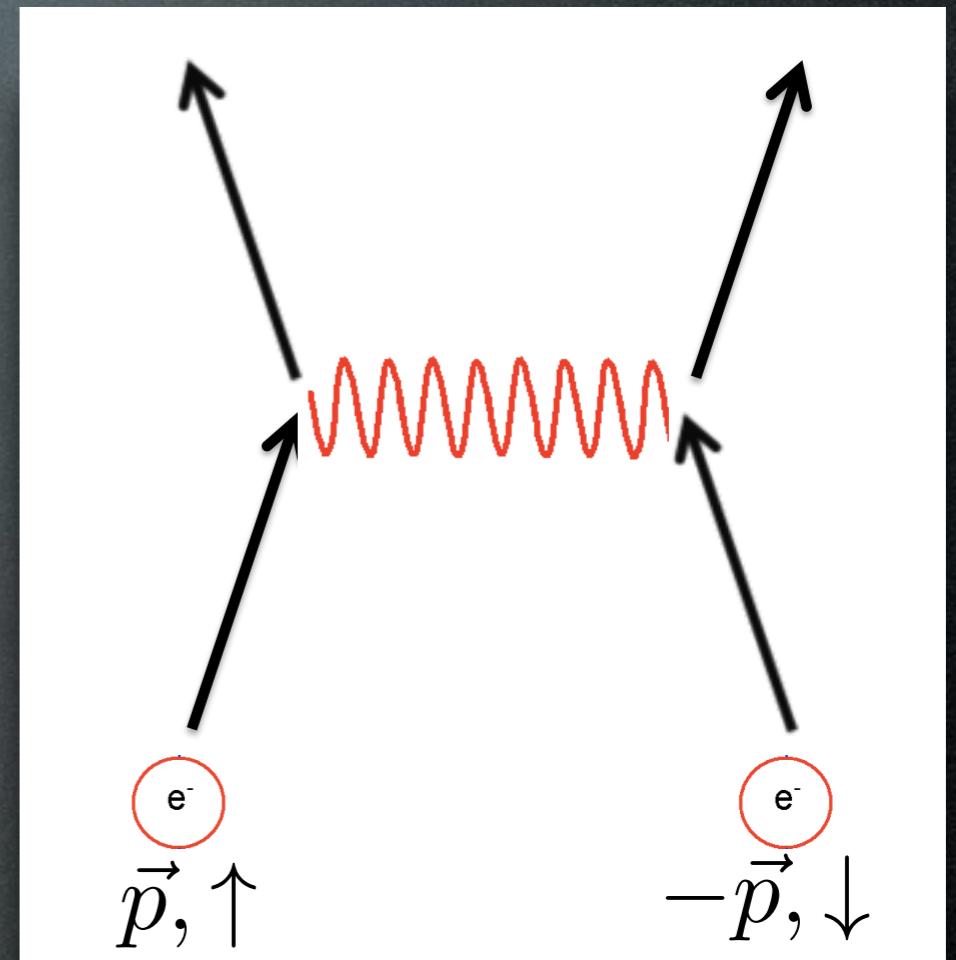
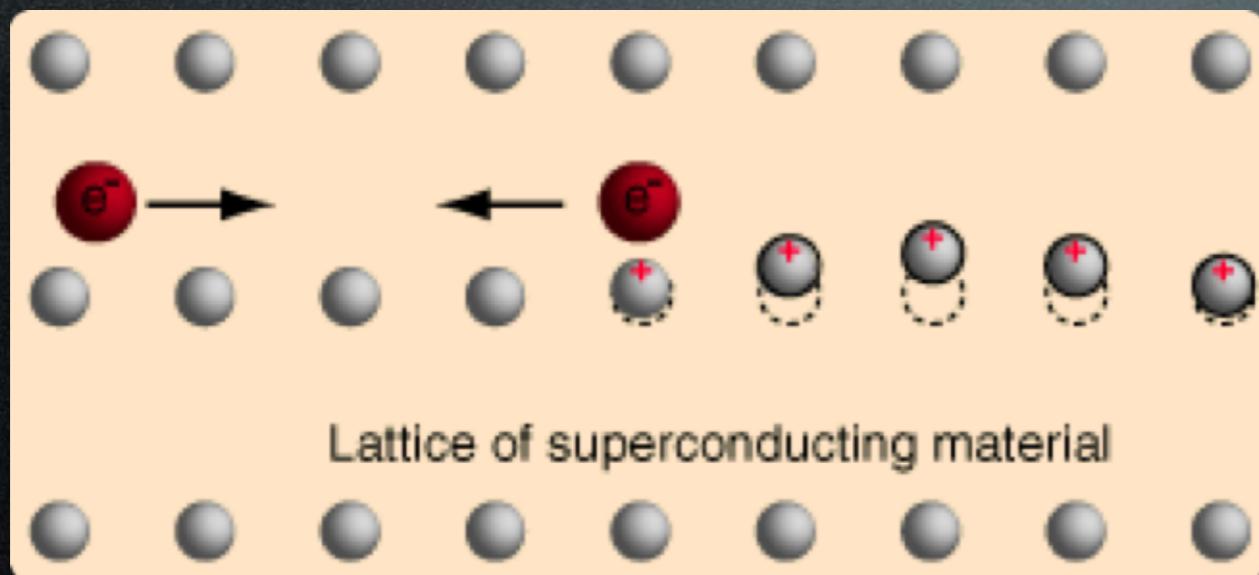
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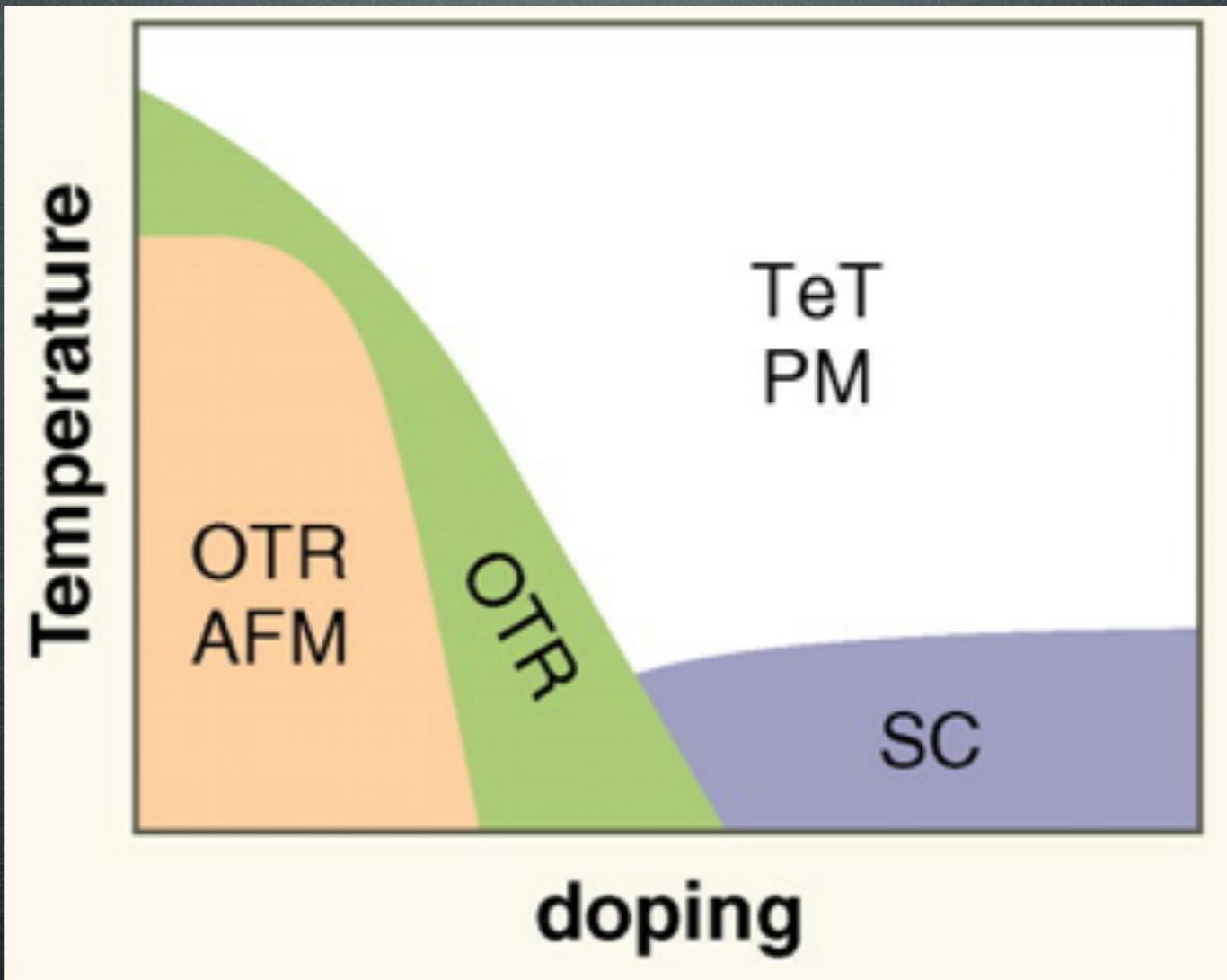
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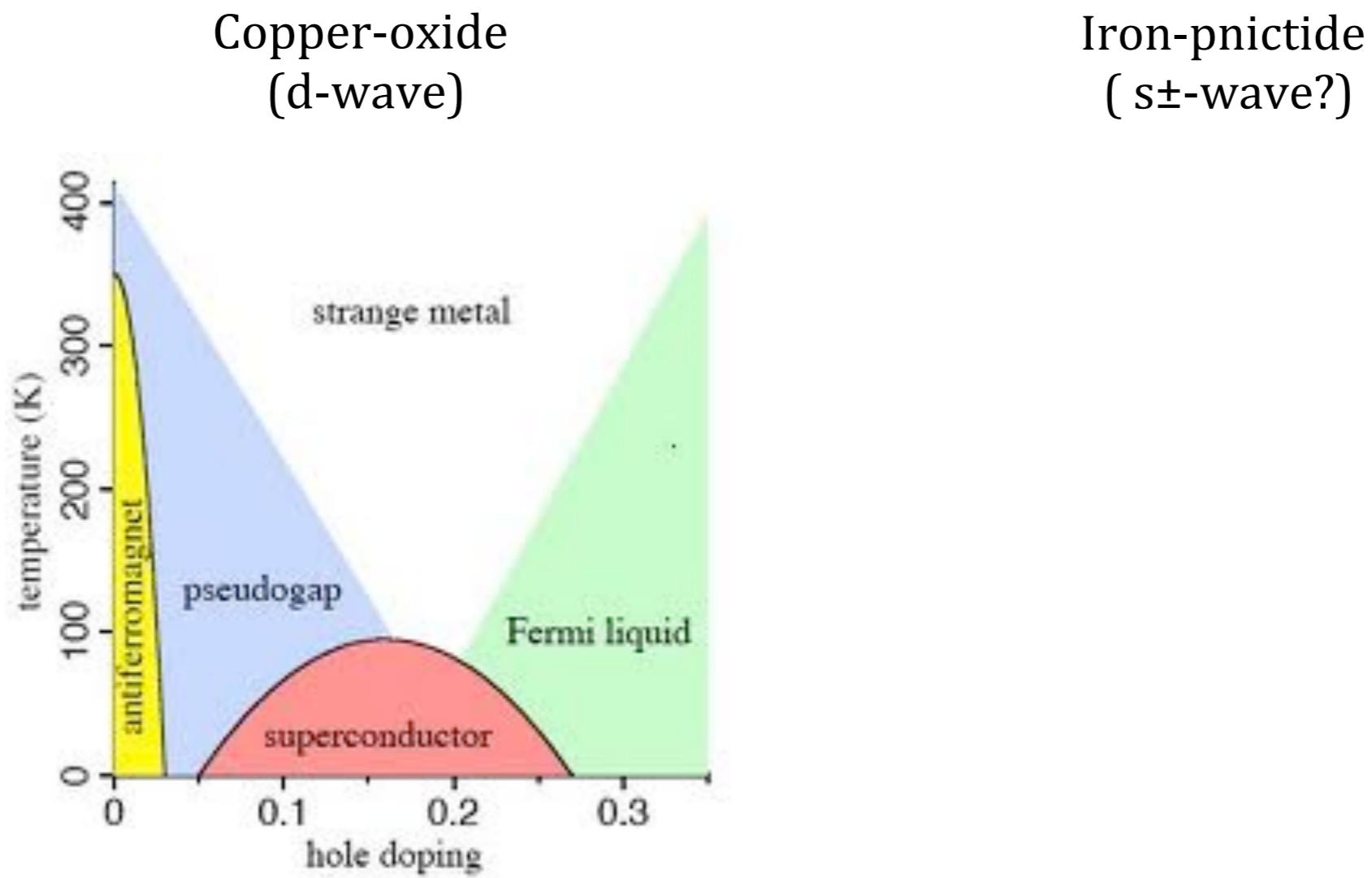
Pairing Mechanism of FeSC?



Wang & Lee, 2011

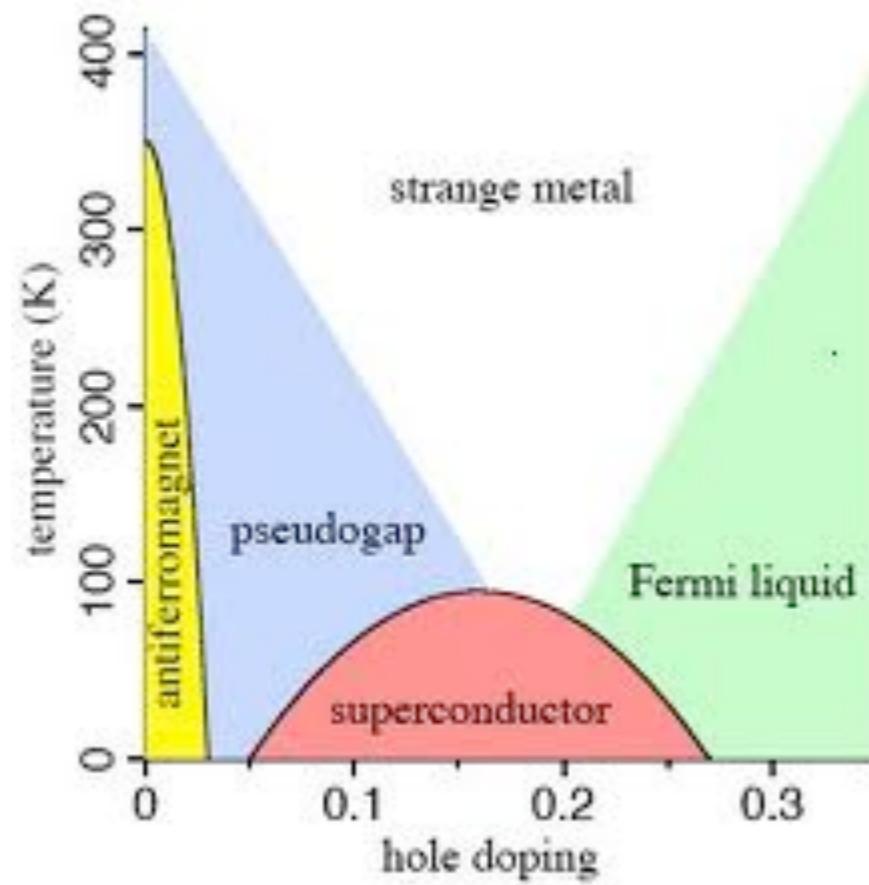
- Structural / magnetic transition near SC
⇒ Is it boson-mediated superconductivity?

Copper-oxide vs Iron-pnictide

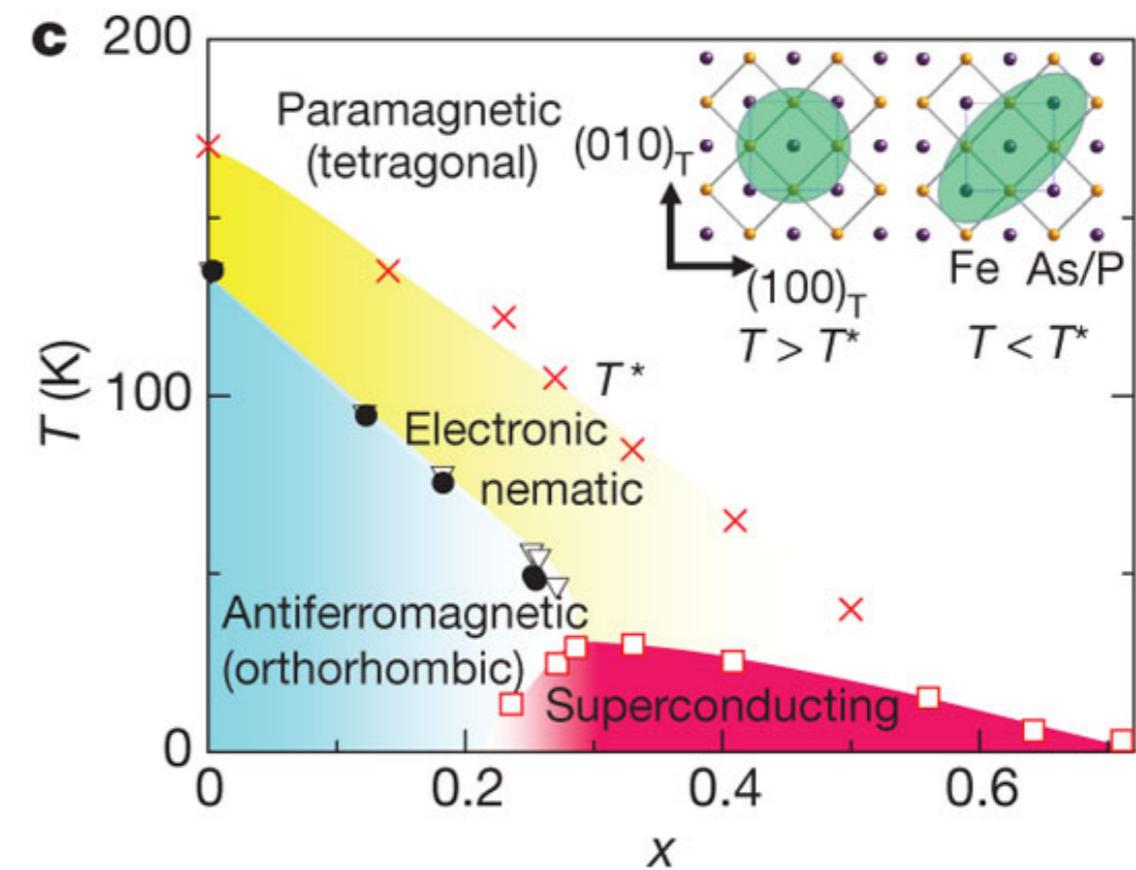


Copper-oxide vs Iron-pnictide

Copper-oxide
(d-wave)

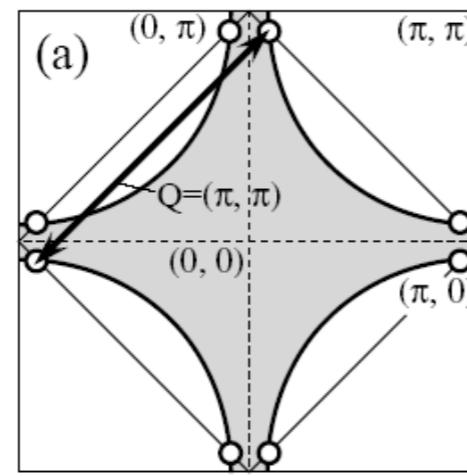
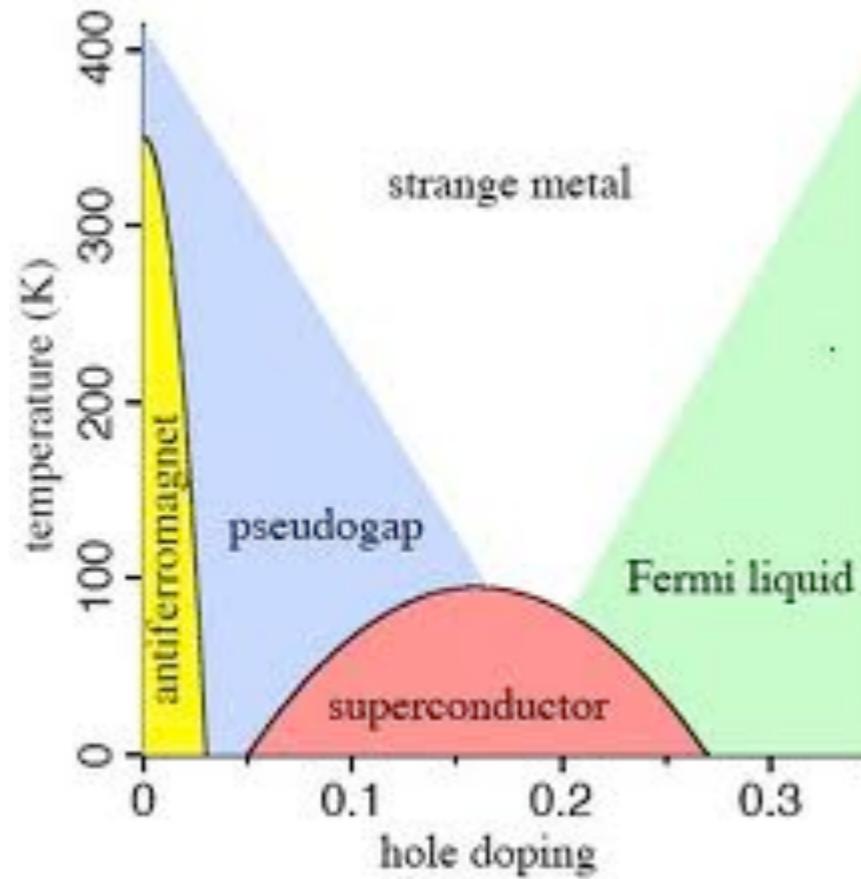


Iron-pnictide
(s±-wave?)

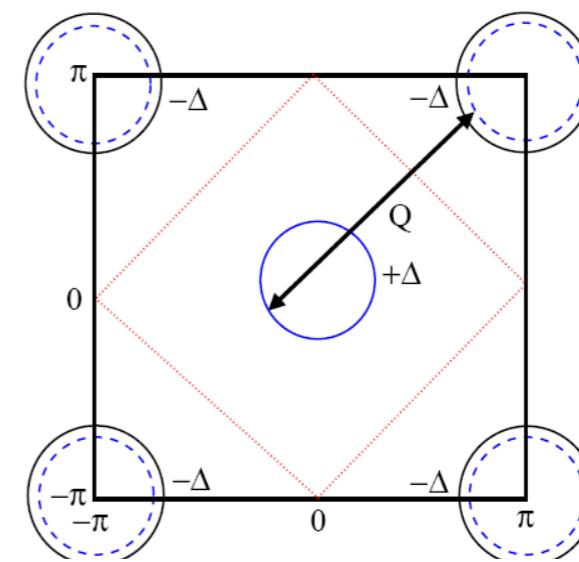
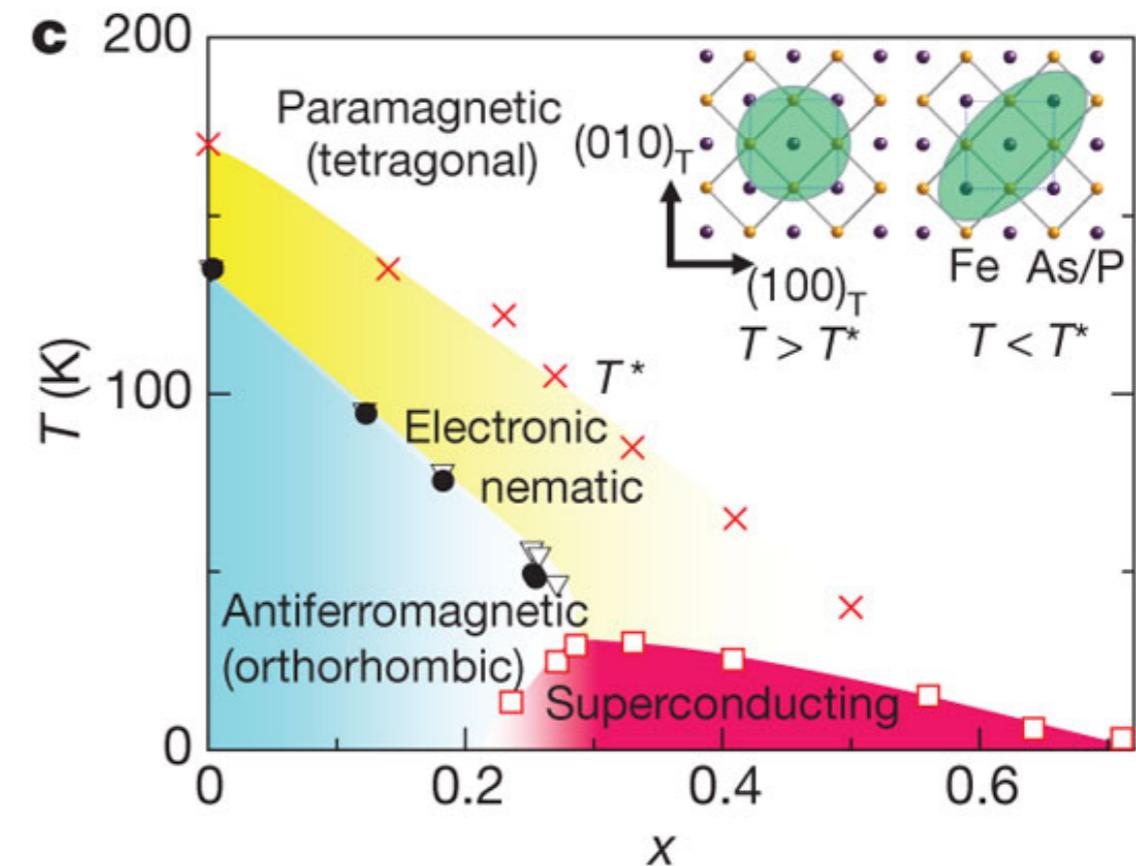


Copper-oxide vs Iron-pnictide

Copper-oxide
(d-wave)

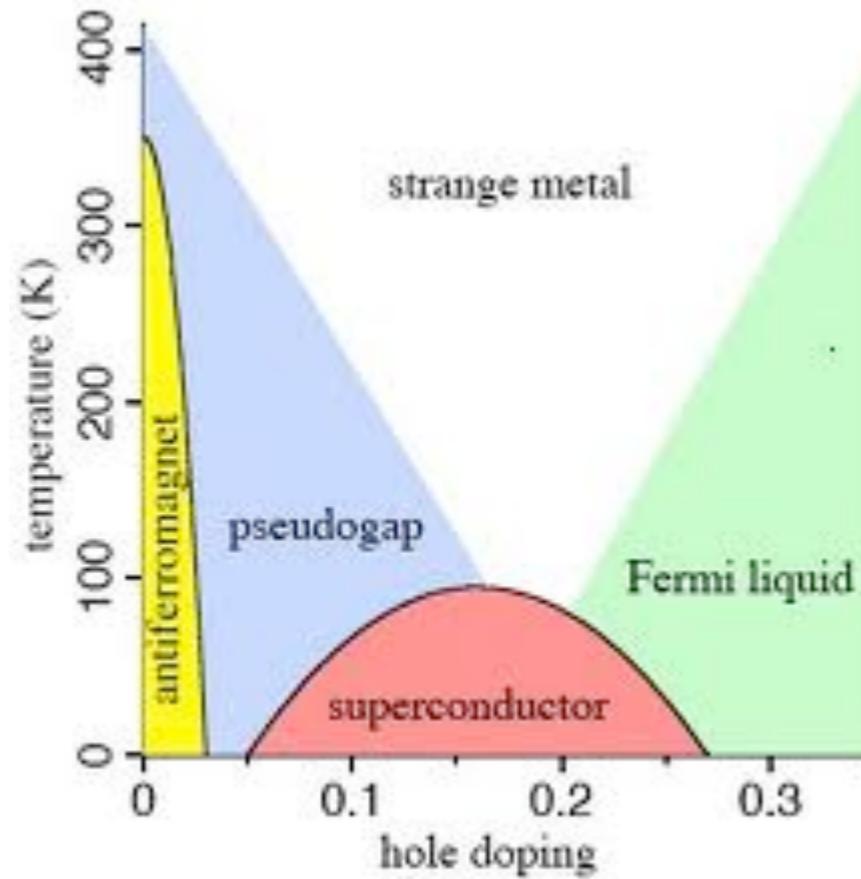


Iron-pnictide
(s±-wave?)

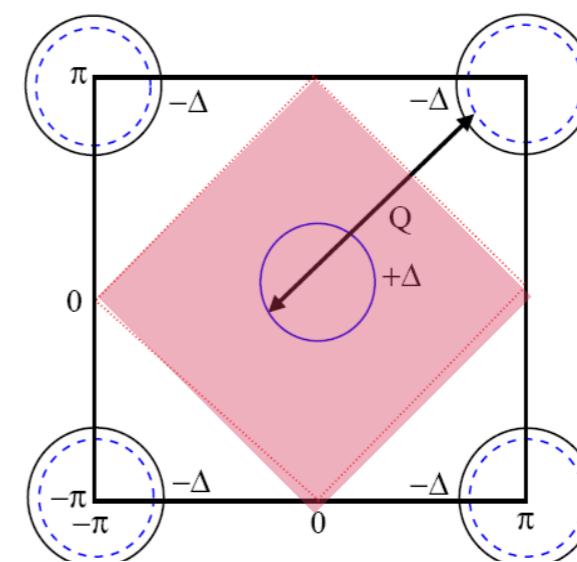
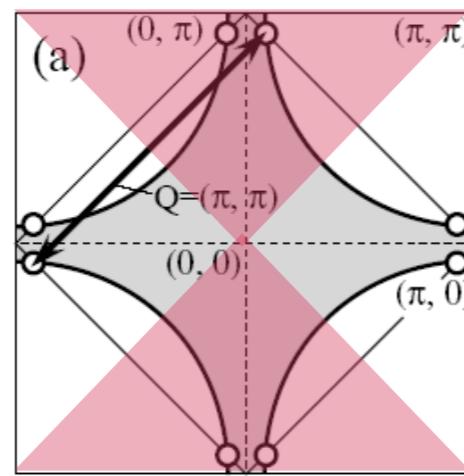
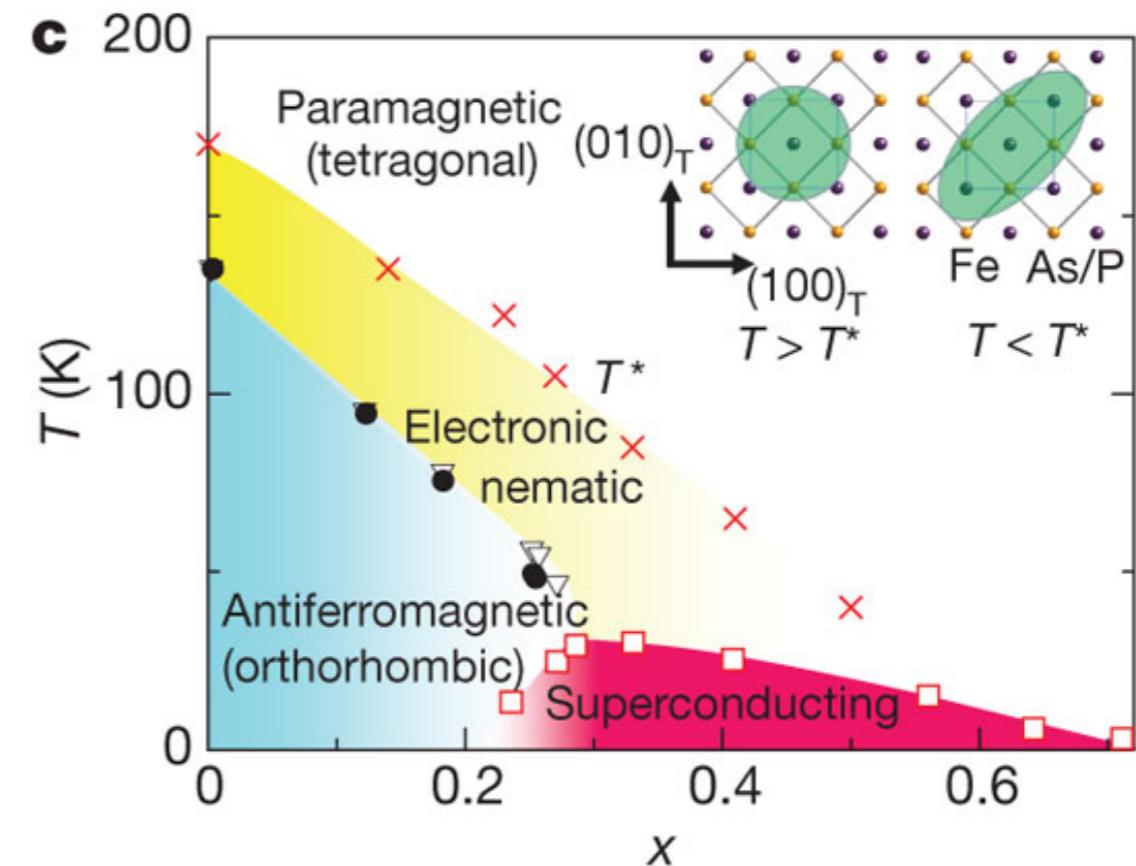


Copper-oxide vs Iron-pnictide

Copper-oxide
(d-wave)



Iron-pnictide
(s±-wave?)



Three step approach



Three step approach



1. Identify suspects

Three step approach



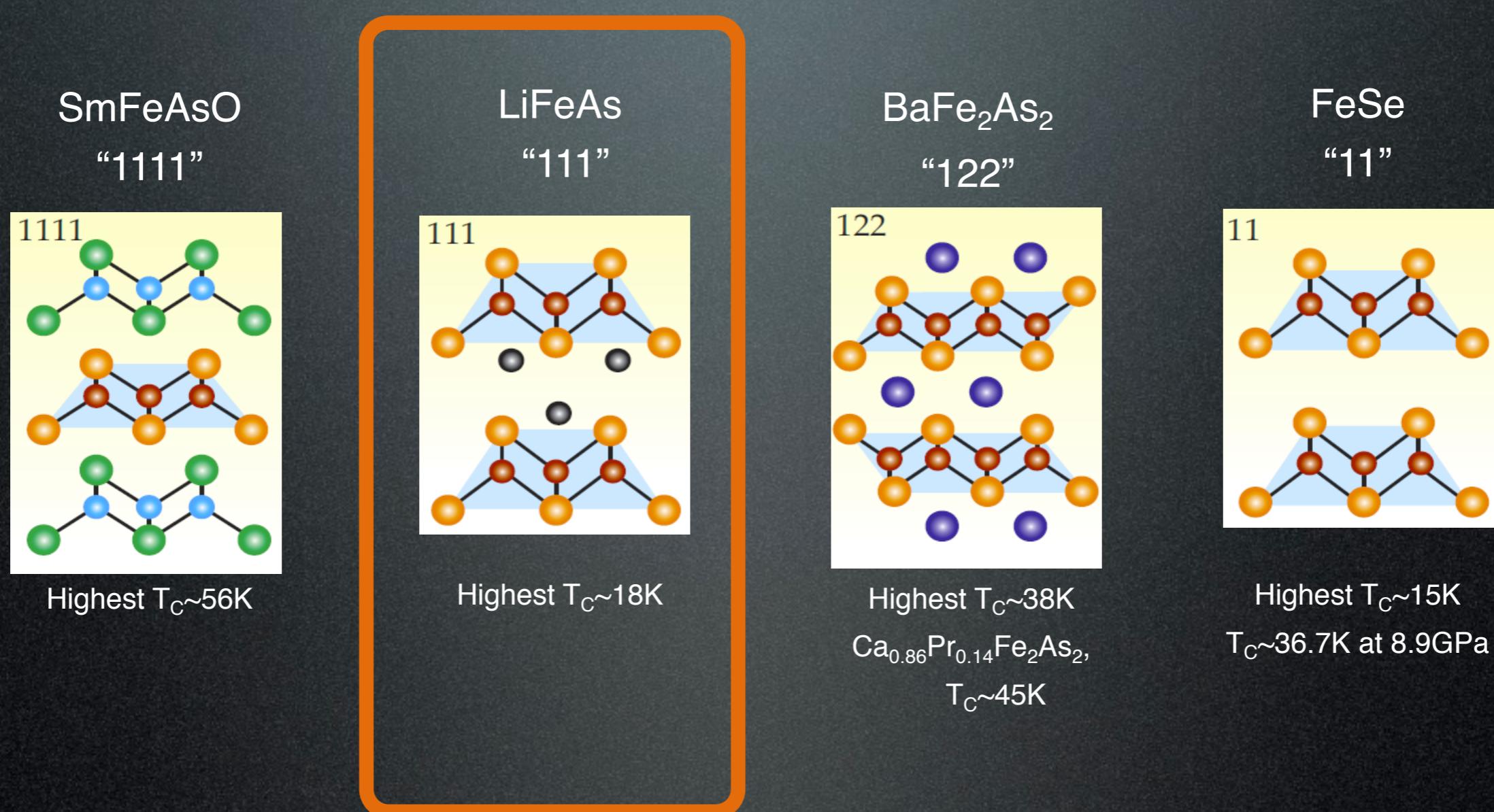
1. Identify suspects
2. Gather evidence

Three step approach



1. Identify suspects
2. Gather evidence
3. Match evidence to a suspect

LiFeAs



Why LiFeAs?

Why LiFeAs?

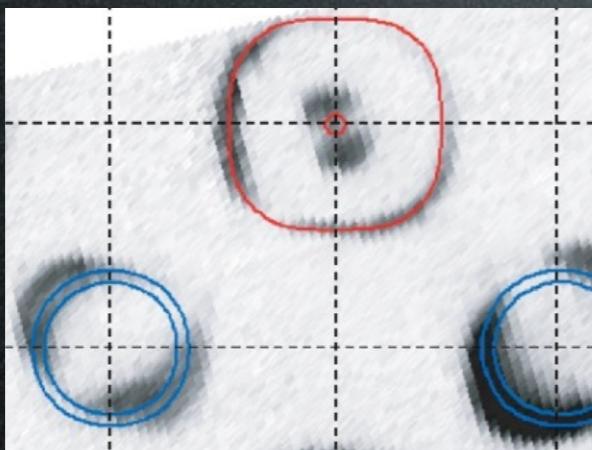
- Neutral cleave plane

Why LiFeAs?

- Neutral cleave plane
- Detailed knowledge of electronic structure

Why LiFeAs?

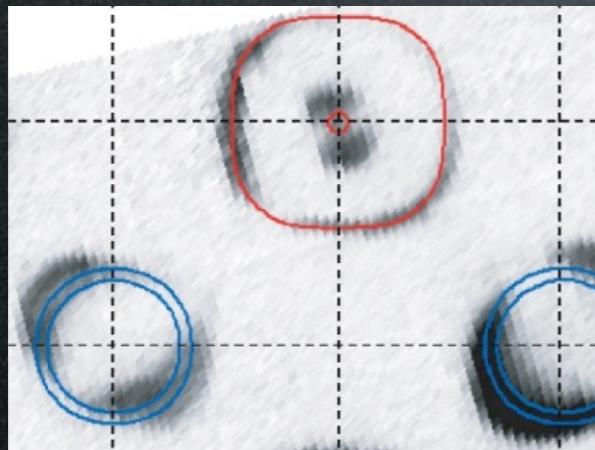
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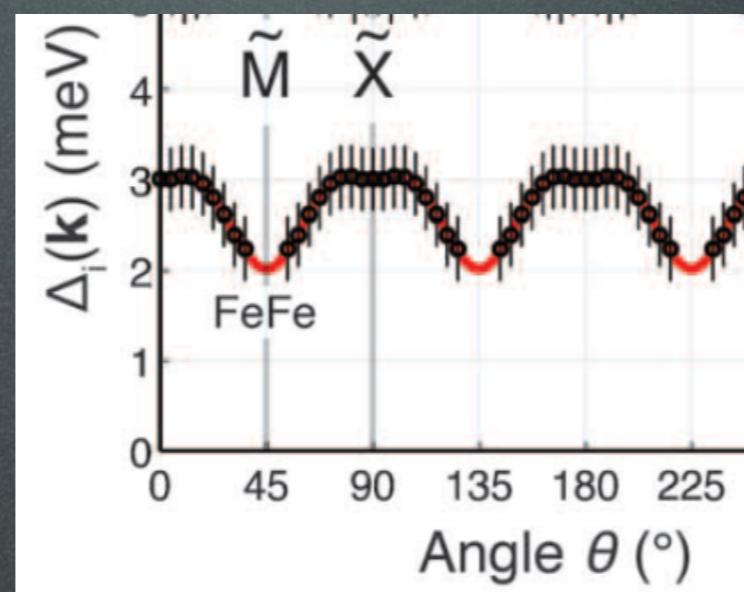
ARPES
Knolle *et al.* 2012

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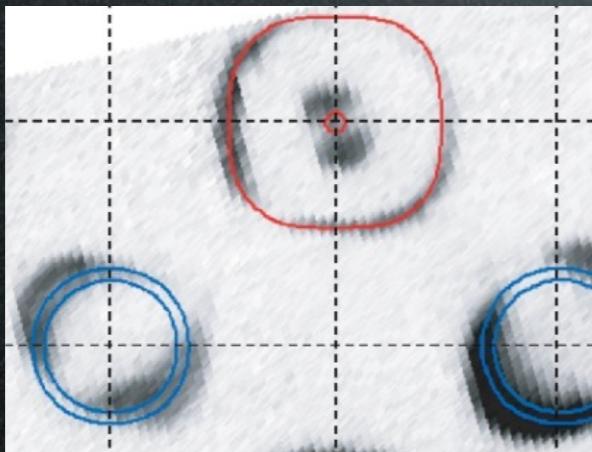
ARPES
Knolle *et al.* 2012



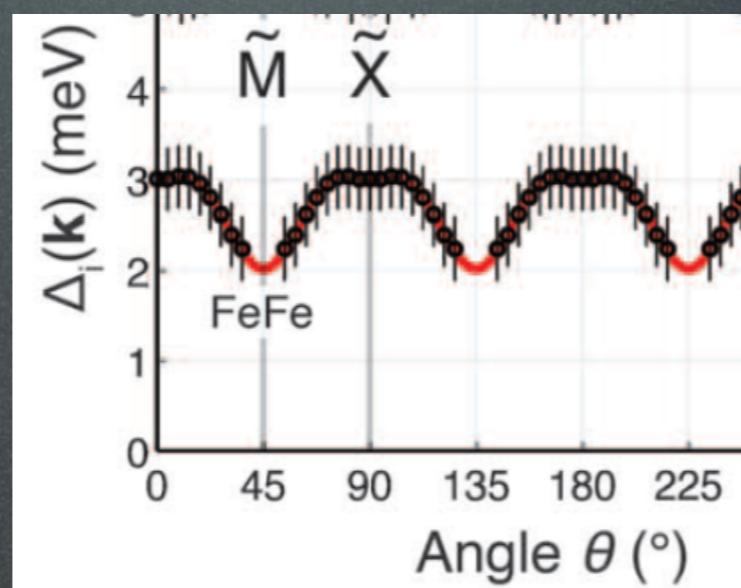
STM
Allan & Rost *et al.* 2012

Why LiFeAs?

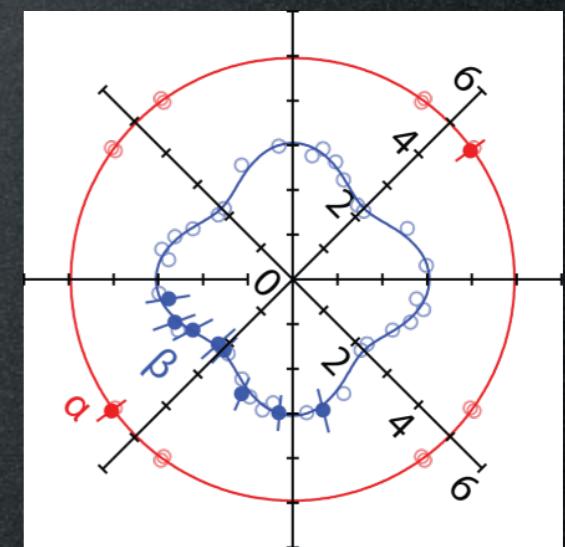
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ARPES
Knolle *et al.* 2012



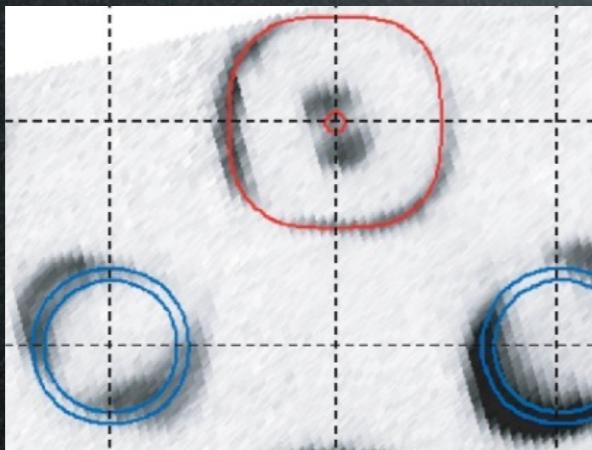
STM
Allan & Rost *et al.* 2012



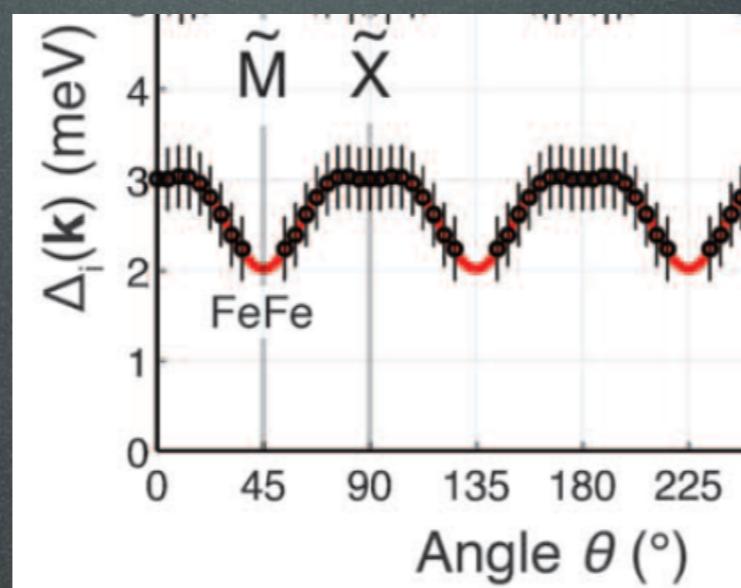
ARPES
Umezawa *et al.* 2012

Why LiFeAs?

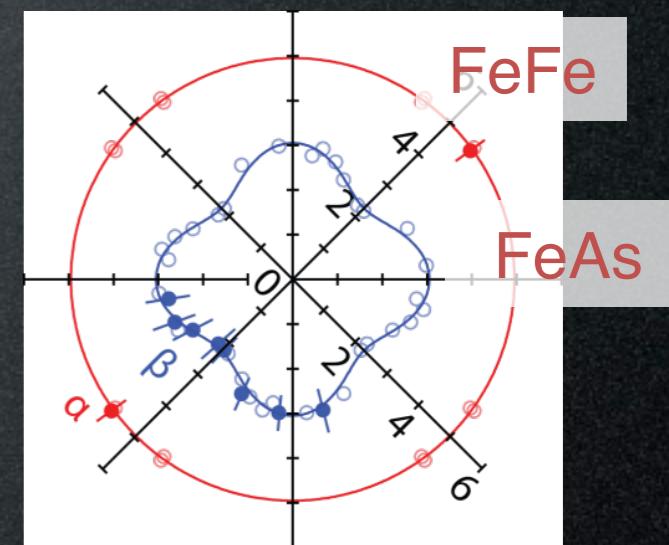
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ARPES
Knolle *et al.* 2012



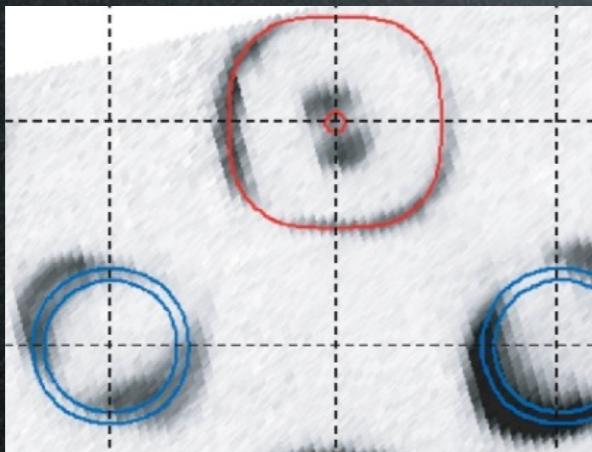
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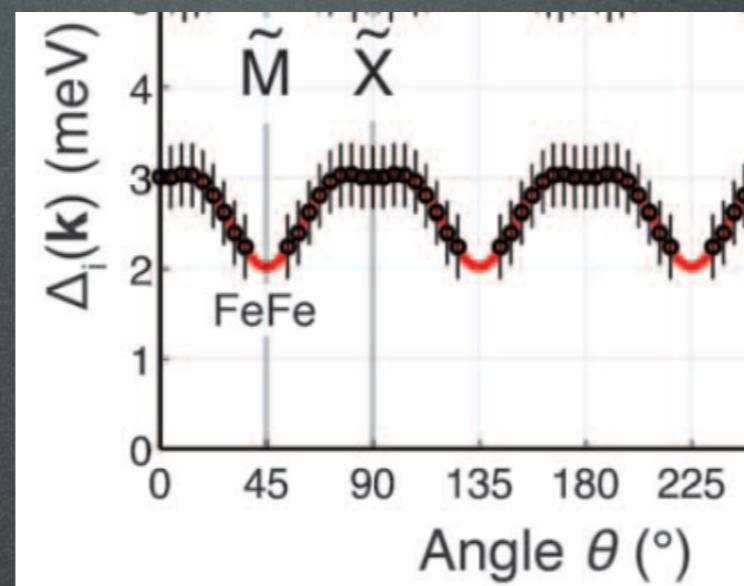
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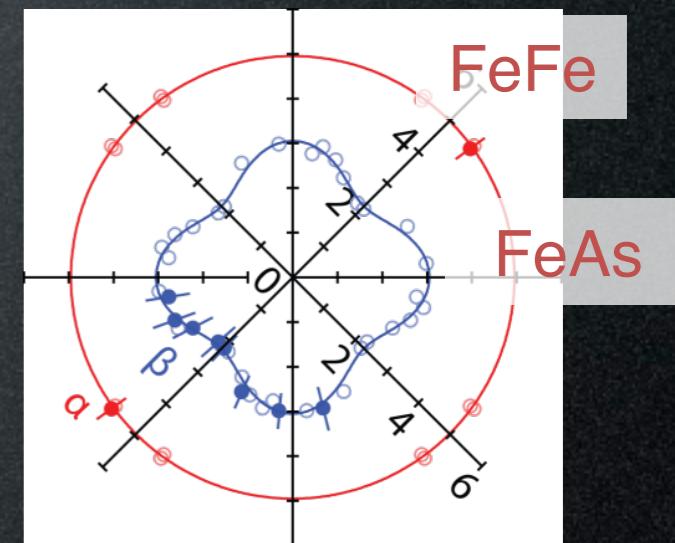
- Neutral cleave plane
- Detailed knowledge of electronic structure



ARPES
Knolle *et al.* 2012



STM
Allan & Rost *et al.* 2012



ARPES
Umezawa *et al.* 2012

- Large hole pocket (γ) with a single orbital character d_{xy}

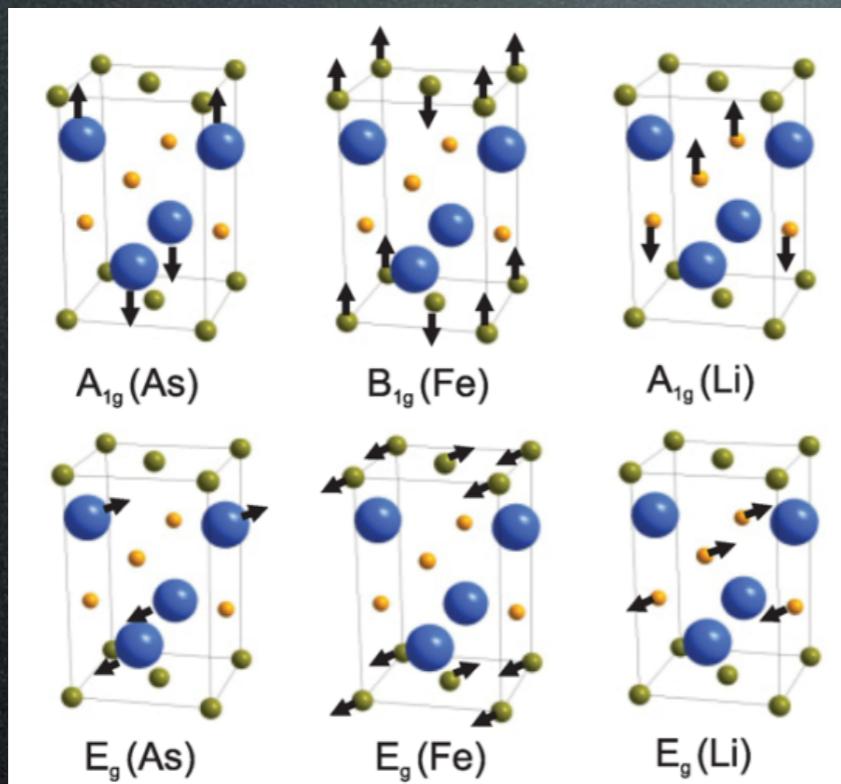
1. Identify suspects

Bosons suspects in LiFeAs

- Fe E_g optical phonon
 - argued to induce orbital fluctuation
 - $\Omega=15\text{meV}$ (Raman, DFT)

Bosons suspects in LiFeAs

Phonons



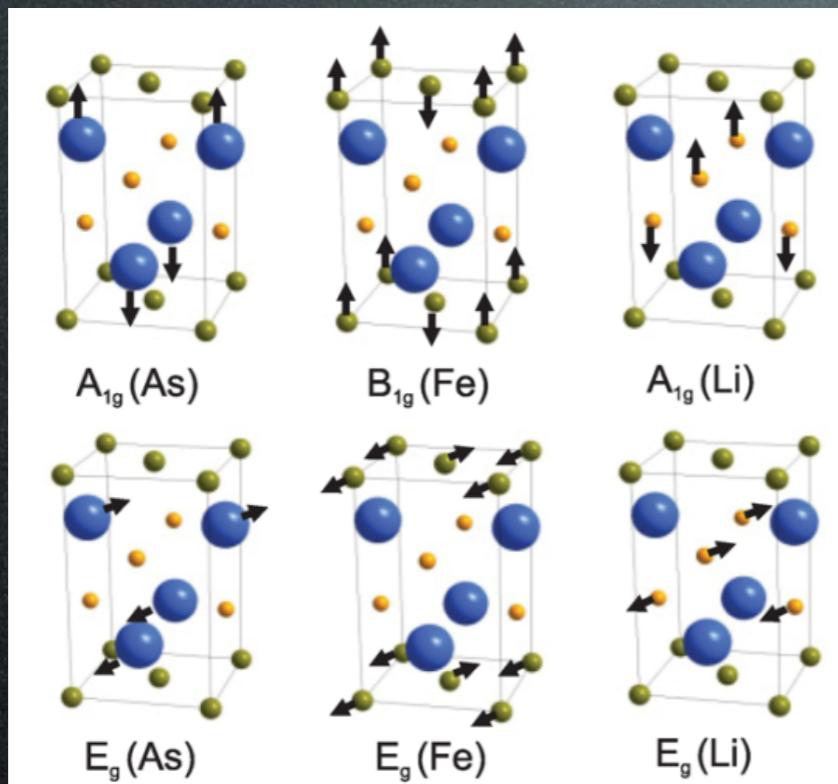
Raman
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Bosons suspects in LiFeAs

Phonons

Spin Fluctuation



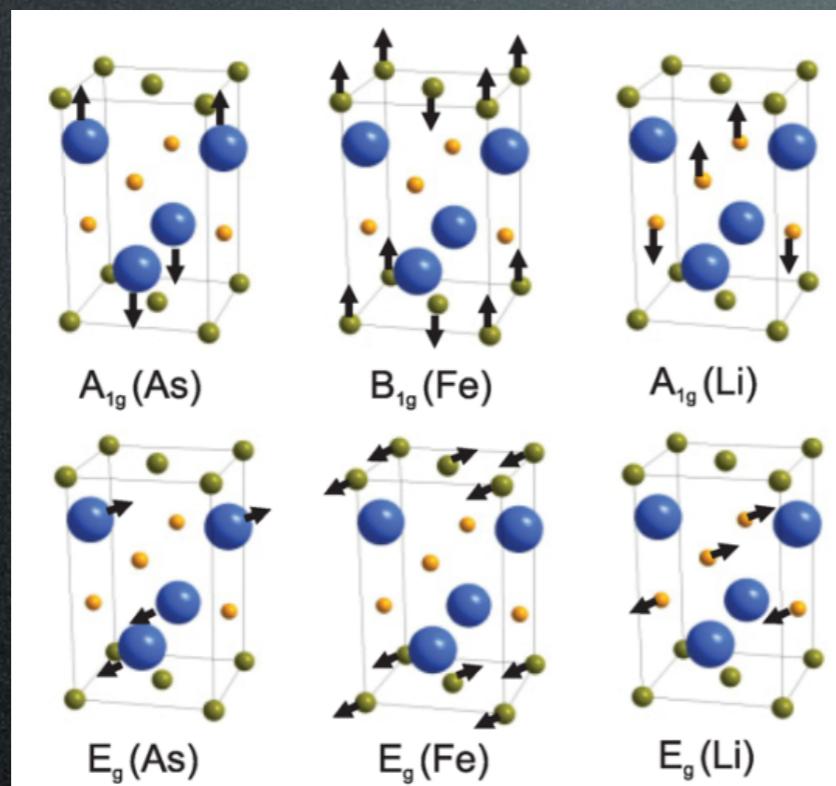
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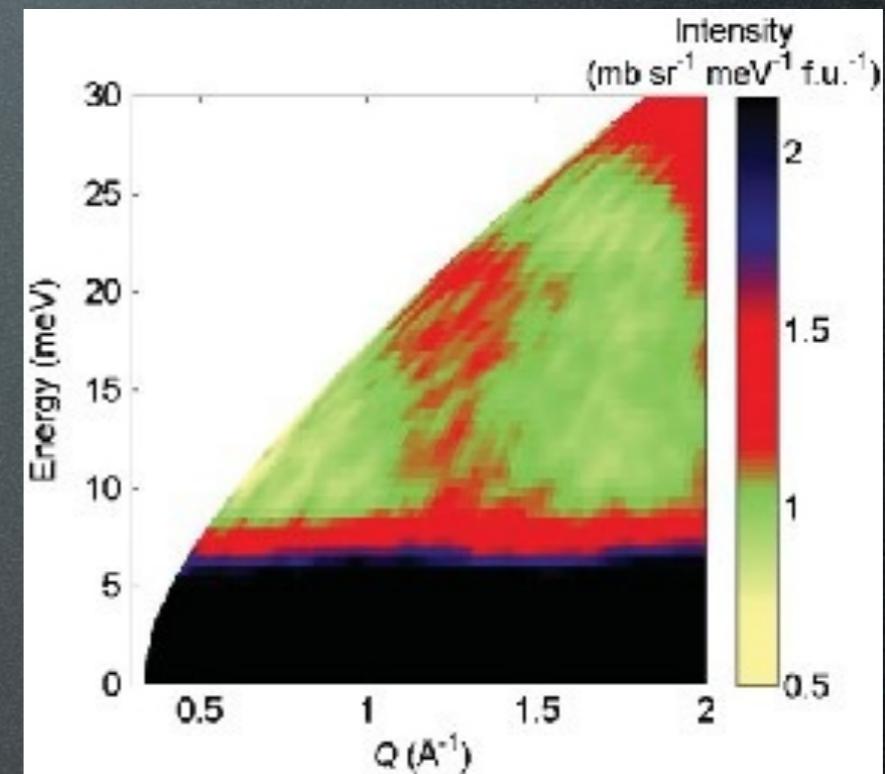
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Phonons



Raman
Um *et al.* 2012

Spin Fluctuation

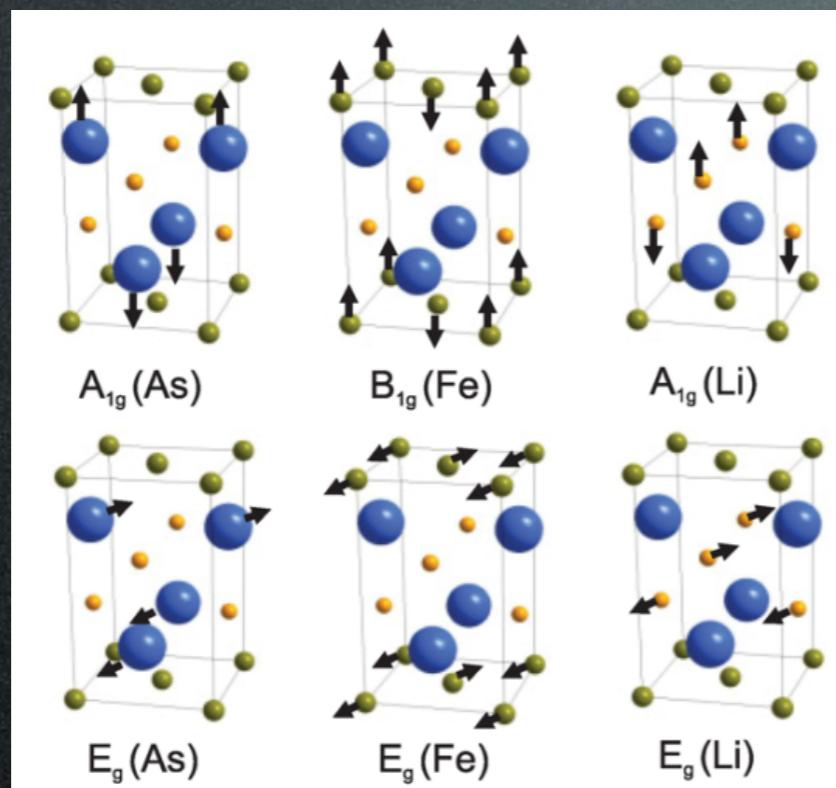


Inelastic Neutron
Taylor *et al.* 2011

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Bosons suspects in LiFeAs

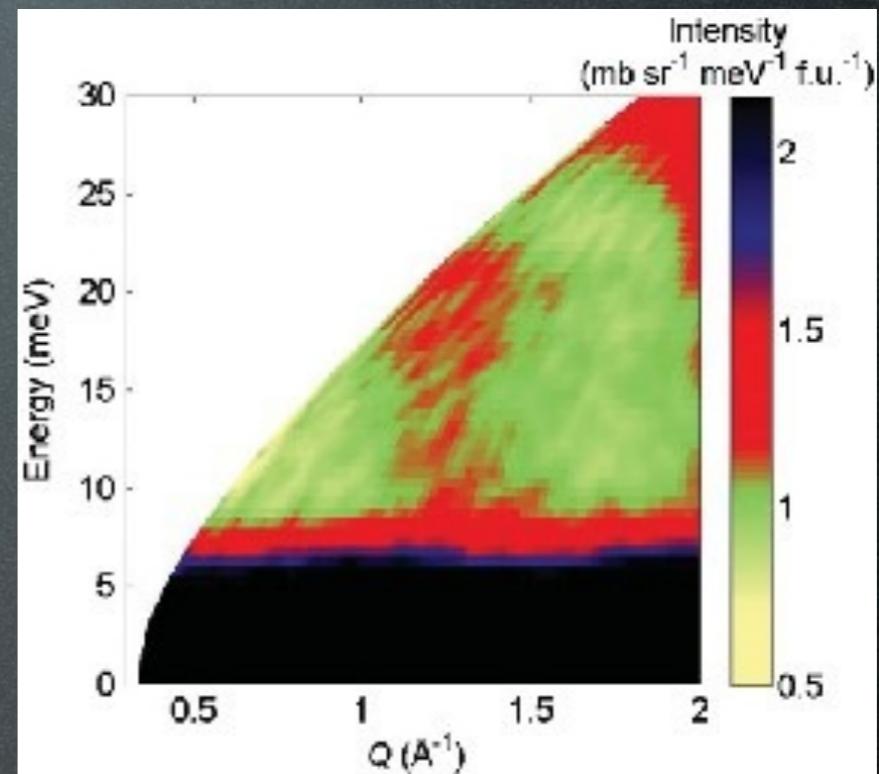
Phonons



Raman
Um *et al.* 2012

- Fe E_g optical phonon
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 - $\Omega=15\text{meV}$ (Raman, DFT)

Spin Fluctuation



Inelastic Neutron
Taylor *et al.* 2011

- Resonant mode centered at $Q=(\pi, \pi)$ (AFSF)
 - $\Omega=6\text{meV}$

2. Gather evidence

Scanning Tunneling Spectroscopy
Quasiparticle Interference

2. Gather evidence

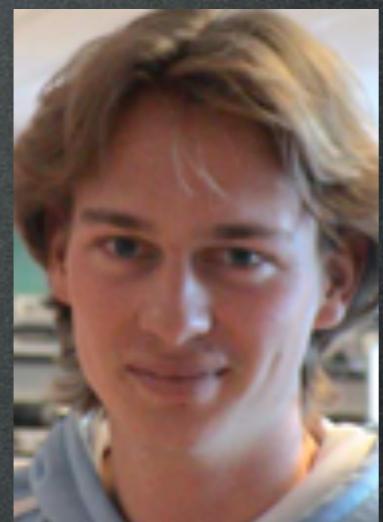
Scanning Tunneling Spectroscopy
Quasiparticle Interference



Milan P. Allan



Andreas W. Rost

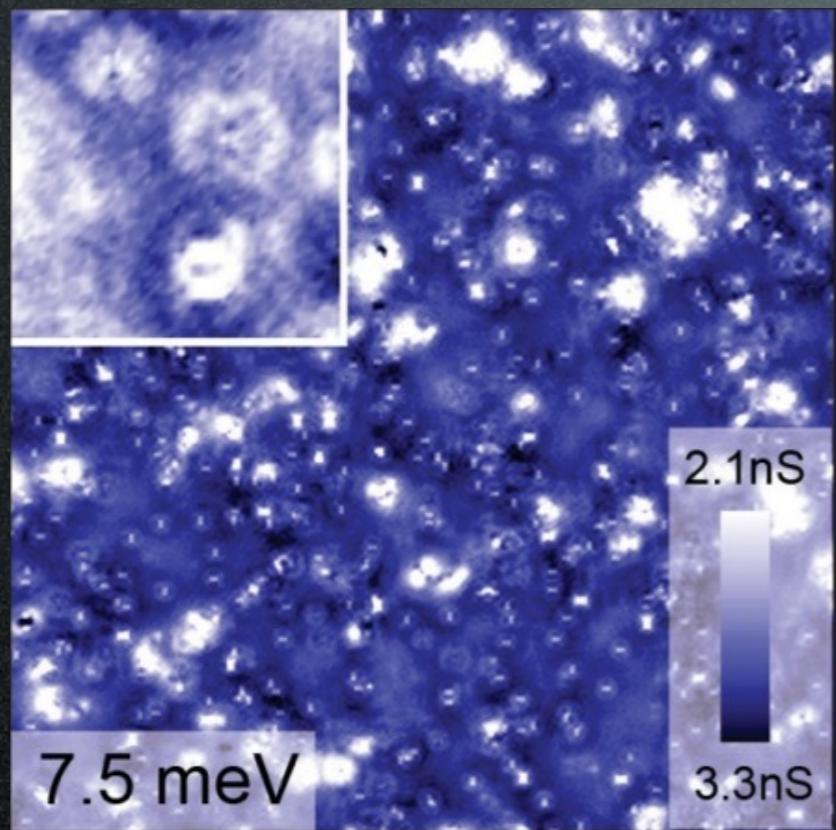


Freek Massee



J.C. Davis

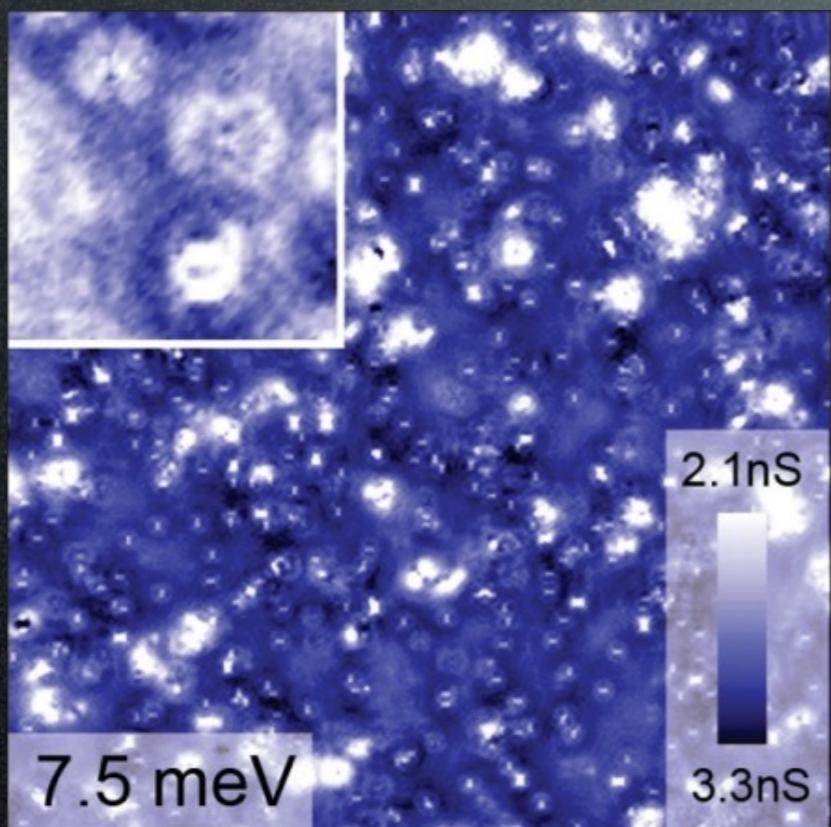
Scanning Tunneling Spectroscopy



$$g(\mathbf{r}, \omega = eV) \equiv \frac{dI}{dV}(\mathbf{r}, V)$$

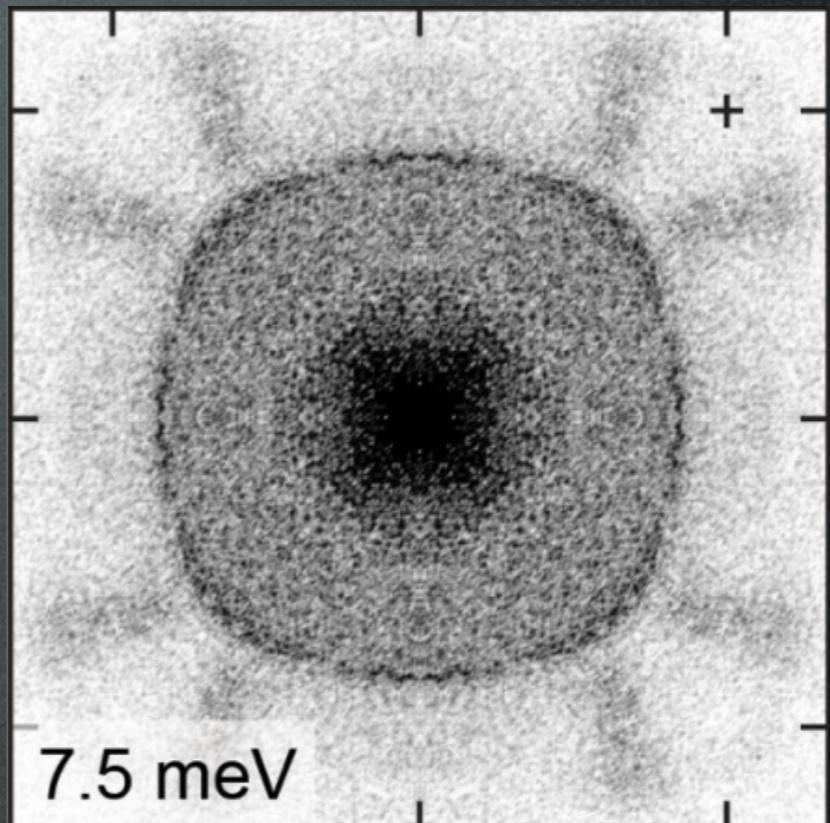
$g(\mathbf{r}, \omega)$

Quasiparticle Interference



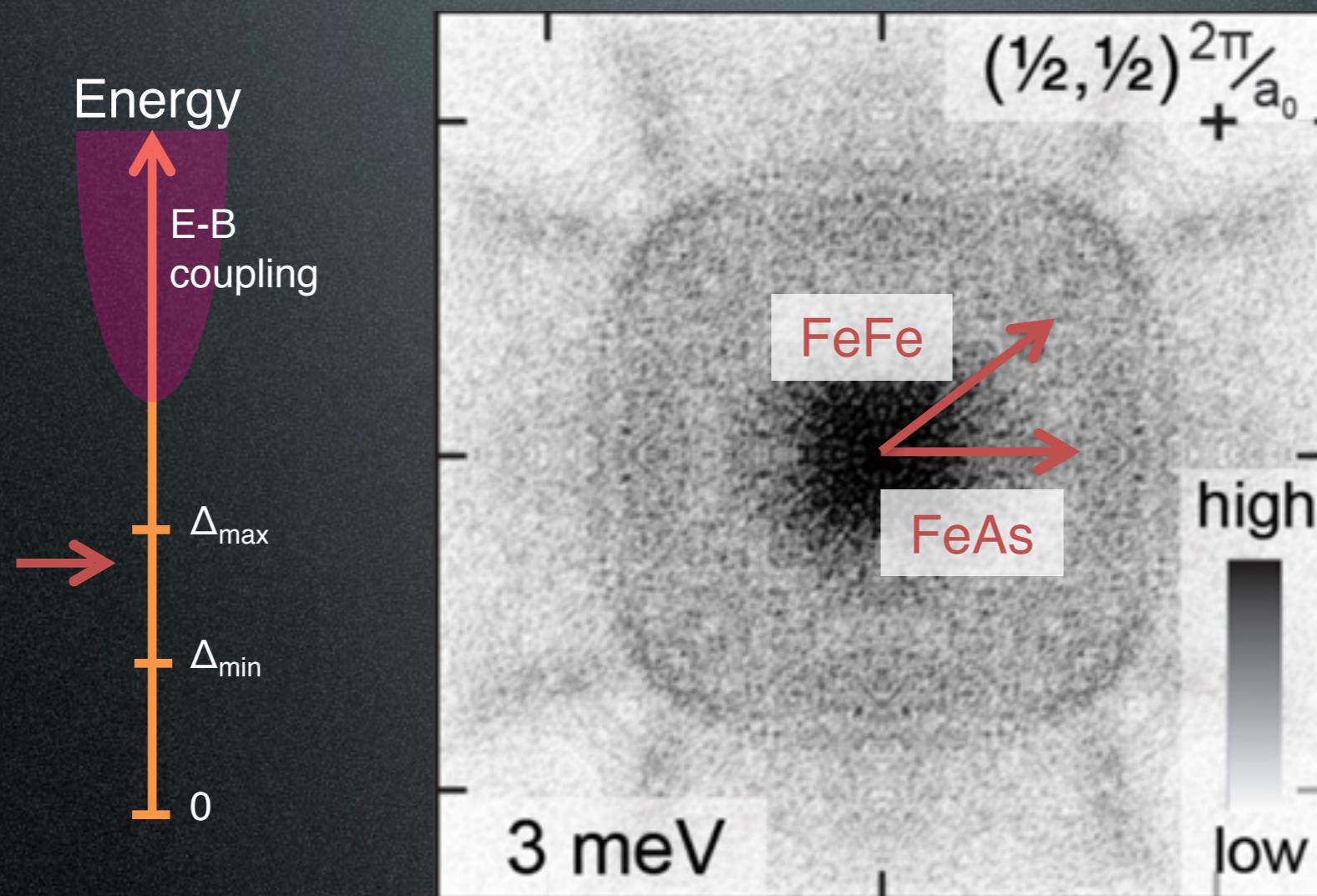
$g(\mathbf{r}, \omega)$

Fourier
Transform

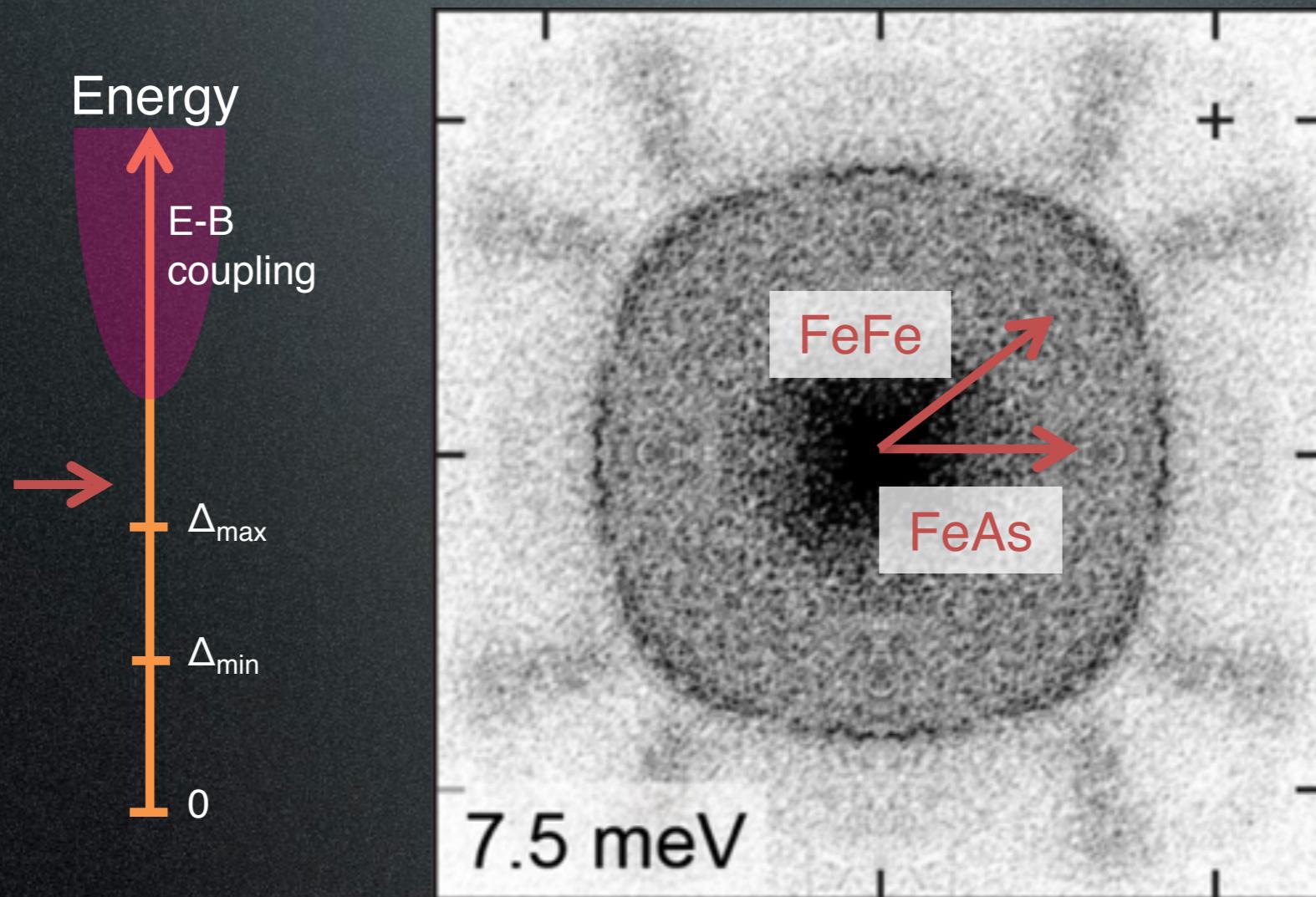


$g(\mathbf{q}, \omega)$

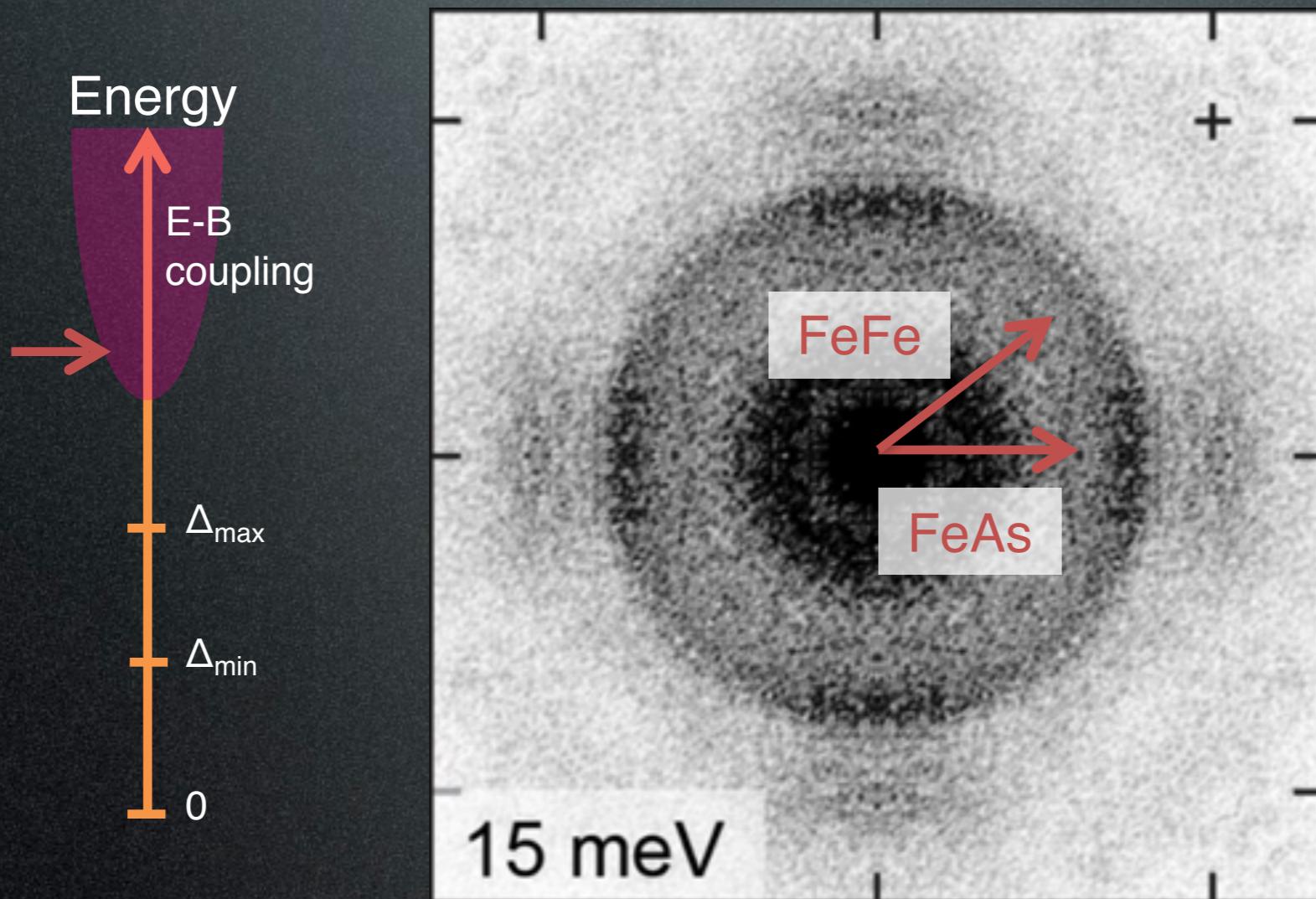
Energy dependent anisotropy



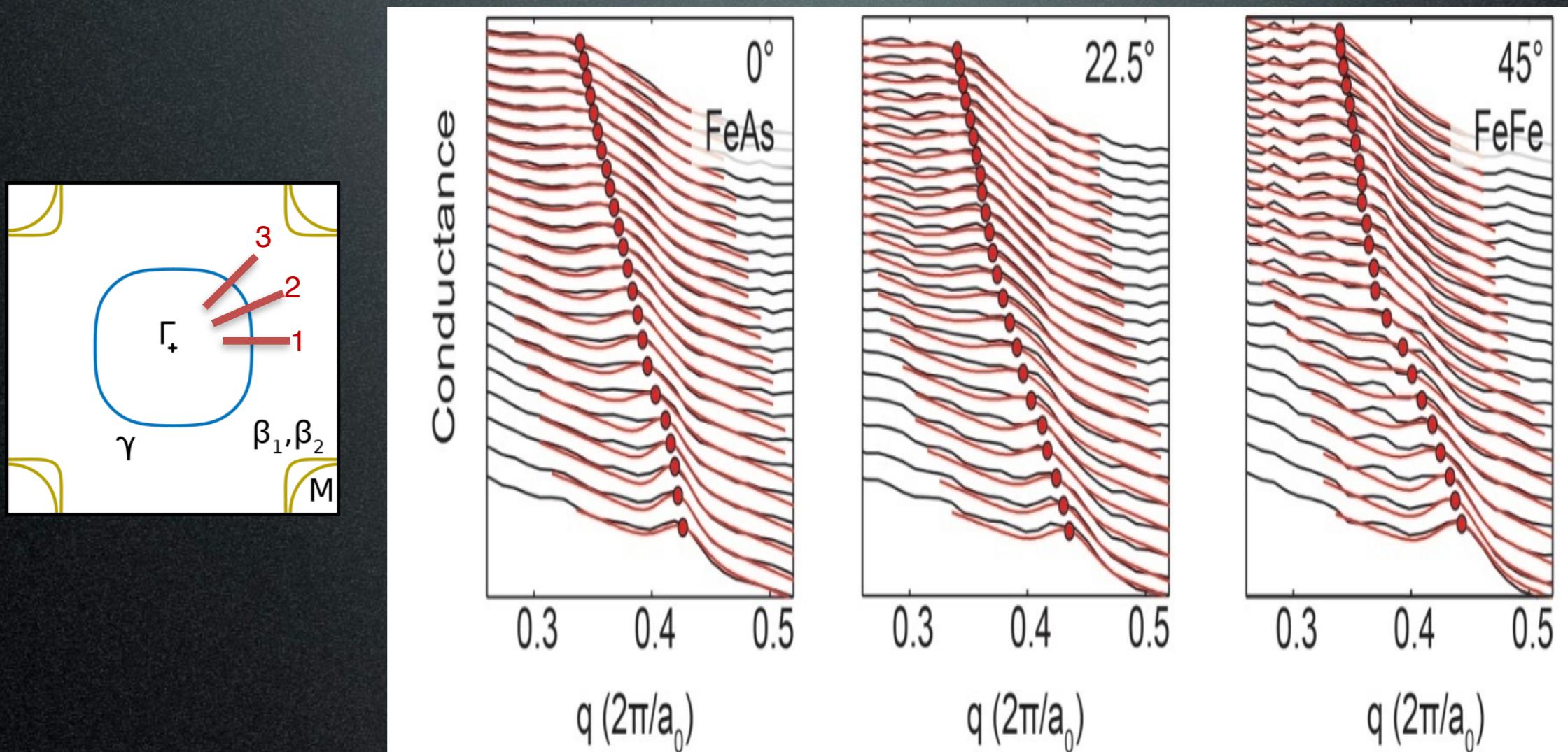
Energy dependent anisotropy



Energy dependent anisotropy



Energy dependent anisotropy



3. Match evidence to a suspect

Electron Self Energy



Kyungmin Lee



Mark Fischer

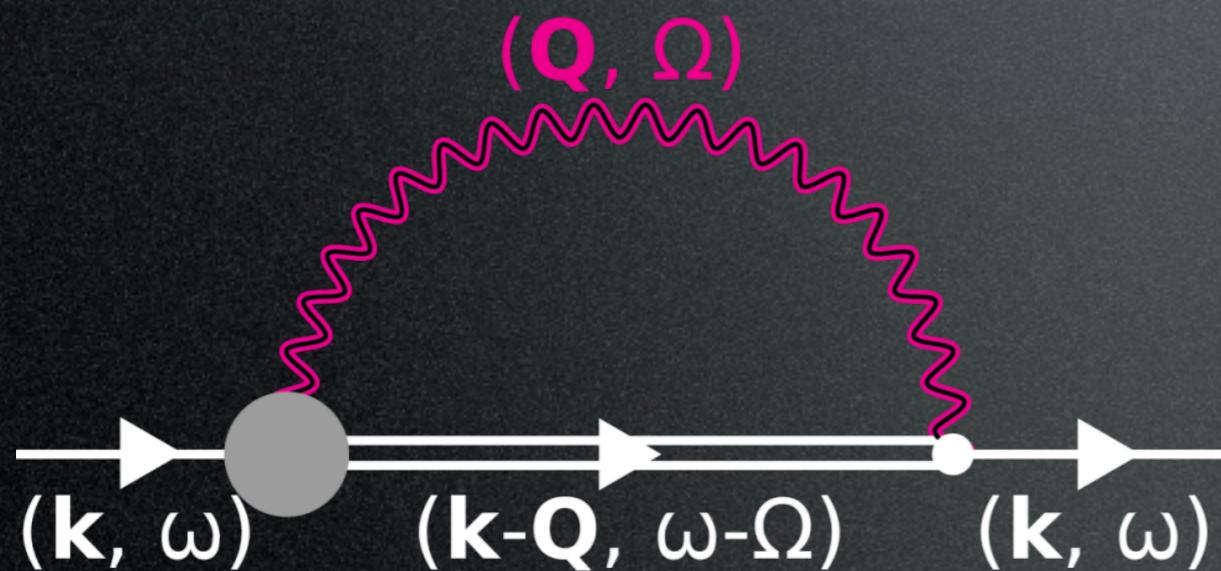
Self-Energy

Electron Self Energy

- Self energy captures electron-boson coupling

$$\hat{G}^{-1}(\mathbf{k}, \omega) = \hat{G}_0^{-1}(\mathbf{k}, \omega) - \hat{\Sigma}(\mathbf{k}, \omega)$$

- $\text{Re}\Sigma$: change in dispersion
- $\text{Im}\Sigma$: broadening

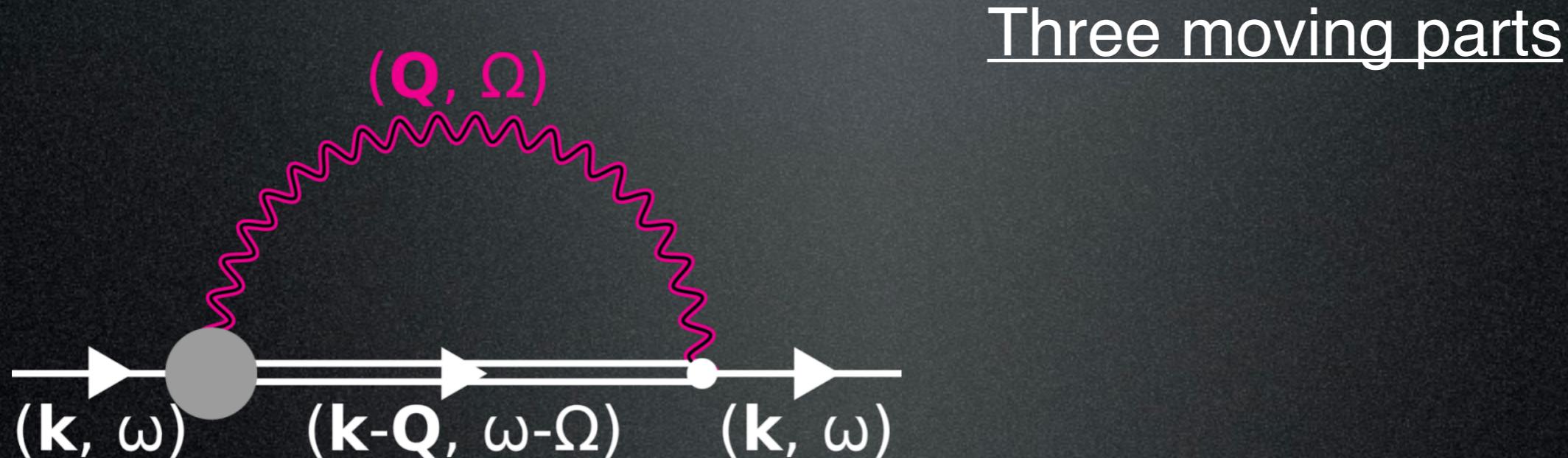


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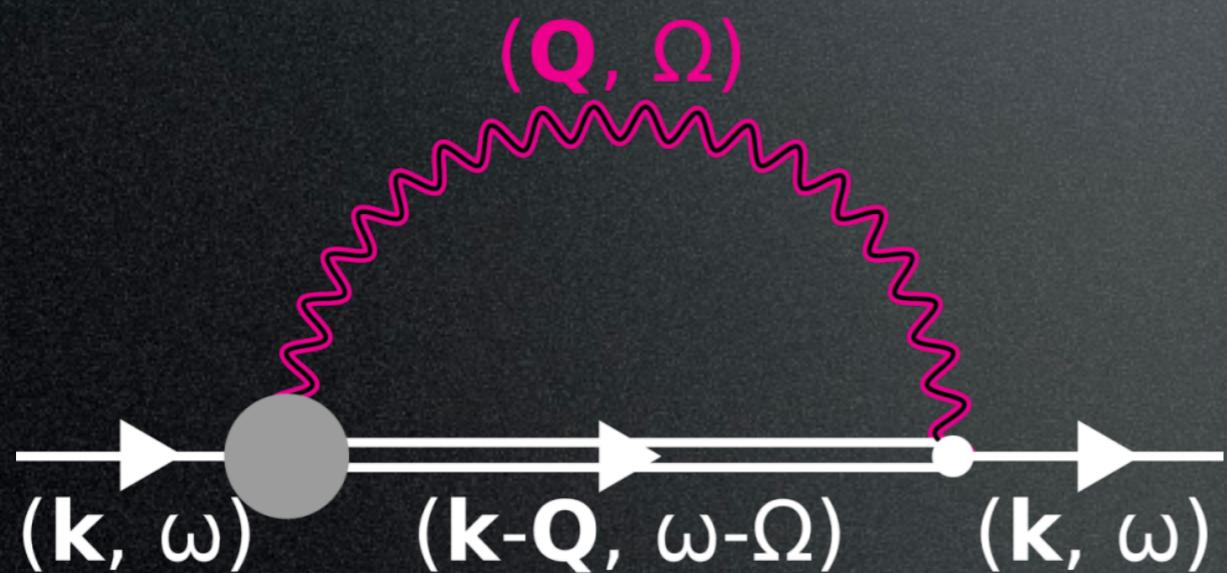


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Three moving parts

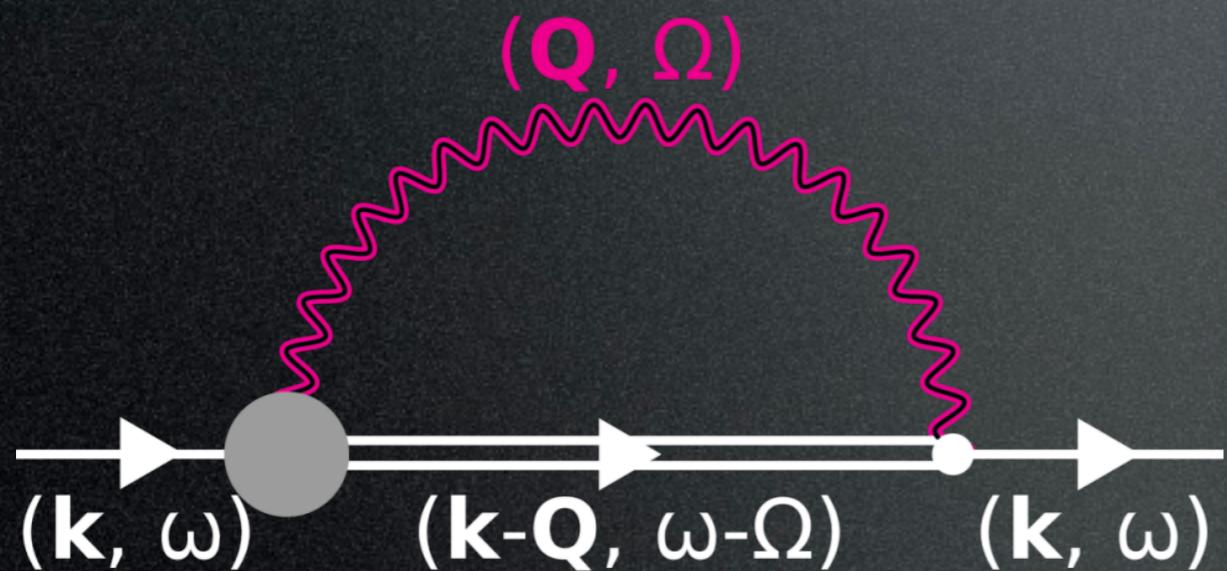
- Fermion propagator \Rightarrow

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Three moving parts

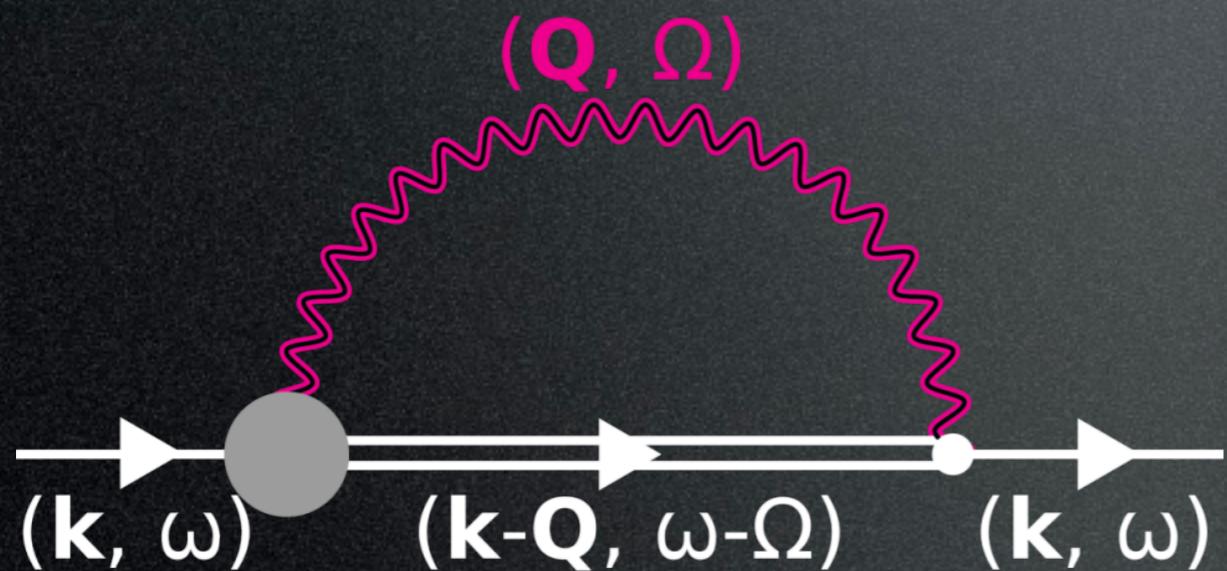
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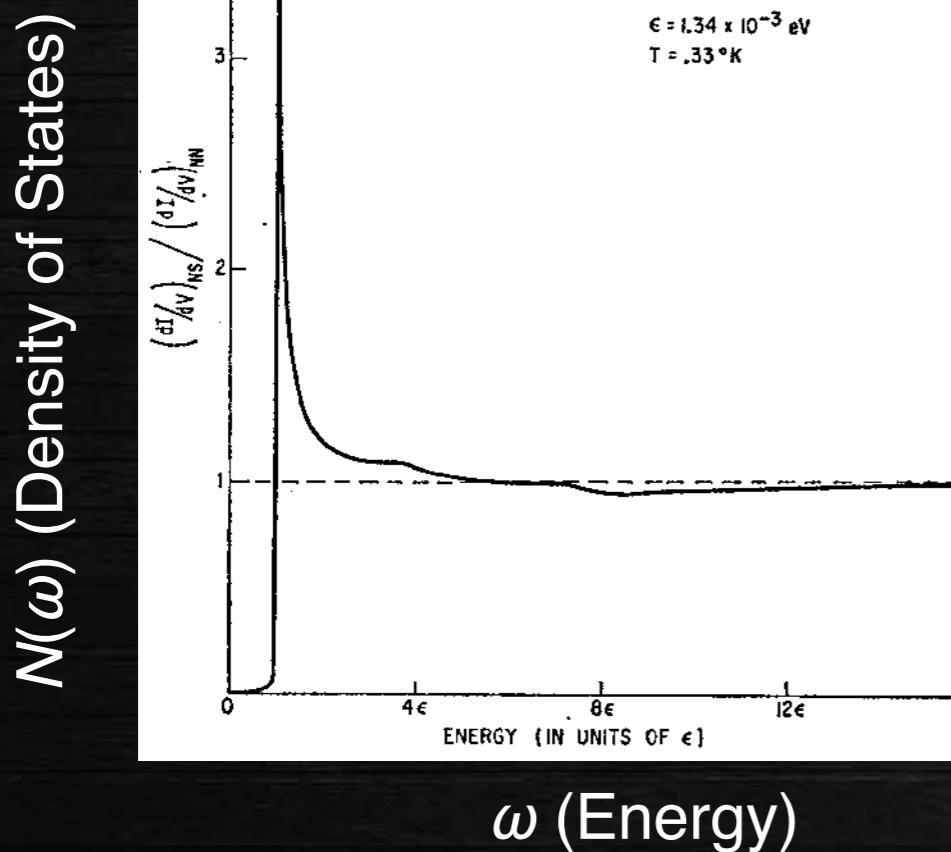


Three moving parts

- Fermion propagator
- Boson propagator
- Coupling vertex

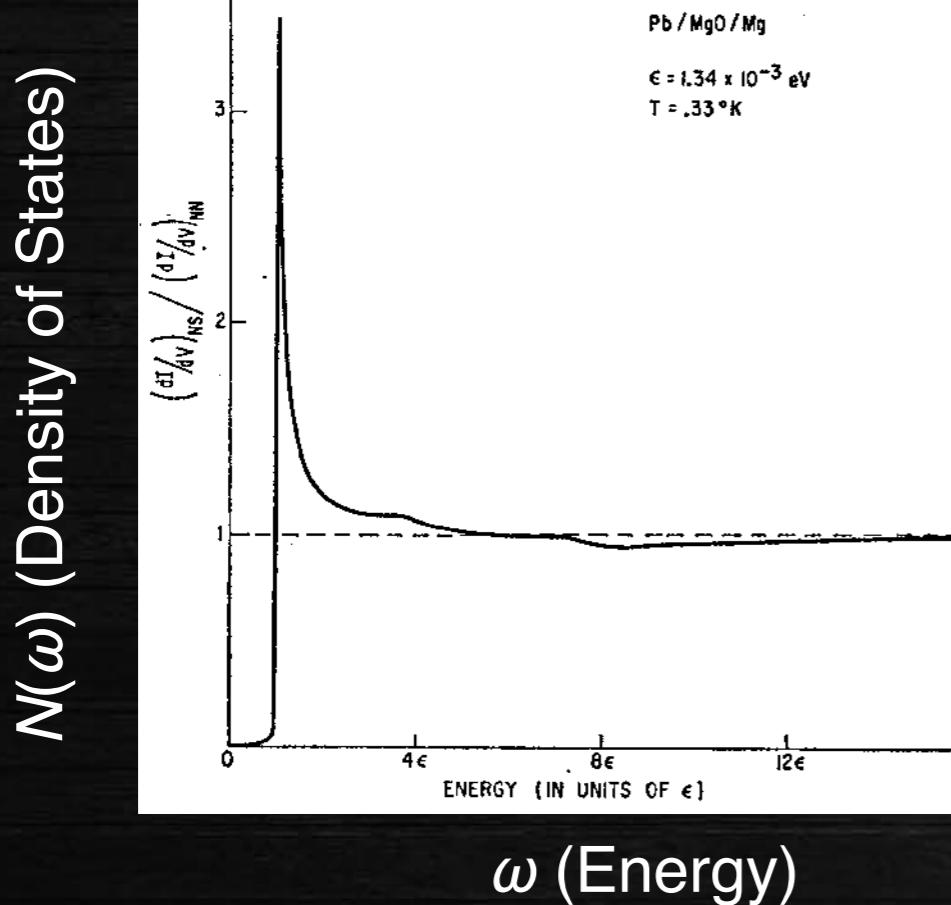
Classic Example: Pb

- Tunneling experiment
 - Superconducting Pb
 - Signature of electron-phonon coupling



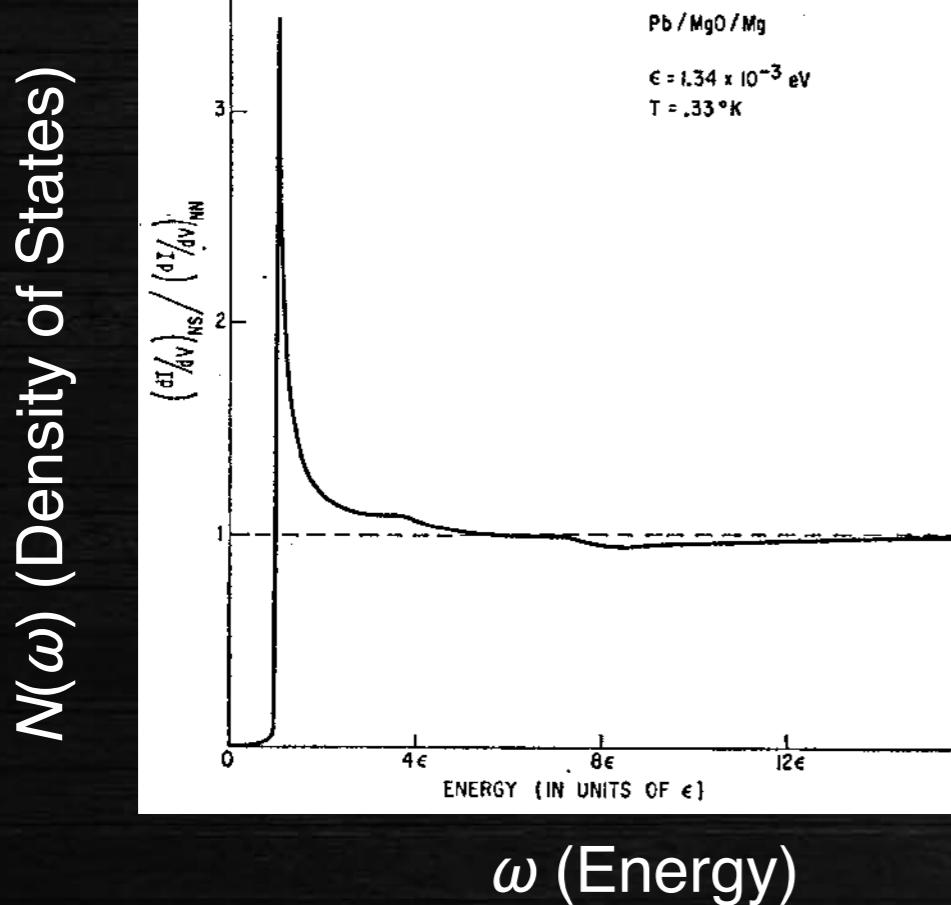
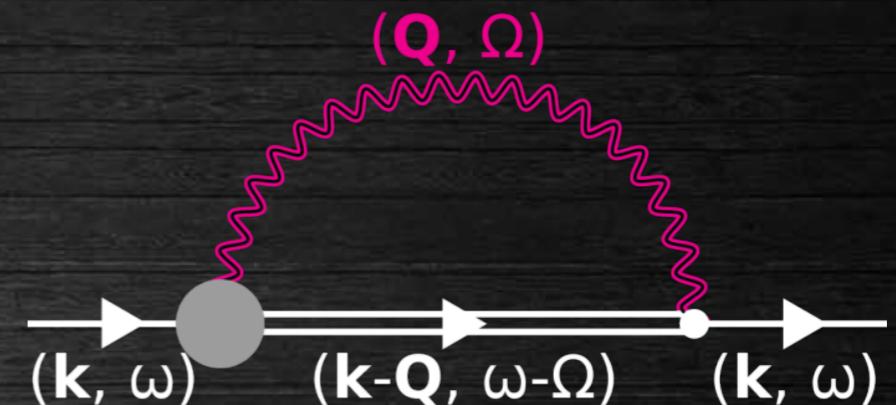
Classic Example: Pb

- Tunneling experiment
 - Superconducting Pb
 - Signature of electron-phonon coupling
- Migdal-Eliashberg,



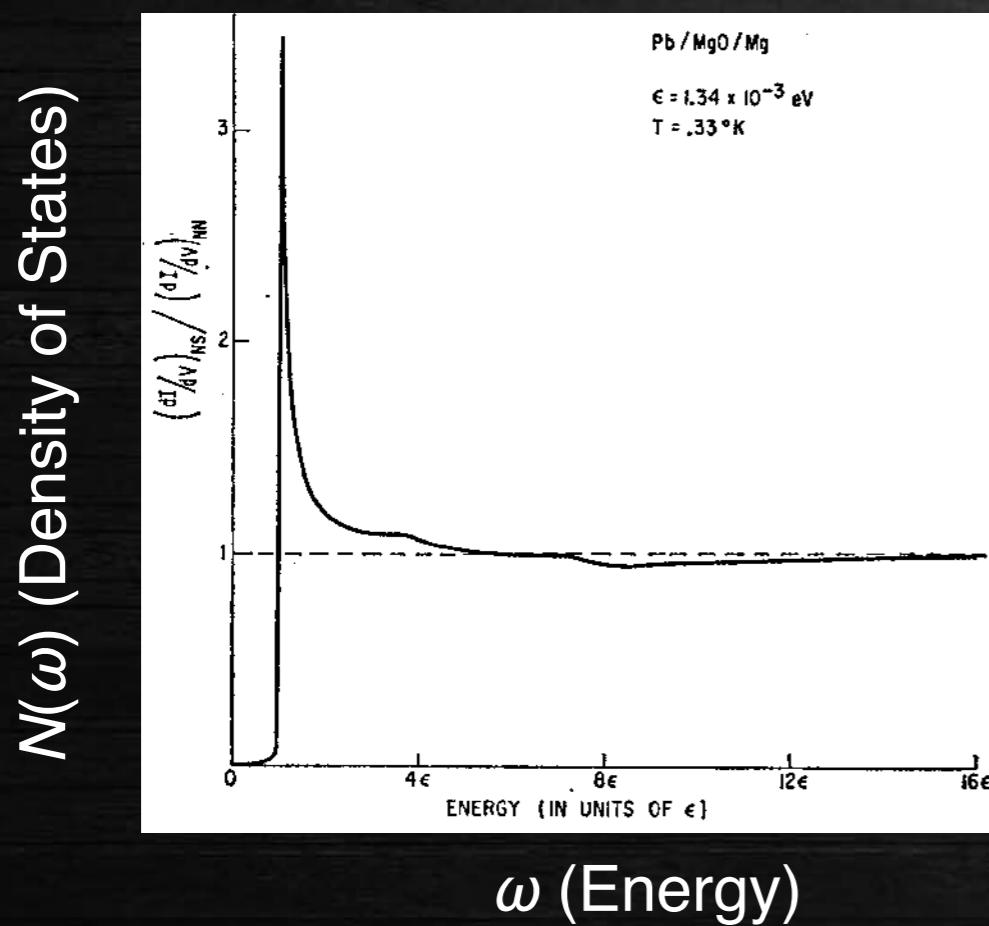
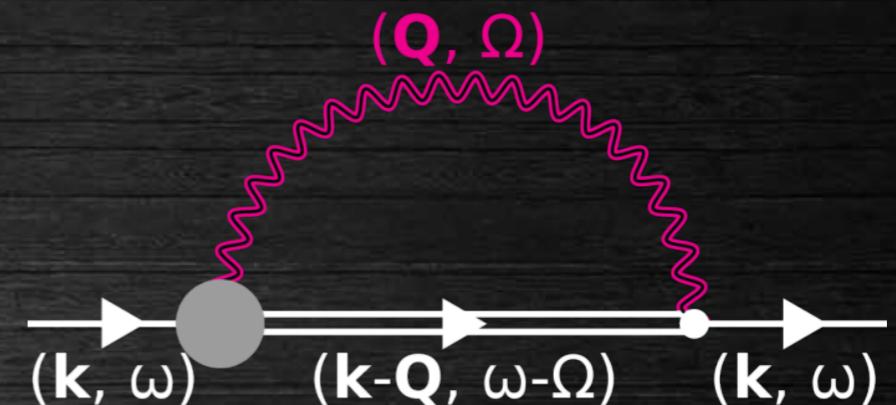
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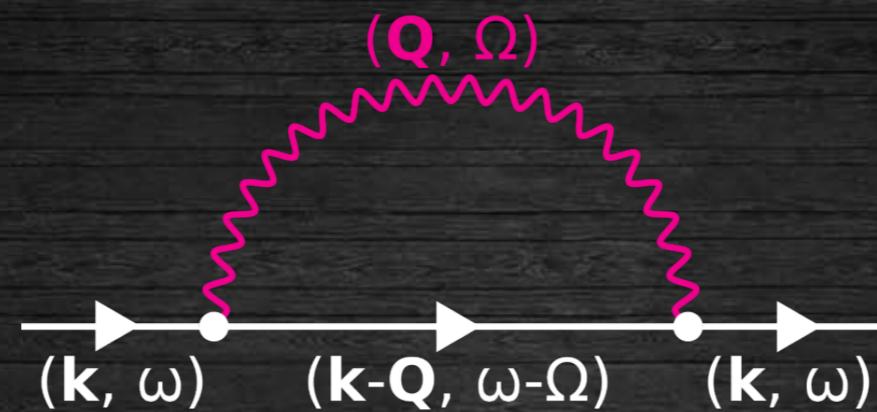


1. Start from Fermi liquid
 2. Compute self energy to all orders, ignoring vertex correction
- Boson coupling produces both SC and high energy fingerprint

Challenges

- No separation of scales for spin fluctuation
→ Vertex correction cannot be ignored
- Multiple bands
(5 Fe3d-orbitals)

Perturbative Self Energy

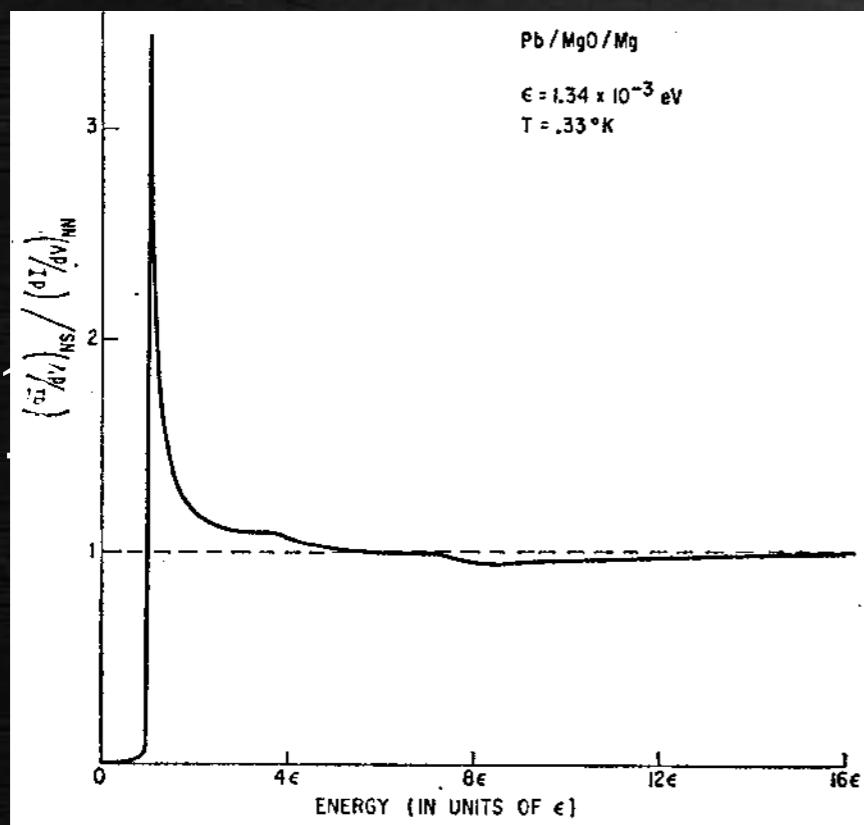


1. Start from experimentally measured gap (BdG)
2. Compute lowest order self energy
→ Boson coupling produces high energy fingerprint

Classic Example: Pb

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 - Superconducting Pb
 - Signature of electron-phonon coupling

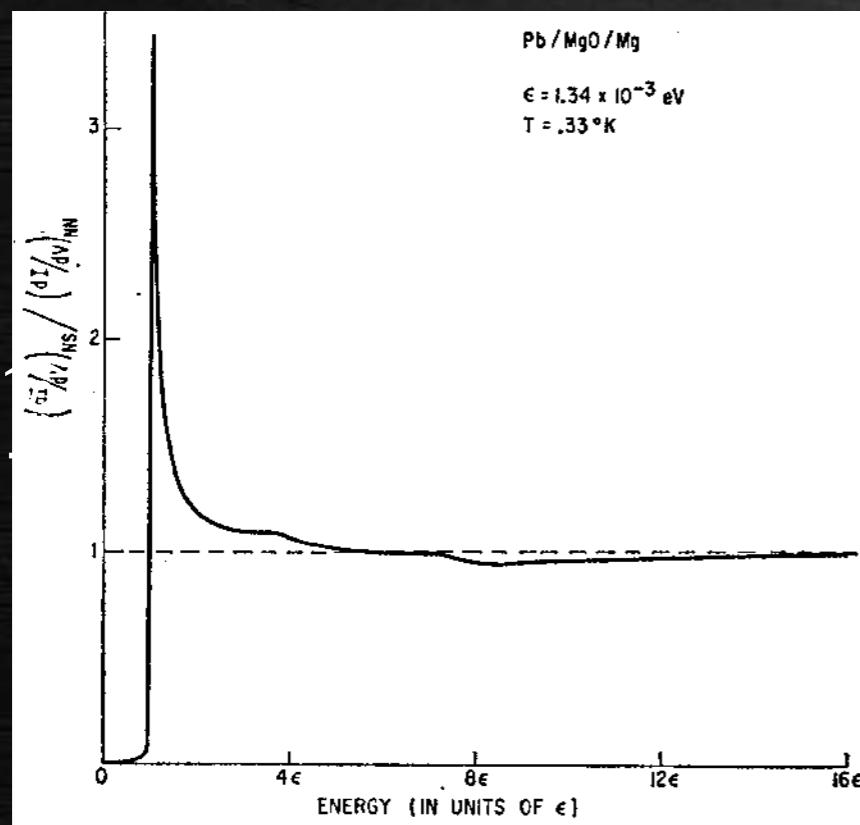
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y of
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ω (Energy)

Classic Example: Pb

- Tunneling
 - Superconducting Pb
 - Signature of electron-phonon coupling
- BdG + perturbative S.E.
 - Circular FS + S-wave Δ
 - Einstein phonon Ω
 - Reproduces deviation from BCS (mean field)

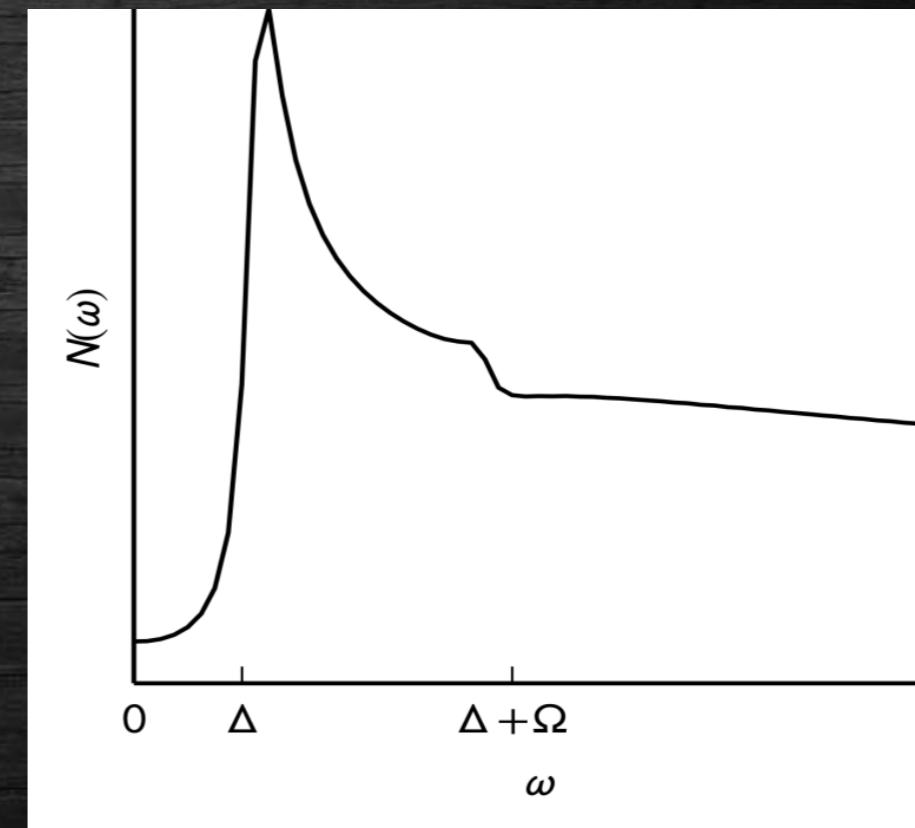
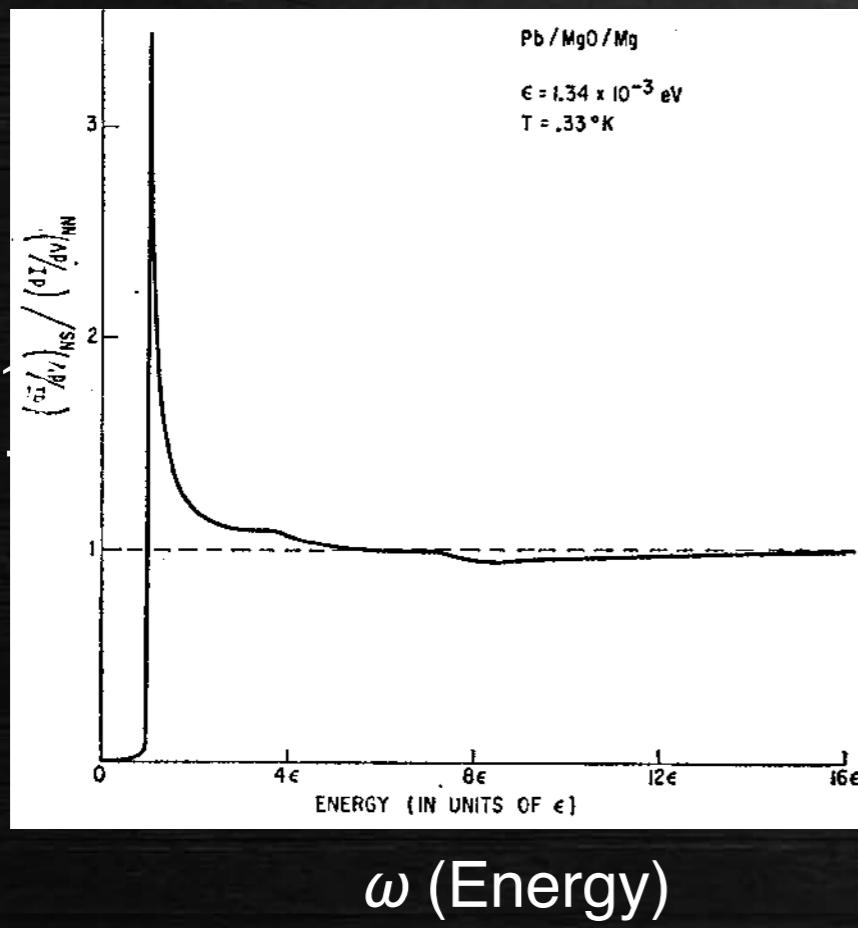


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What about cuprate?

Effect of an electron-phonon interaction on the one-electron spectral weight of a *d*-wave superconductor

A. W. Sandvik,^{1,2,*} D. J. Scalapino,^{2,†} and N. E. Bickers^{3,‡}

¹*Department of Physics, Åbo Akademi University, Porthansgatan 3, FIN-20500 Turku, Finland*

²*Department of Physics, University of California, Santa Barbara, California 93106-9530, USA*

³*Department of Physics, University of Southern California, Los Angeles, California 90089-0484, USA*

(Received 5 September 2003; published 30 March 2004)

Effect of an electron-phonon interaction on the one-electron spectral weight of a *d*-wave superconductor

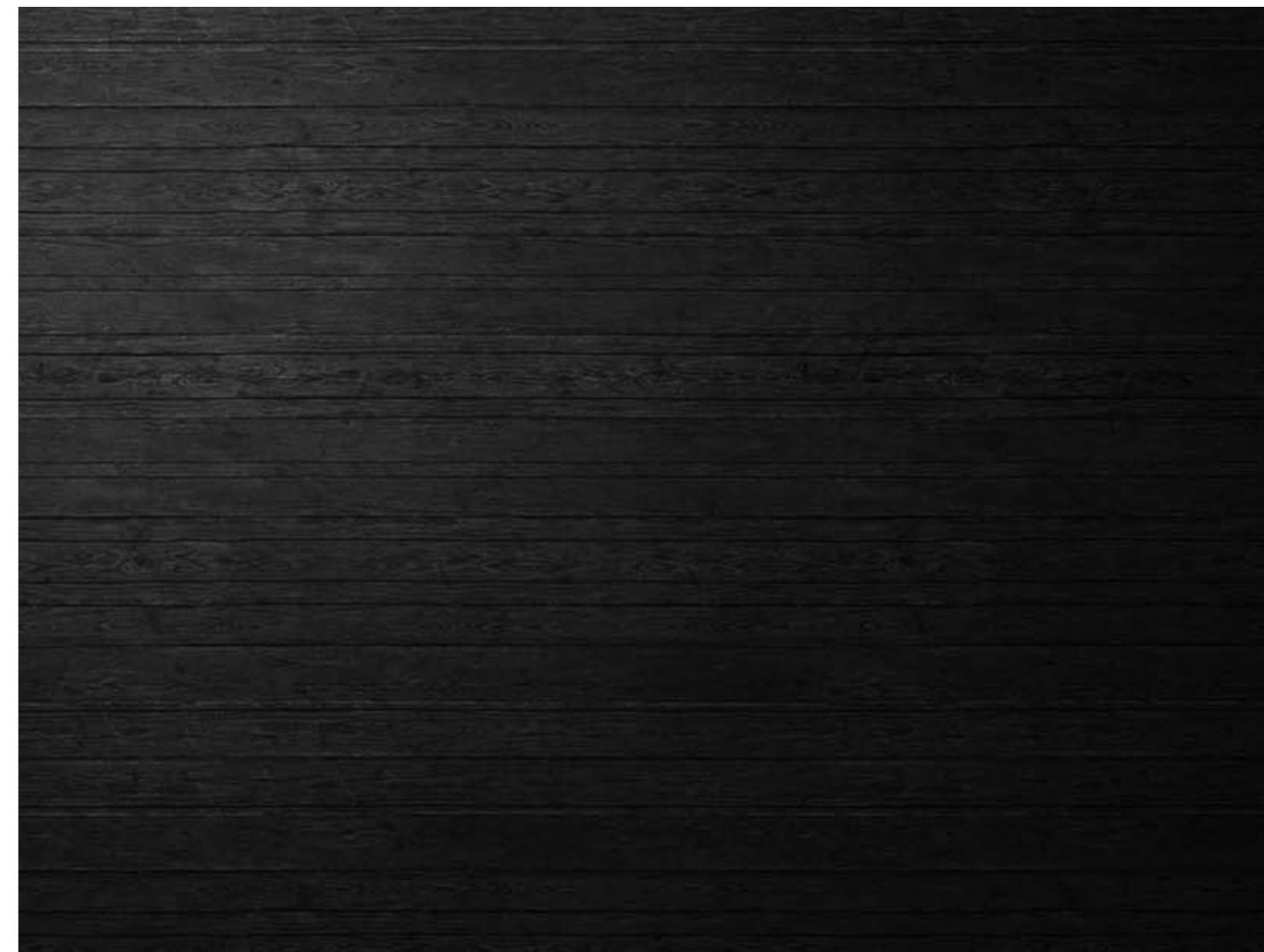
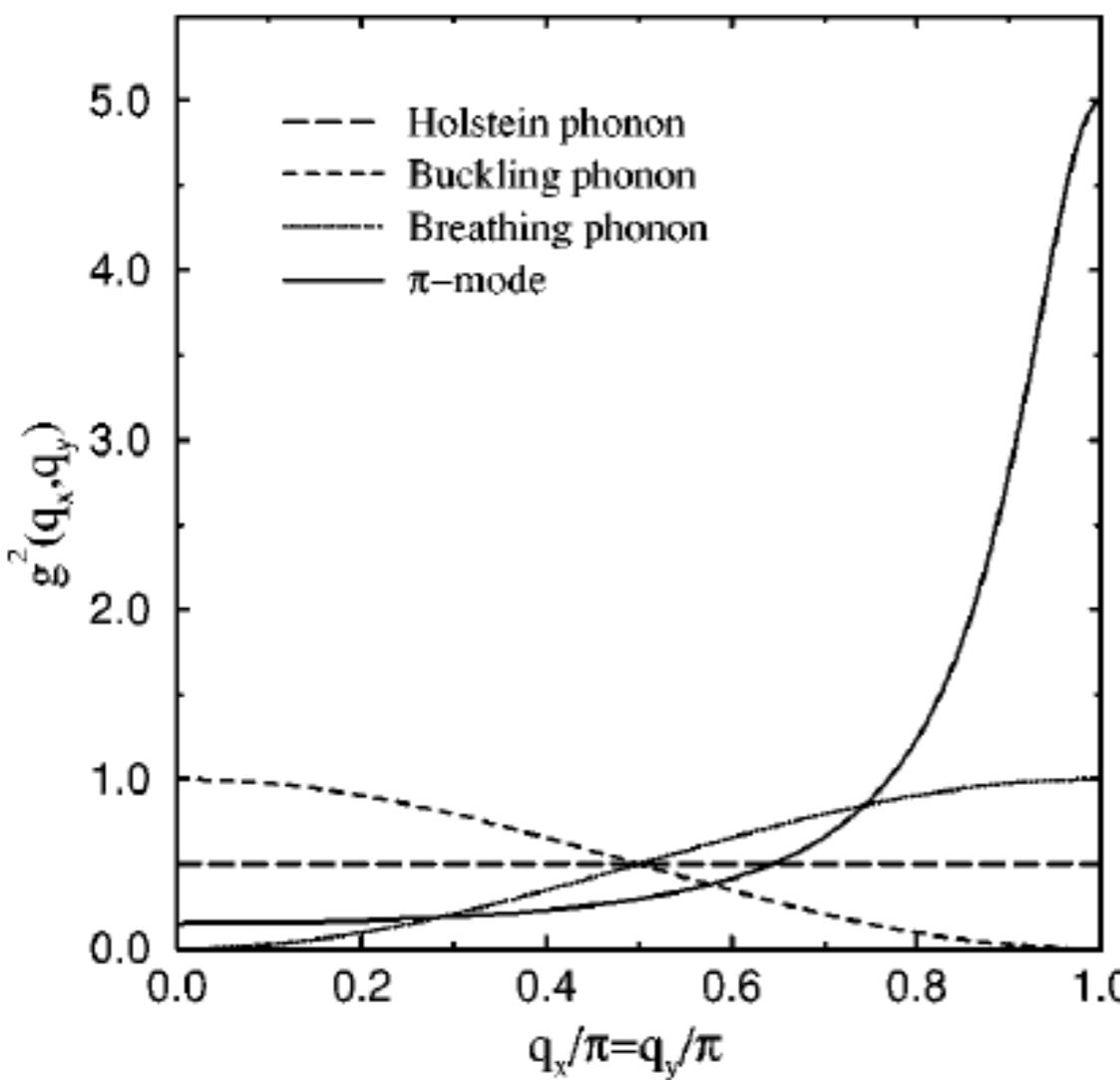
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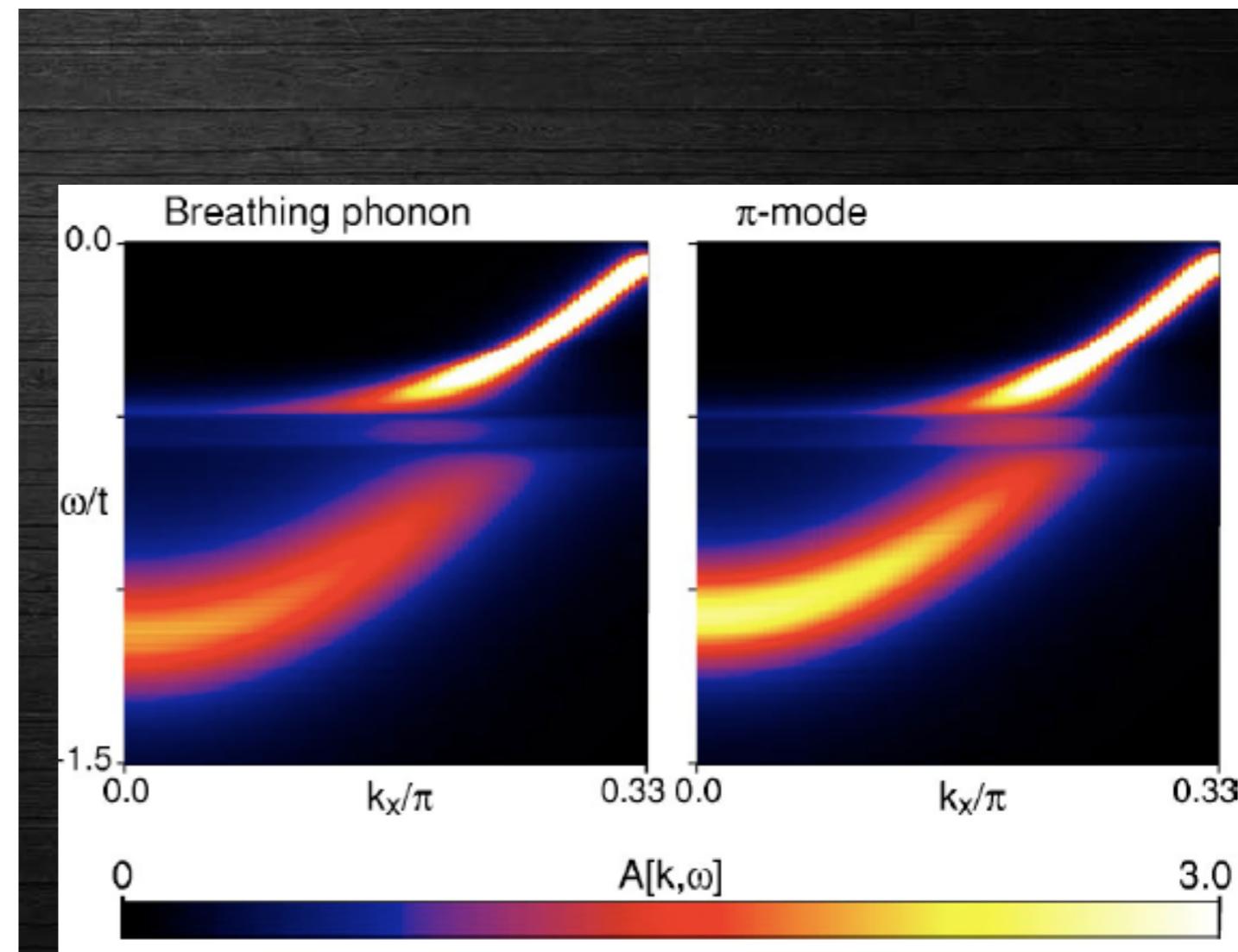
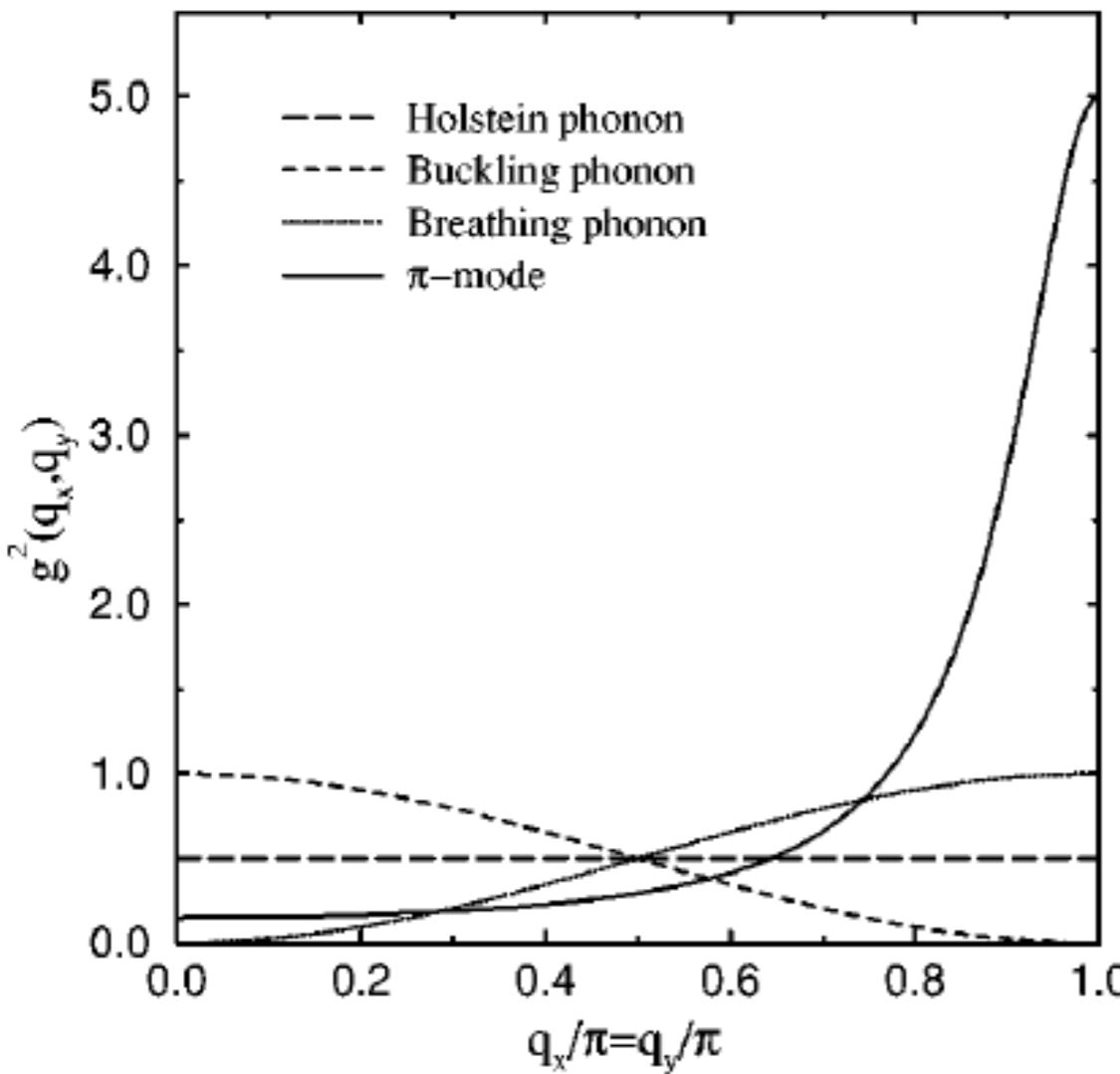
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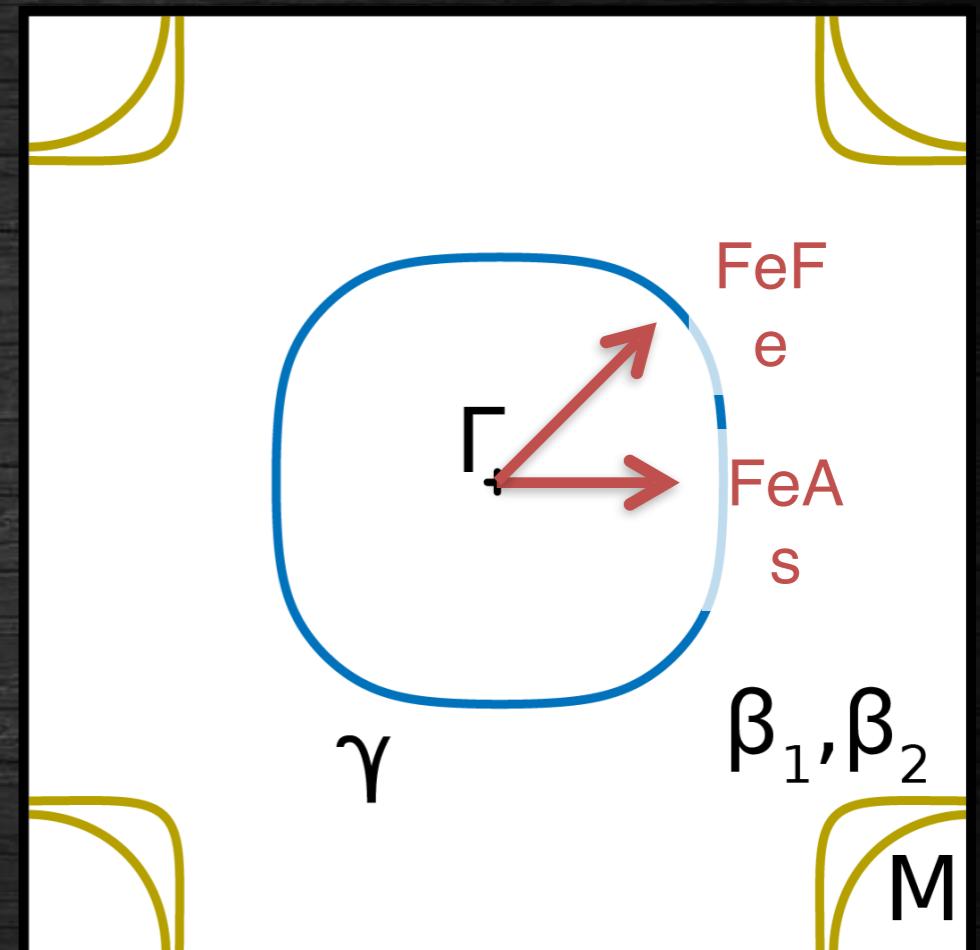
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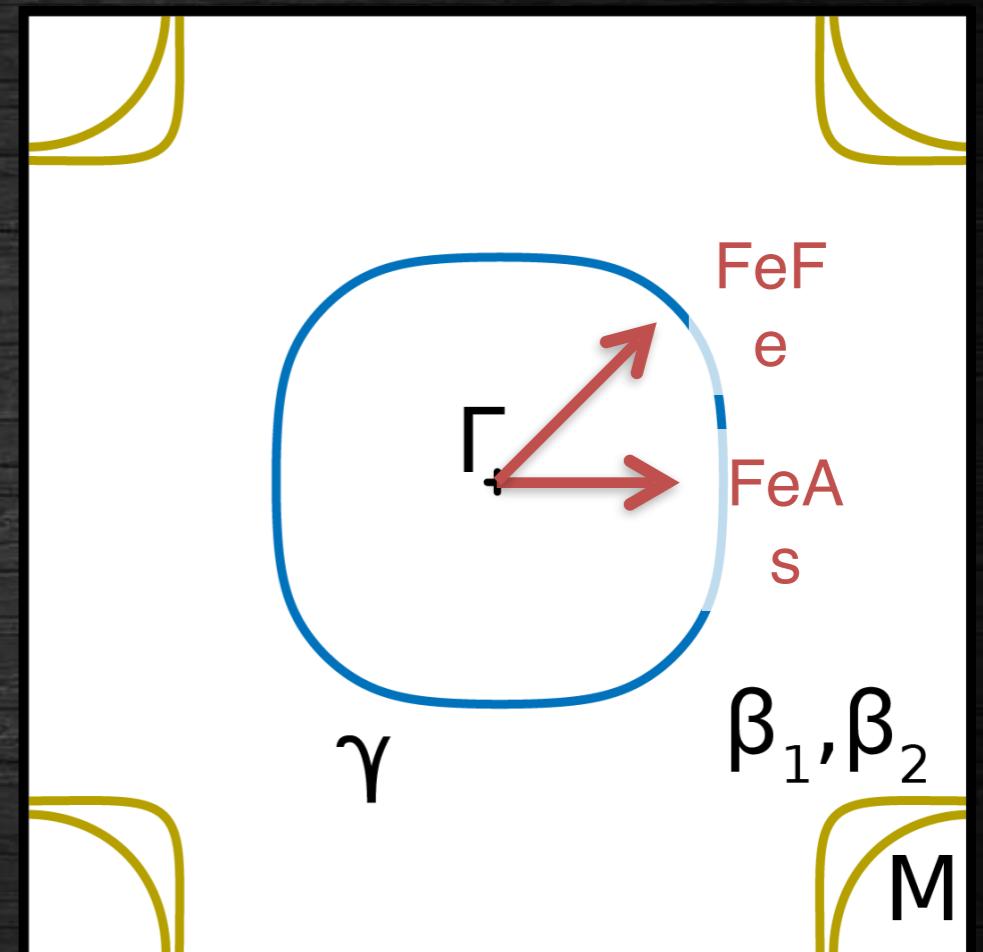
Model Electronic Structure of LiFeAs

- Three band model
 - Electron pockets (β_1, β_2) around M
 - Large hole pocket (γ) around Γ with uniform orbital character (d_{xy})

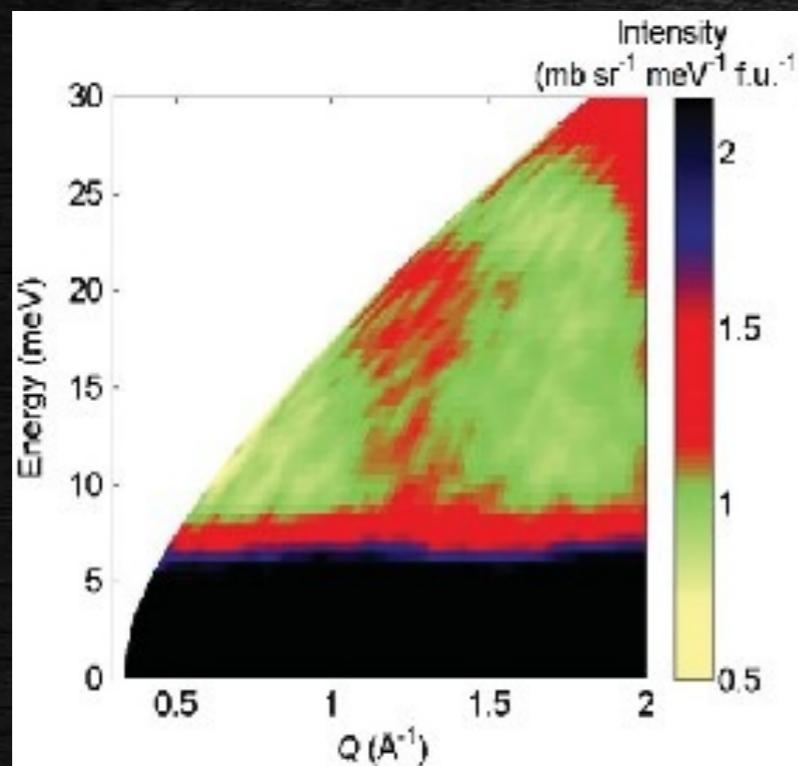


Model Electronic Structure of LiFeAs

- Three band model
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 - Large hole pocket (γ) around Γ with uniform orbital character (d_{xy})
- Experimentally measured Superconducting gap



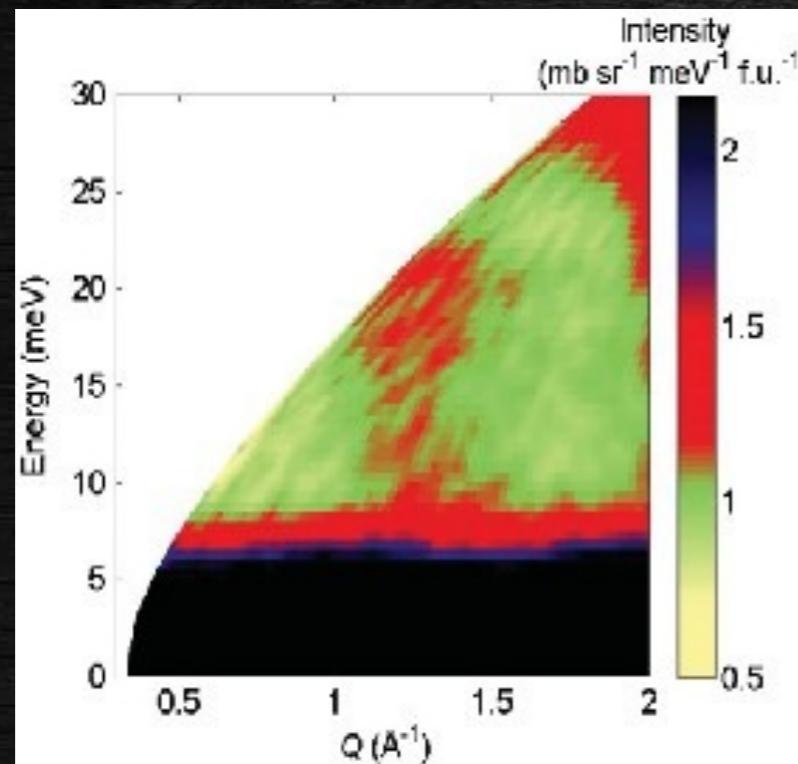
Model for AF Spin Fluctuation



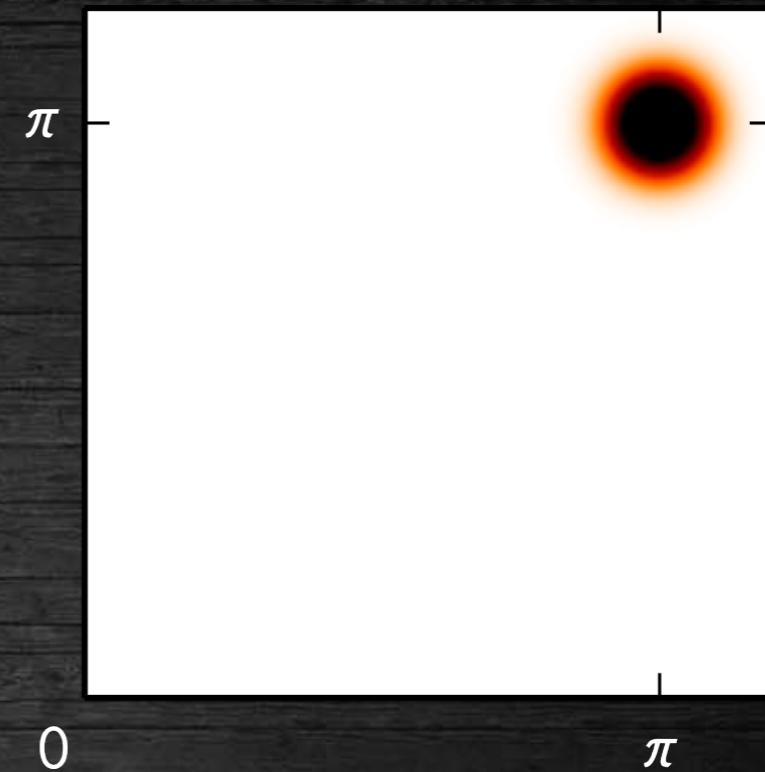
Taylor *et al.* 2011

- Peaked at $Q=(\pi, \pi)$ with energy $\Omega=6\text{meV}$

Model for AF Spin Fluctuation



Taylor *et al.* 2011

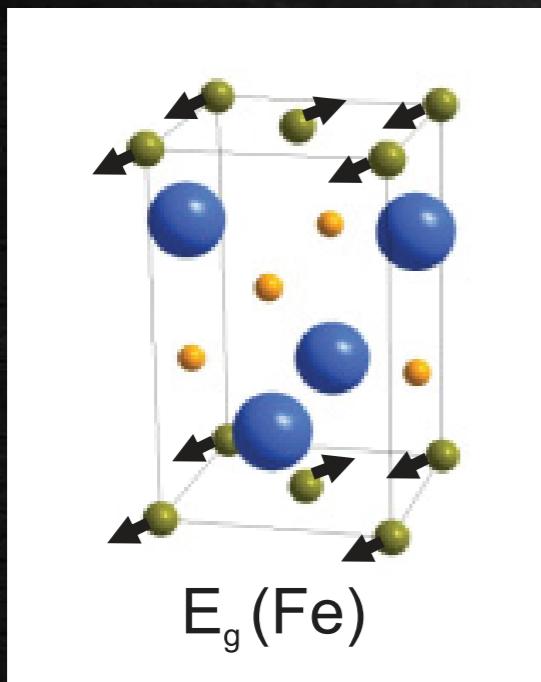


Model Spectral Weight

- Peaked at $Q=(\pi, \pi)$ with energy $\Omega=6\text{meV}$
- Gaussian with $\xi=6a$ (FWHM: $\sim 12\%$ of π/a)

Eg (Fe) phonon

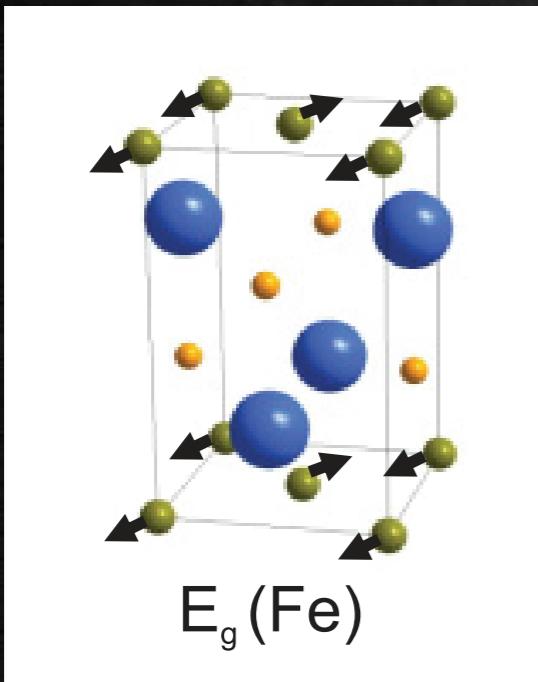
$\Omega=15\text{meV}$



- coupling vertex orbital dependent
→ effective momentum dependence

Eg (Fe) phonon

$\Omega=15\text{meV}$



- coupling vertex orbital dependent
→ effective momentum dependence
- Holstein Eg phonon was shown to induce orbital fluctuations

[Kontani & Onari, PRL 2010]

QPI Calculation with self-energy dressed Greens function

QPI Calculation with self-energy dressed Greens function

$$\hat{G}^{-1}(\mathbf{k}, \omega) = \hat{G}_0^{-1}(\mathbf{k}, \omega) - \hat{\Sigma}(\mathbf{k}, \omega)$$

QPI Calculation with self-energy dressed Greens function

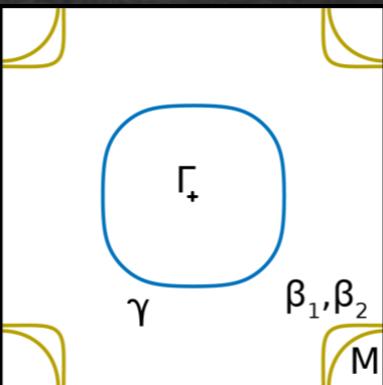
$$\hat{G}^{-1}(\mathbf{k}, \omega) = \hat{G}_0^{-1}(\mathbf{k}, \omega) - \hat{\Sigma}(\mathbf{k}, \omega)$$

$$g(\mathbf{q}, \omega) \propto \text{Im} \sum_{\mathbf{k}} \left[\hat{G}(\mathbf{k}, \omega) \hat{T} \hat{G}(\mathbf{k} + \mathbf{q}, \omega) \right]^{11}$$

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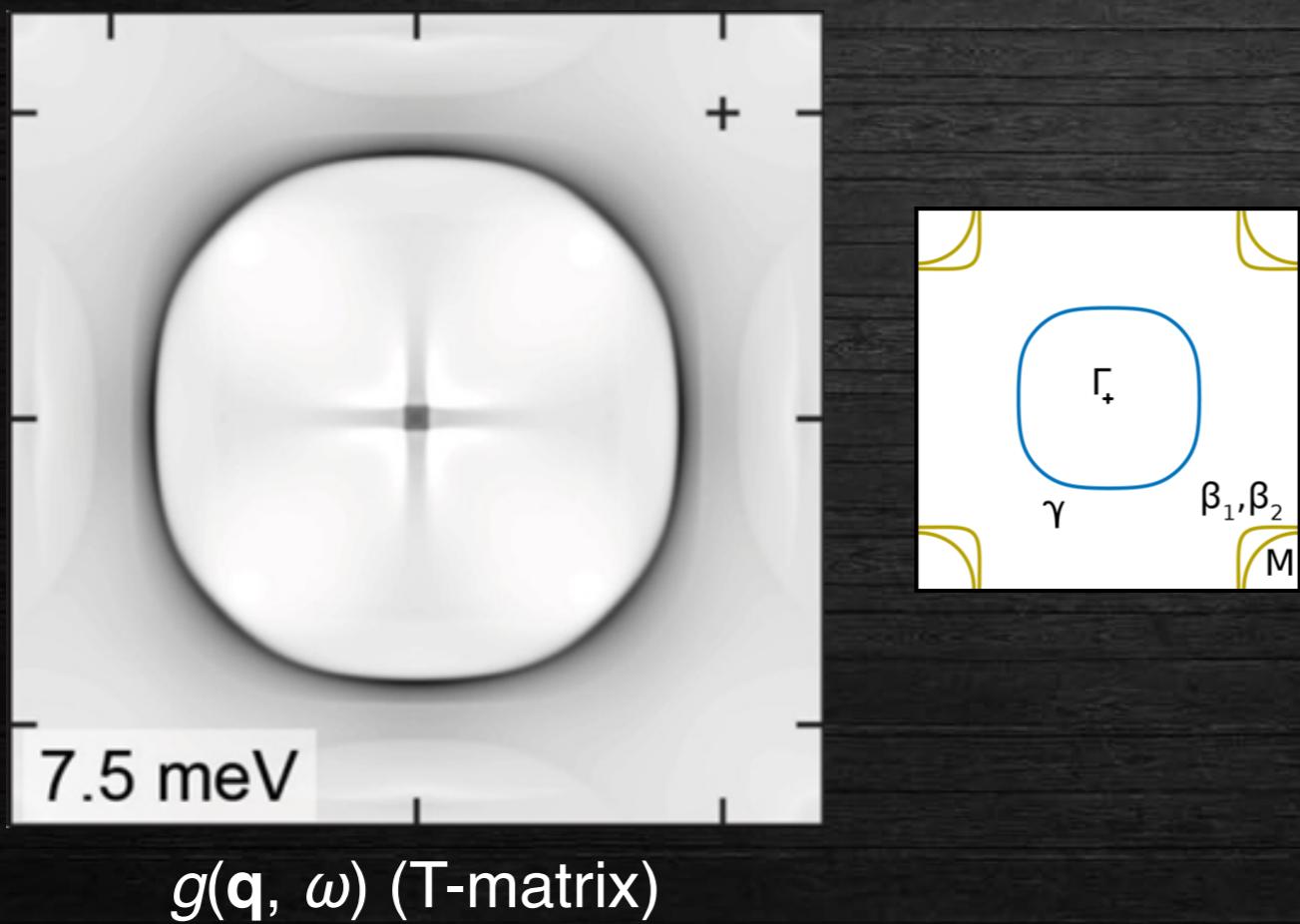
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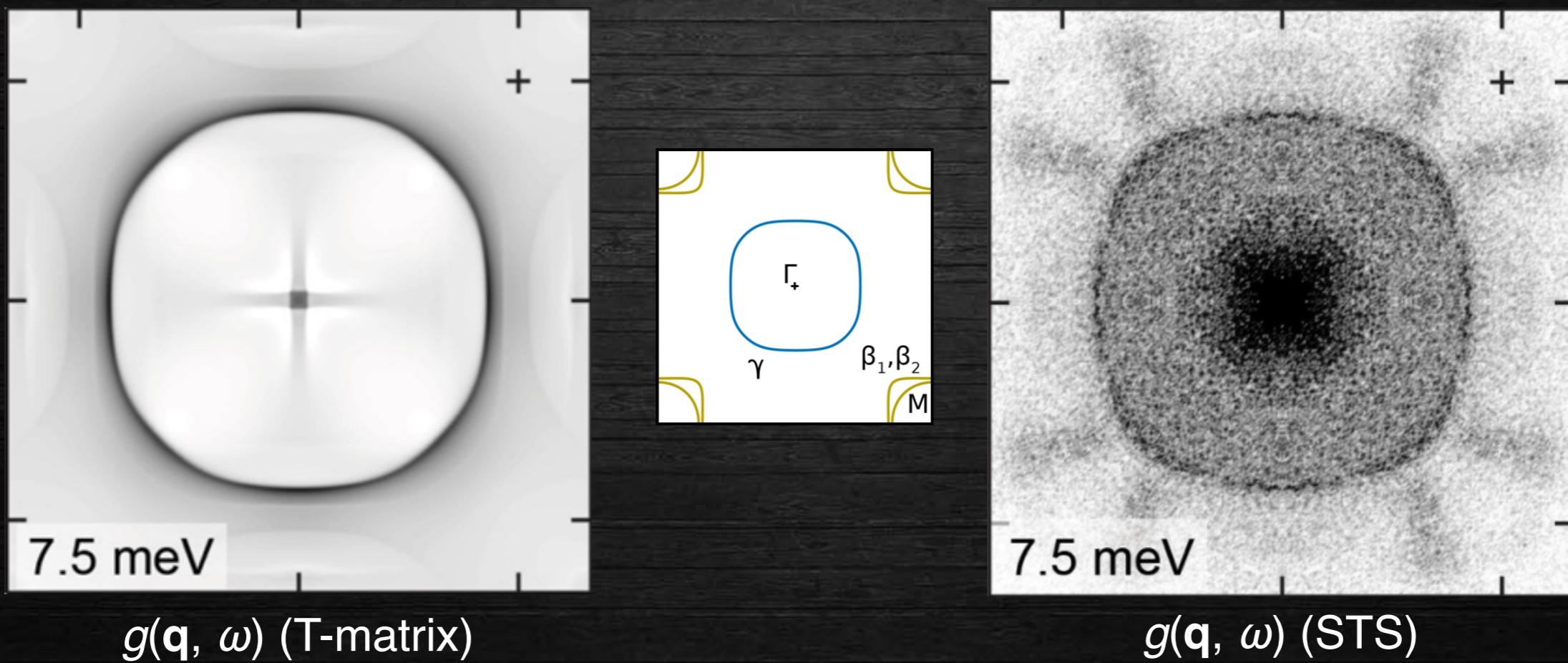
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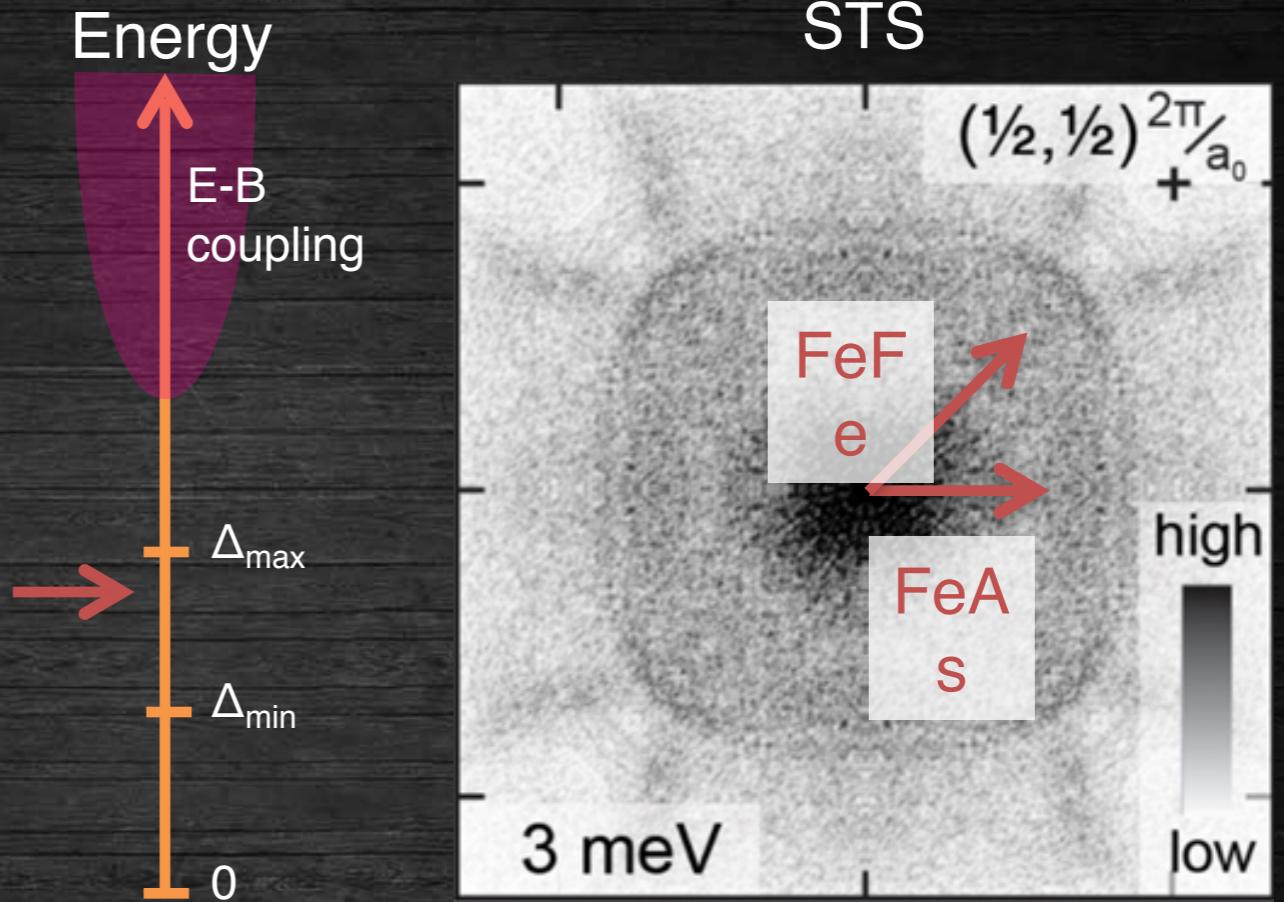
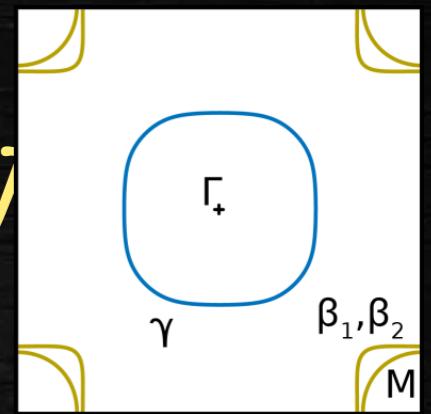
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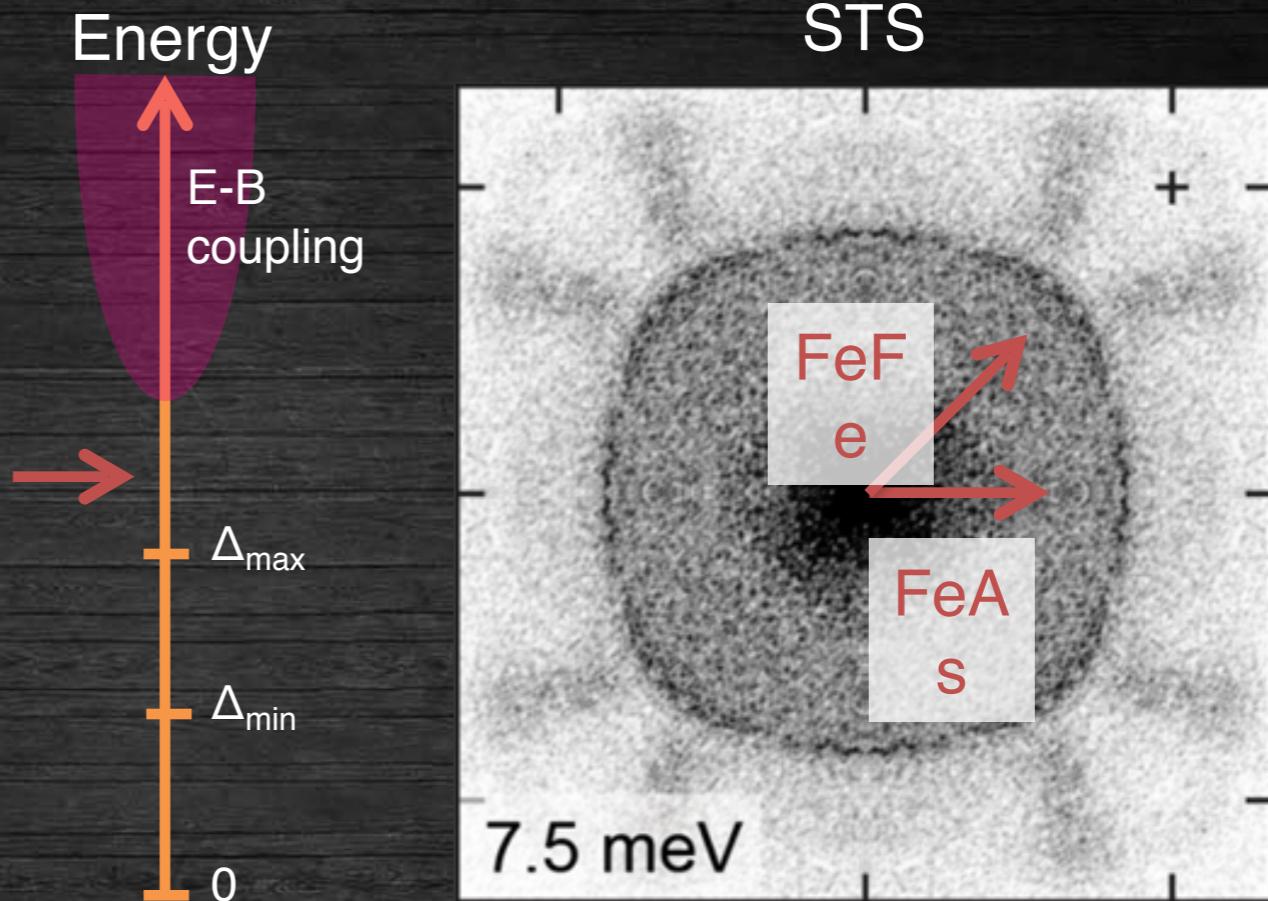
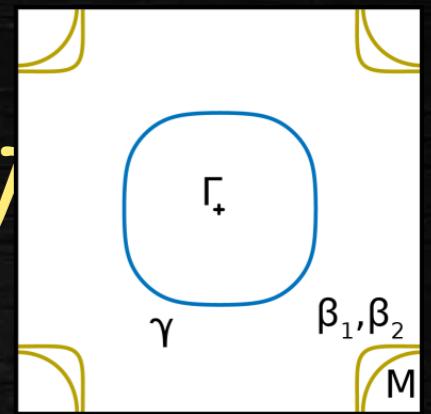
*Comparison of
Theory and Experiment*

Self-energy due to AFSF

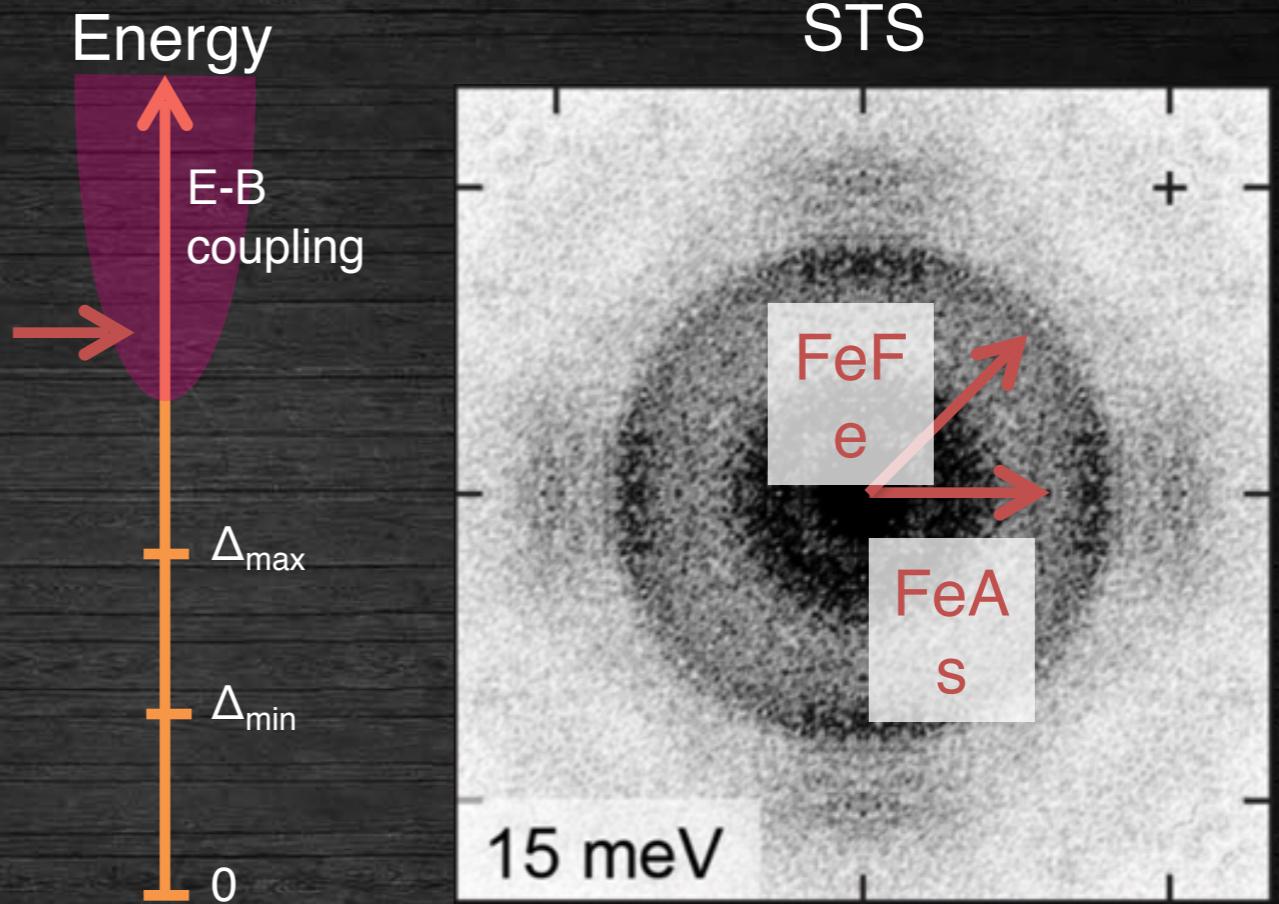
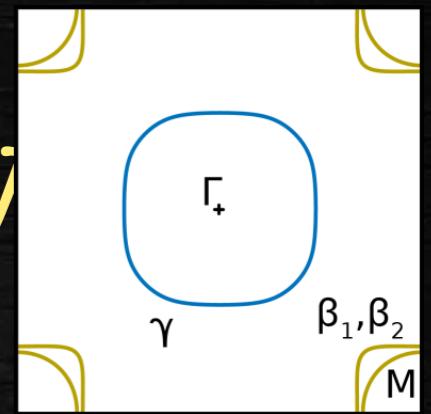
Energy Dependent Anisotropy



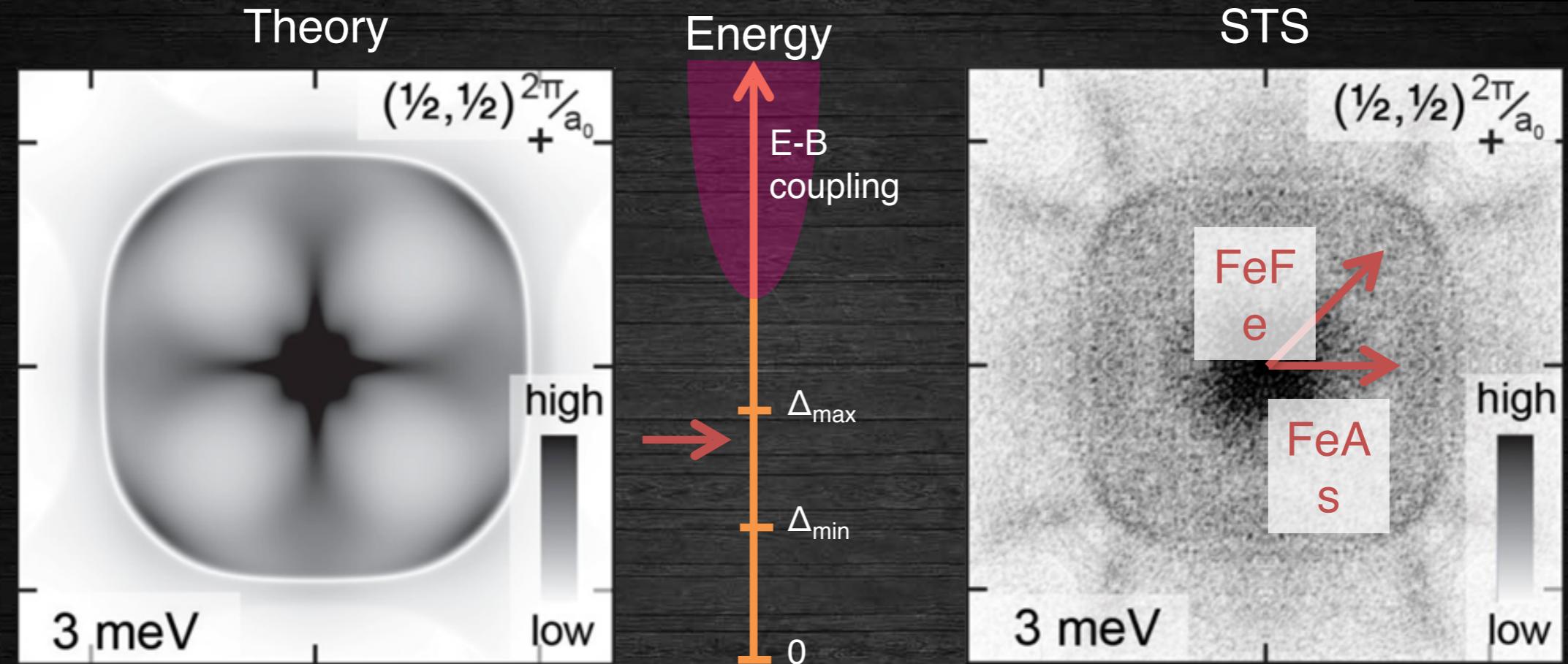
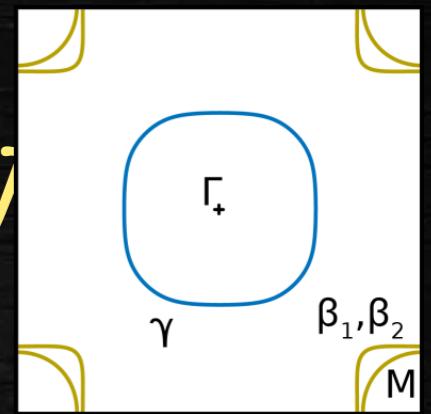
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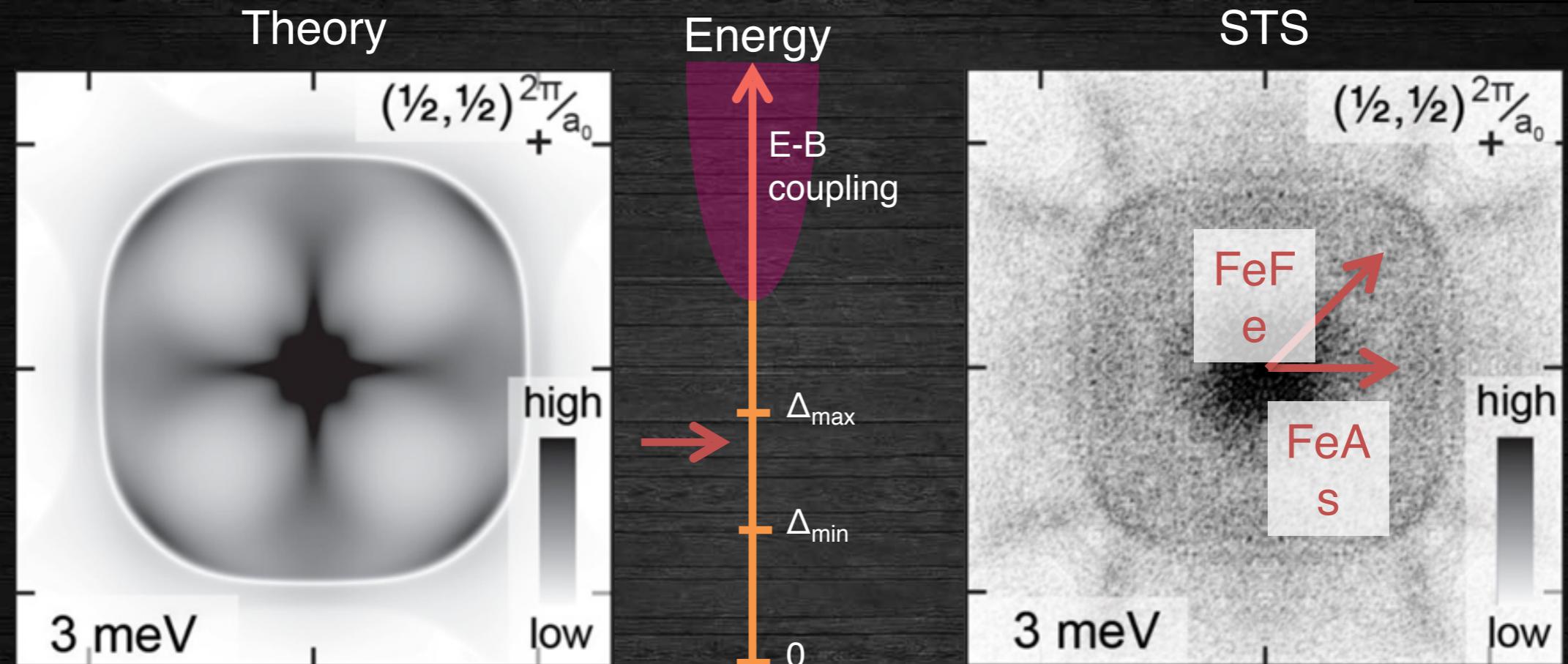
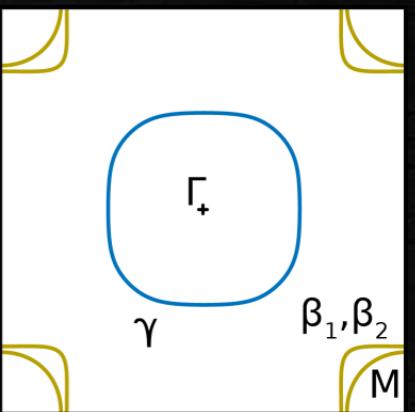
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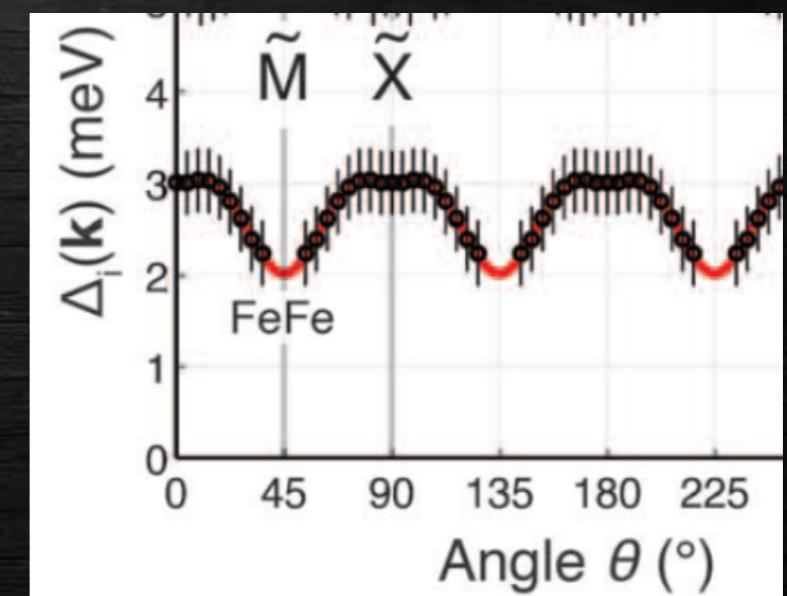
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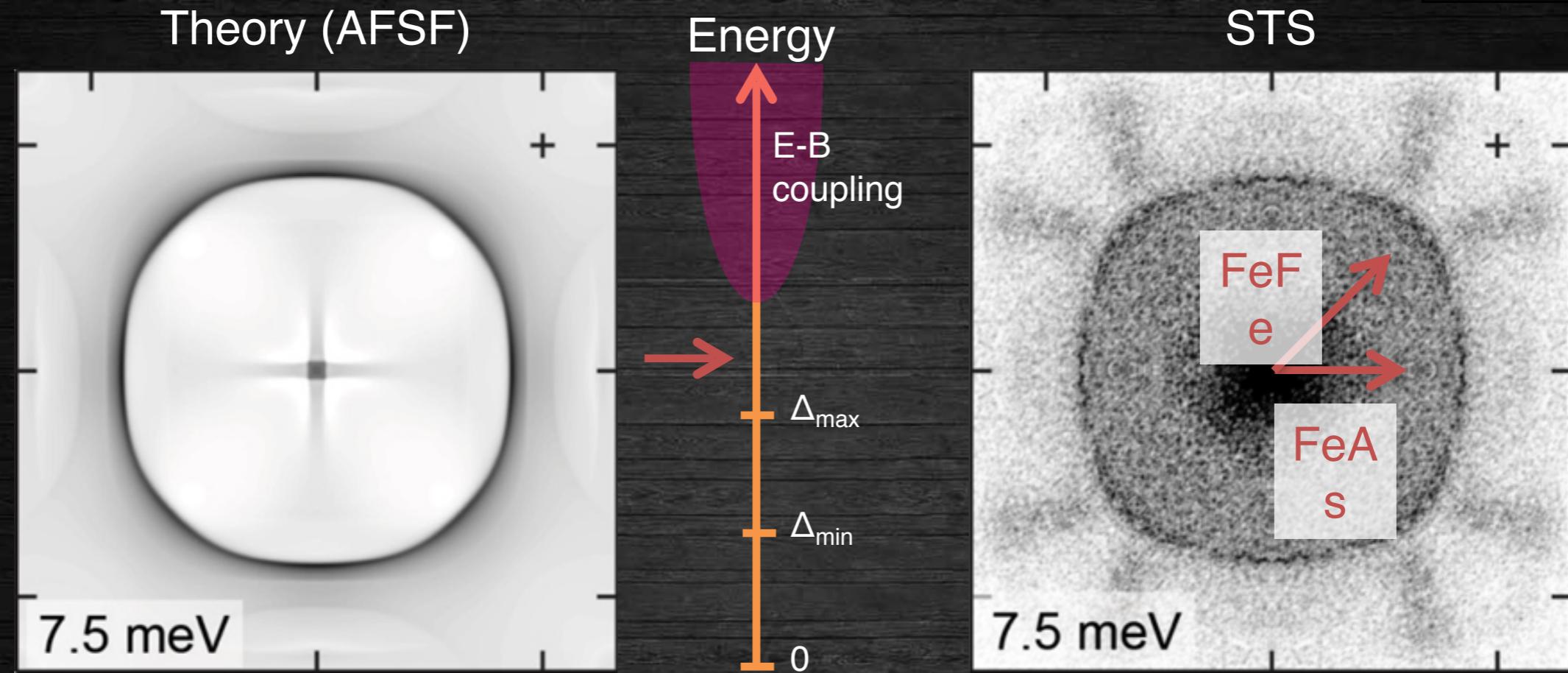
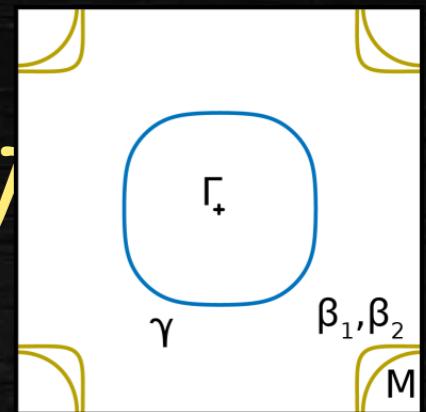
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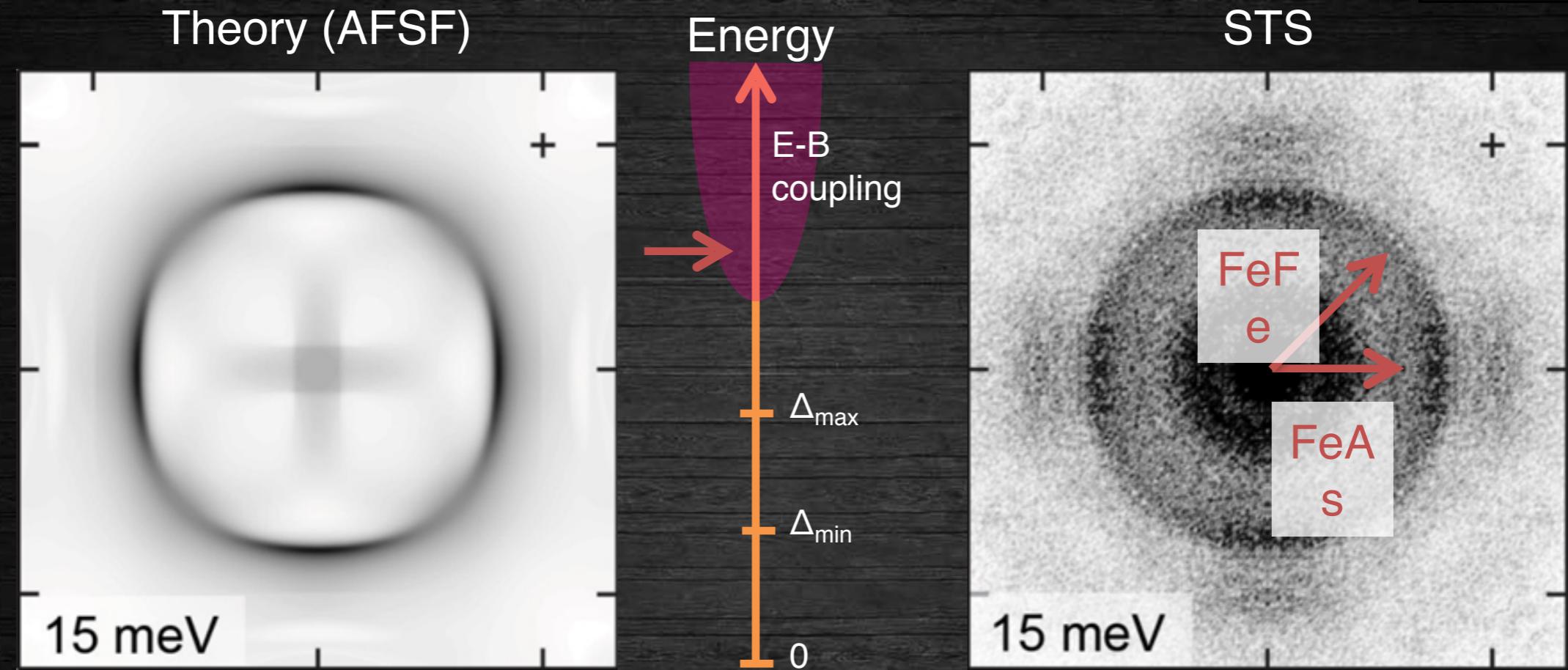
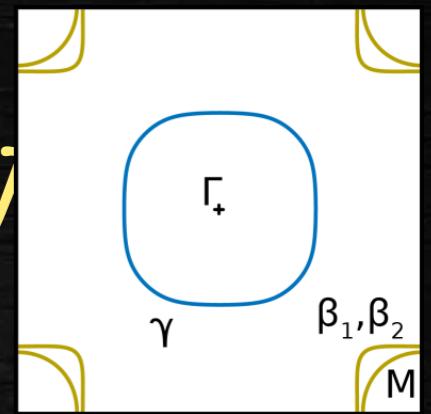
Low energy anisotropy due to
gap anisotropy



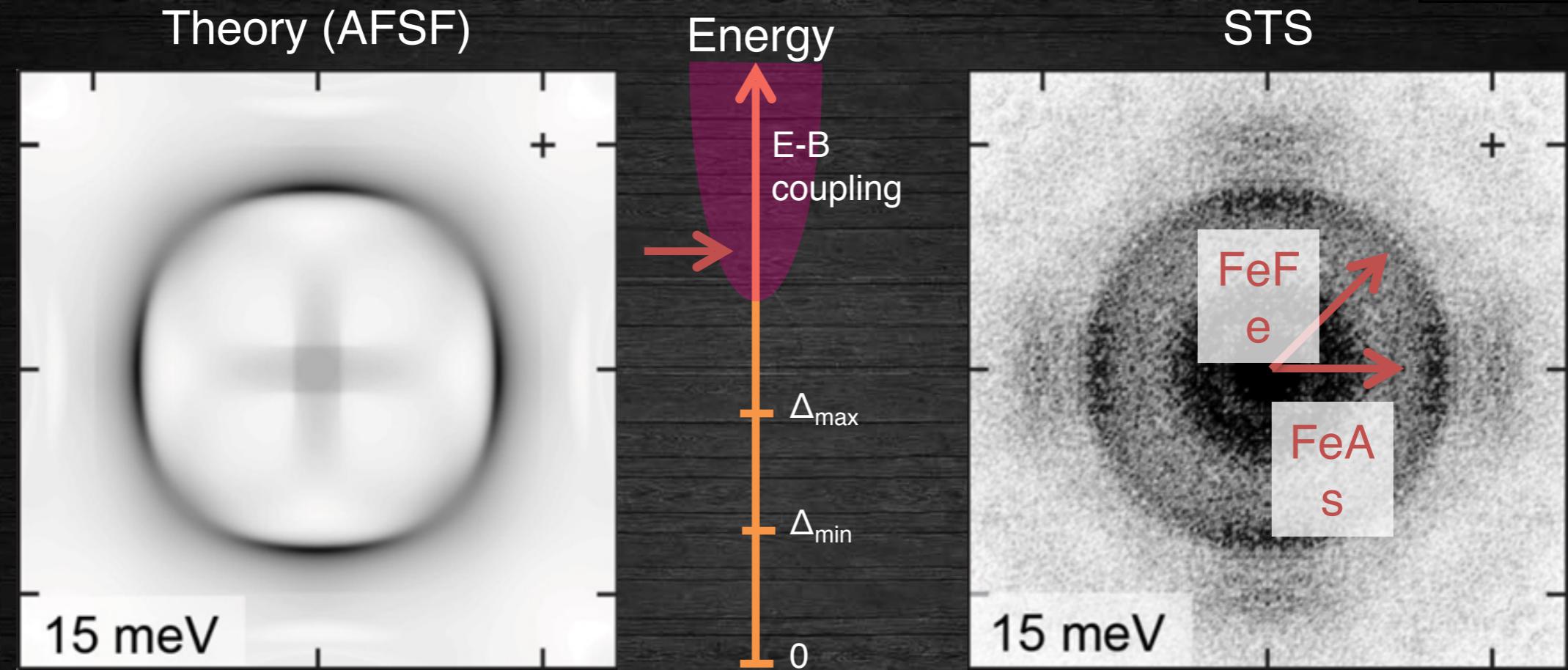
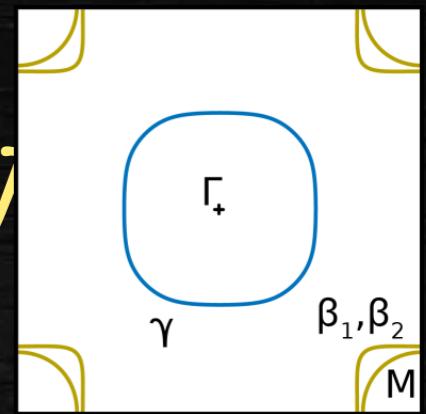
Energy Dependent Anisotropy



Energy Dependent Anisotropy



Energy Dependent Anisotropy



High energy self-energy effect
Intensity suppressed along
Fe-Fe

Insight from Kinematics

Insight from Kinematics

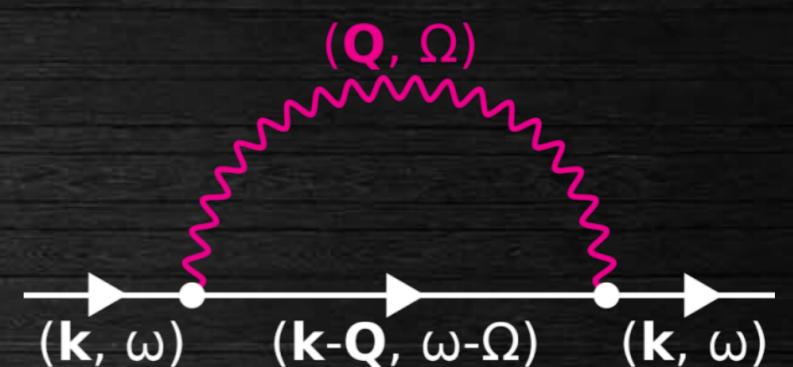
- AFSF centered at (\mathbf{Q}, Ω)

- Strong self energy effect when satisfying

$$\omega_{\mathbf{k}}^{\gamma} = \omega_{\mathbf{k}-\mathbf{Q}}^{\beta} + \Omega$$

- AFSF couples γ pocket to β_1 and β_2

- *Energy dependent anisotropy*



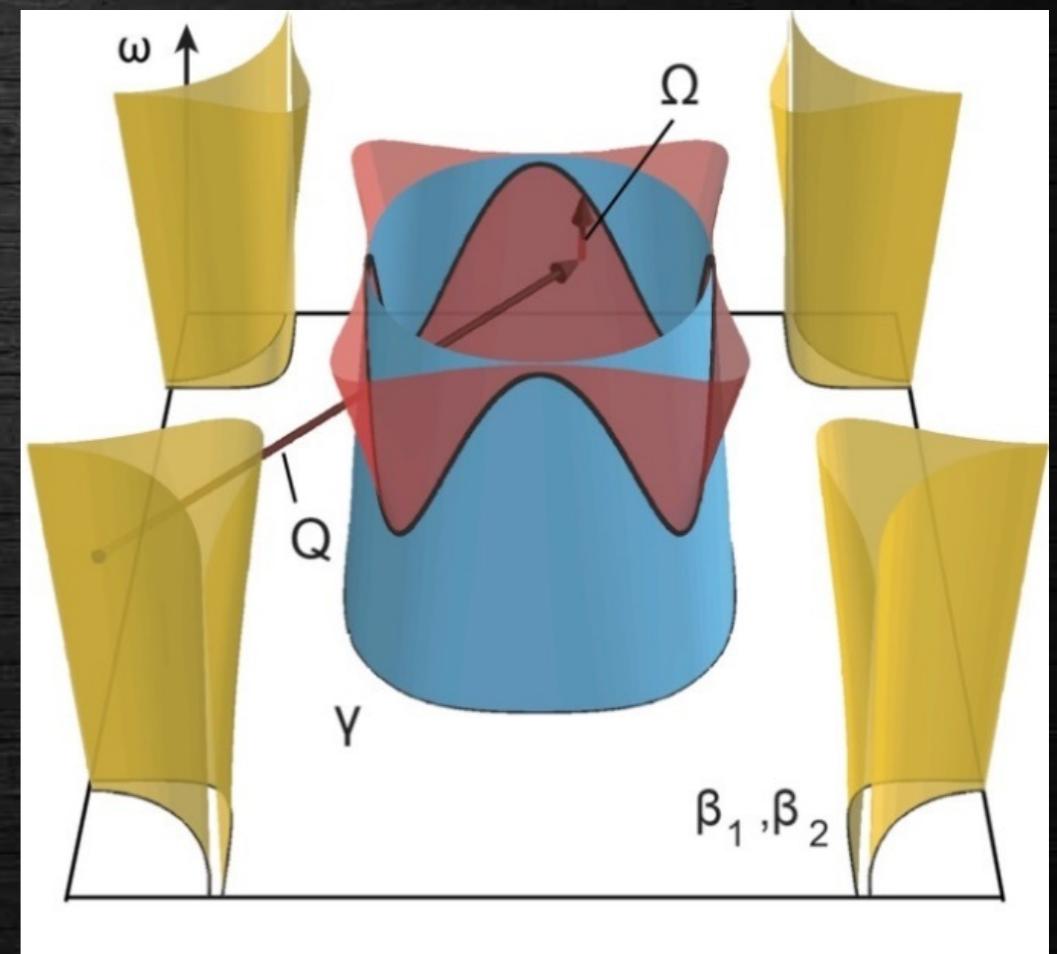
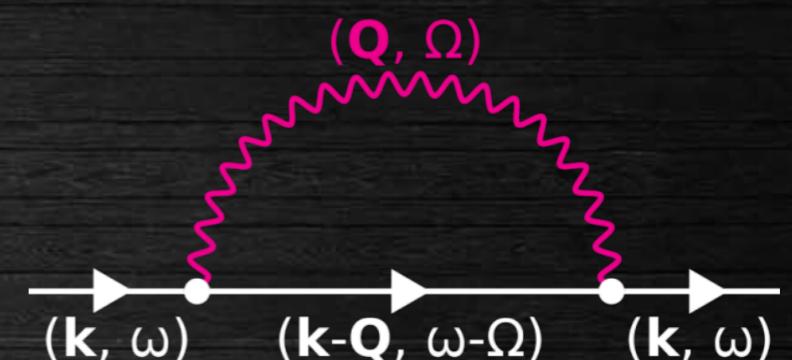
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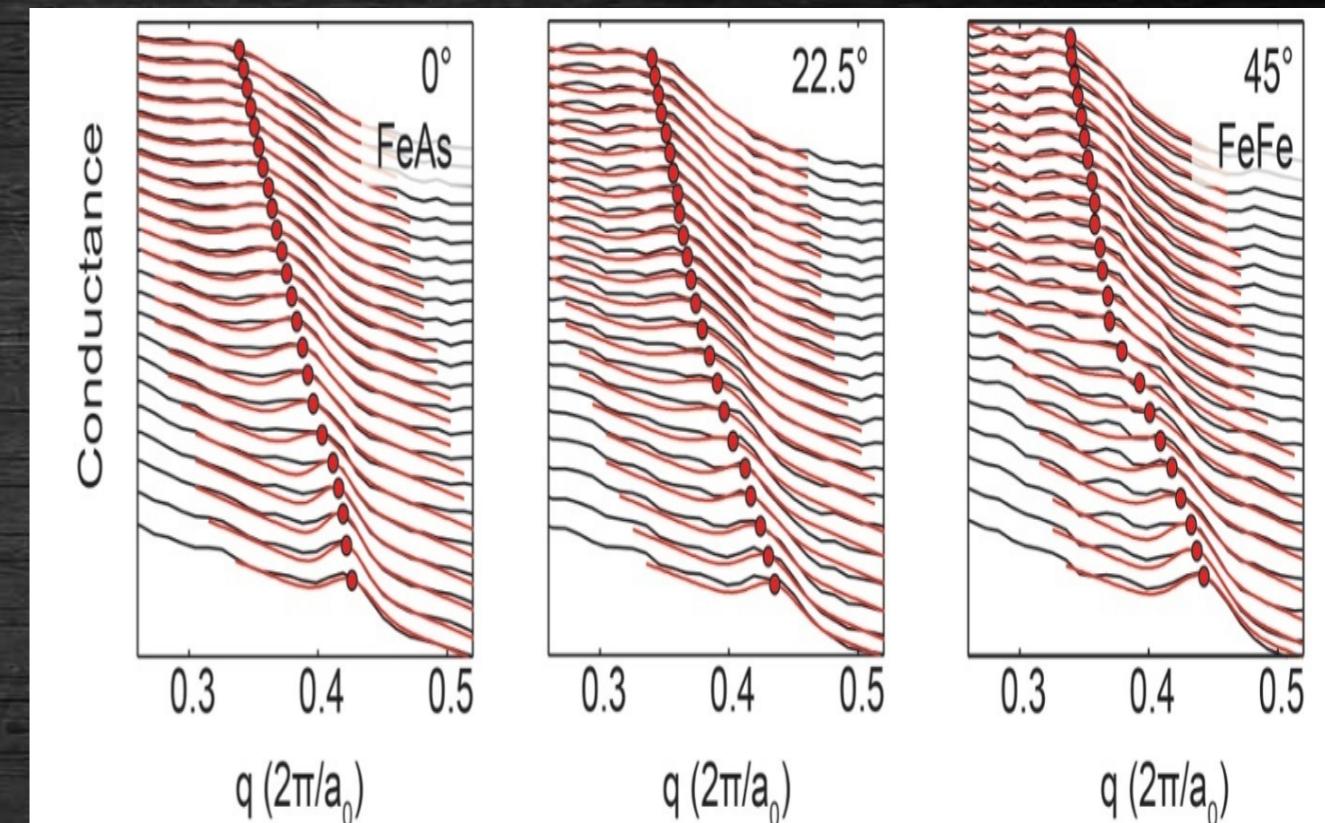
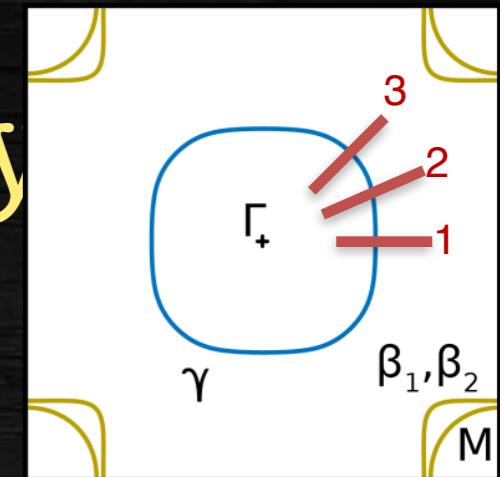
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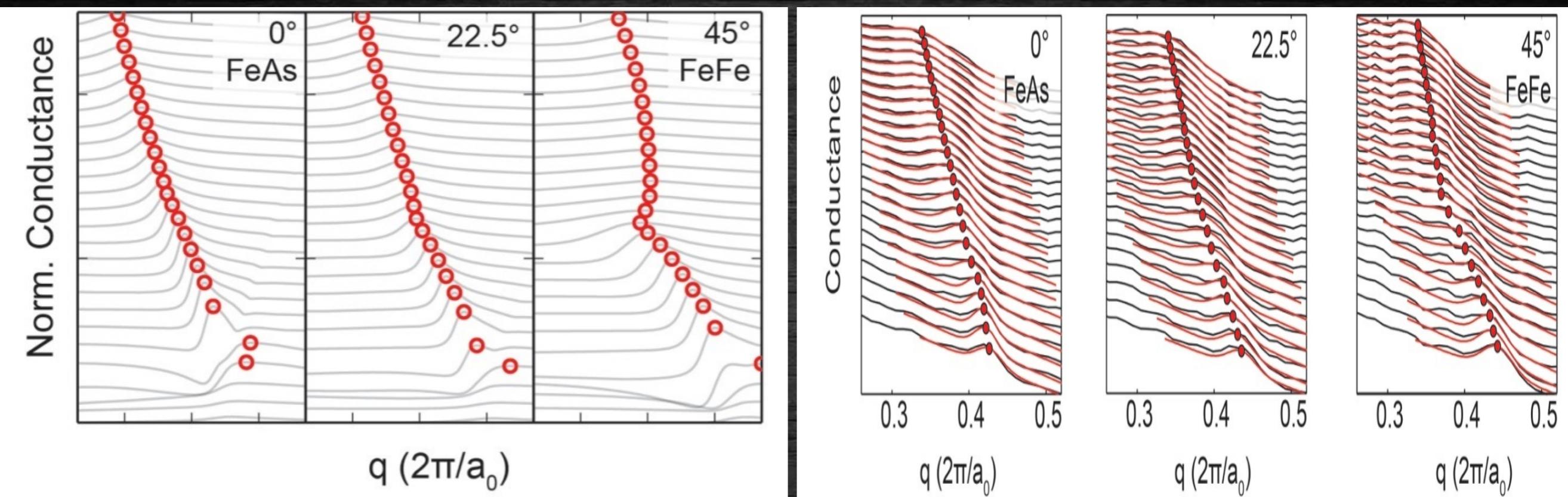
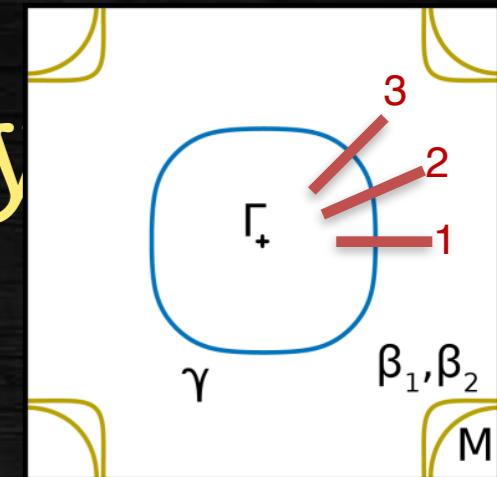
Energy Dependent Anisotropy

- STS



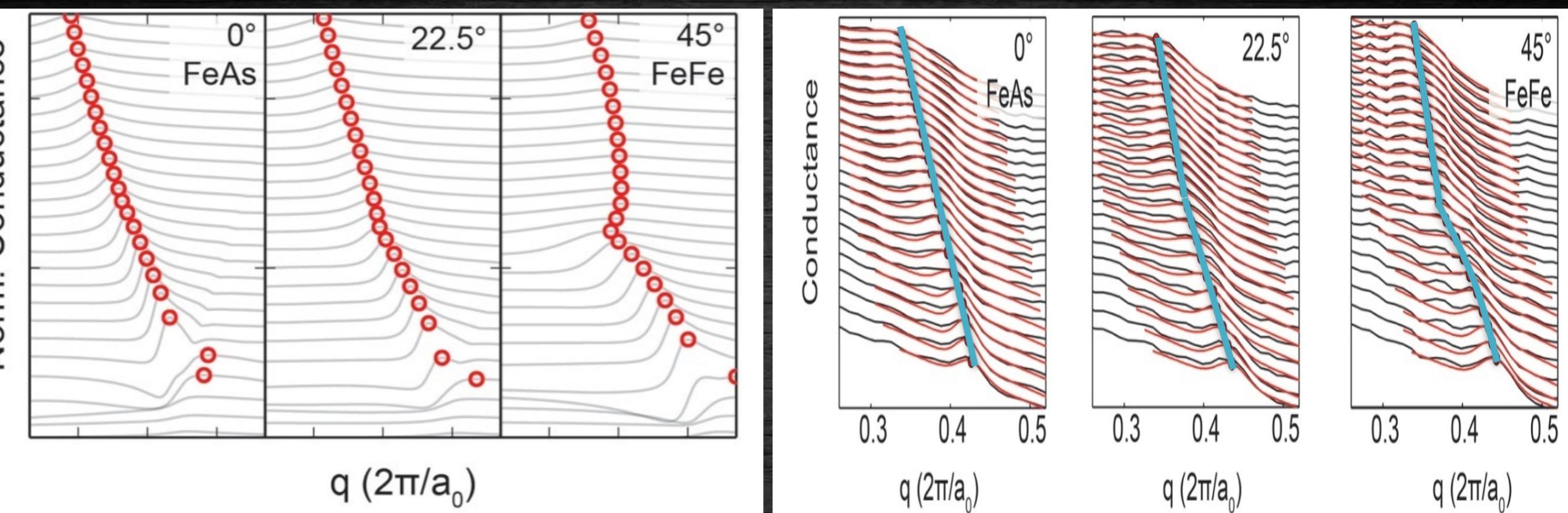
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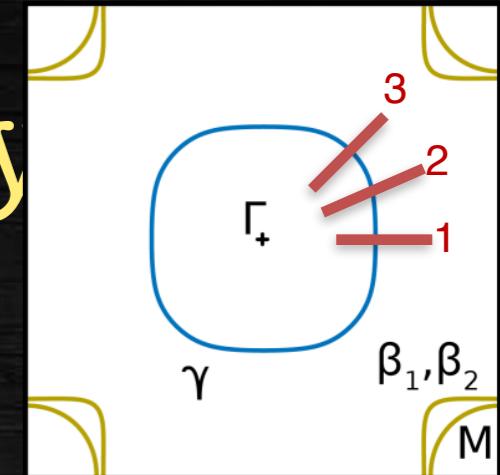


Energy Dependent Anisotropy

- Theory (AFSF)



- STS



Self-energy due to Eg phonon

Prediction for Phonon

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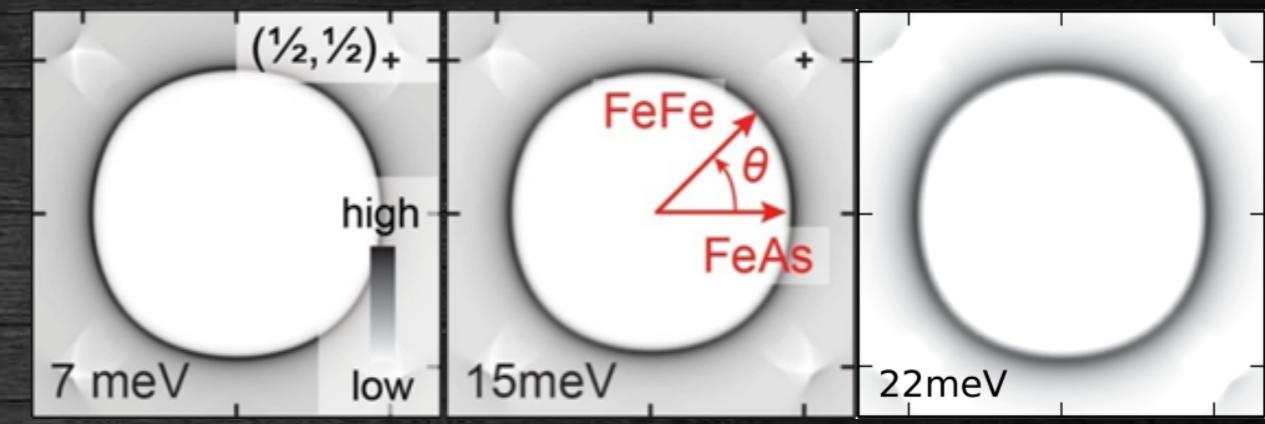
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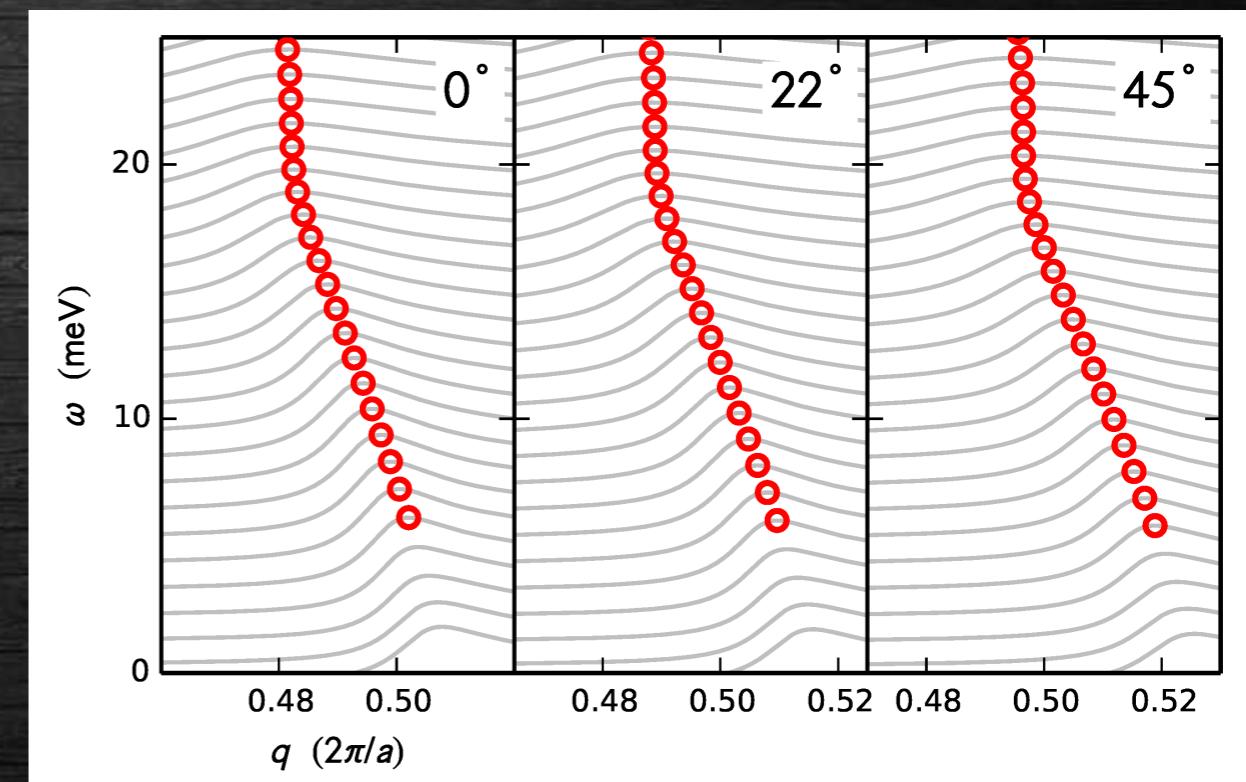
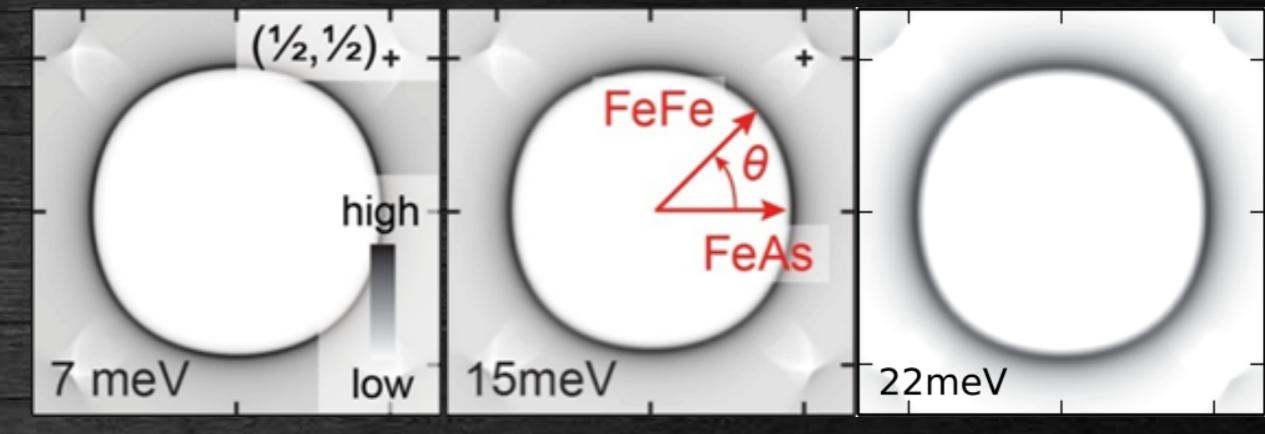
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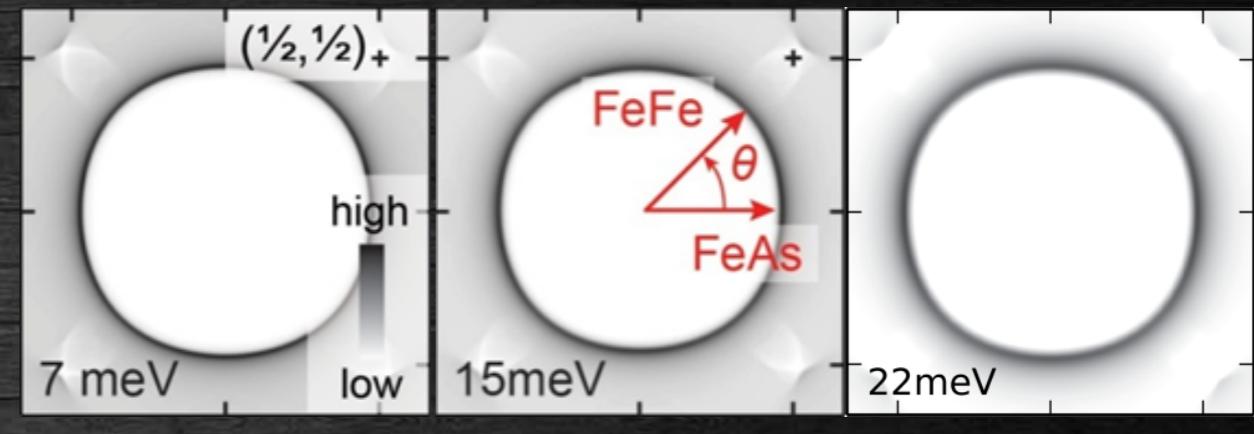
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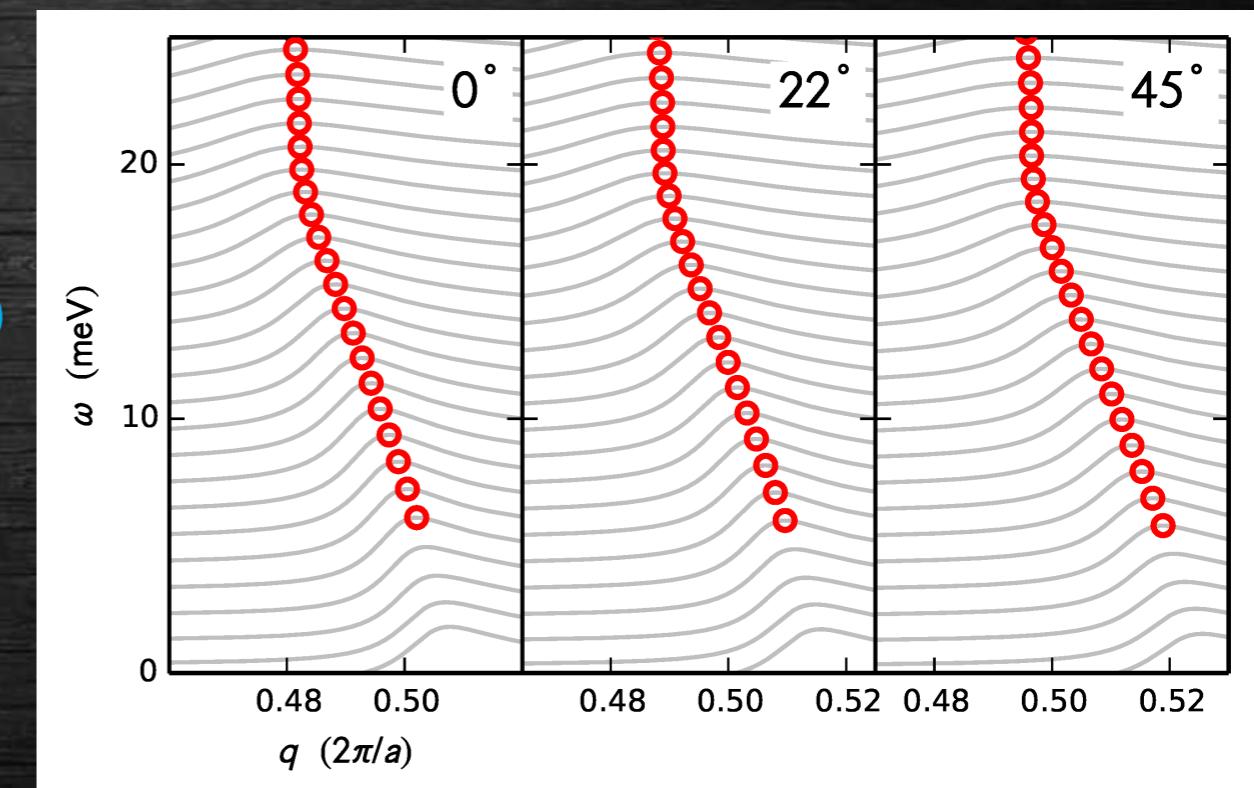


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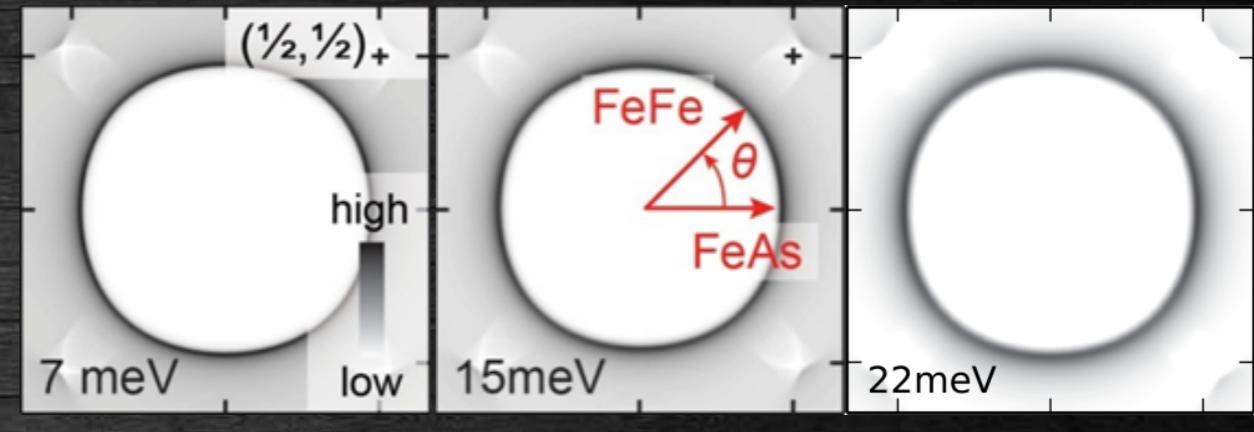


- Isotropic self energy on γ
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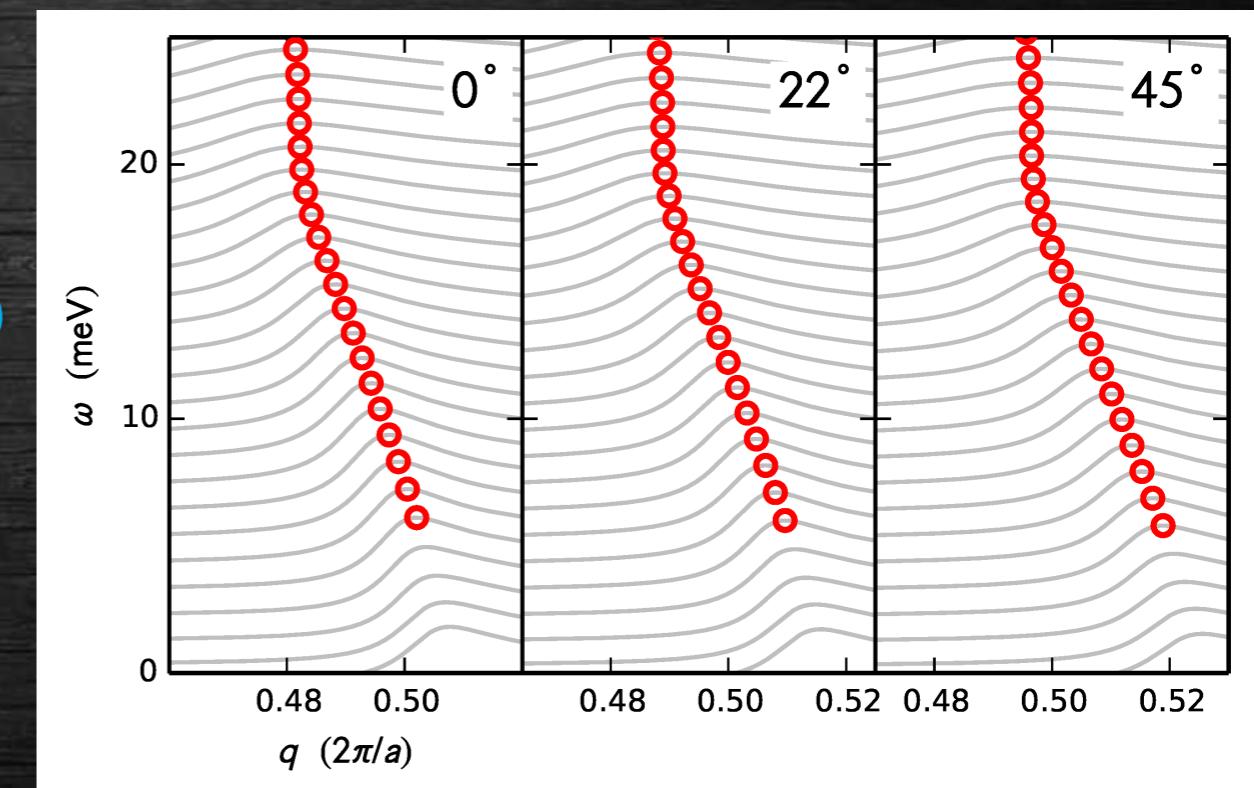


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- Isotropic self energy on γ
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Mechanism: Summary

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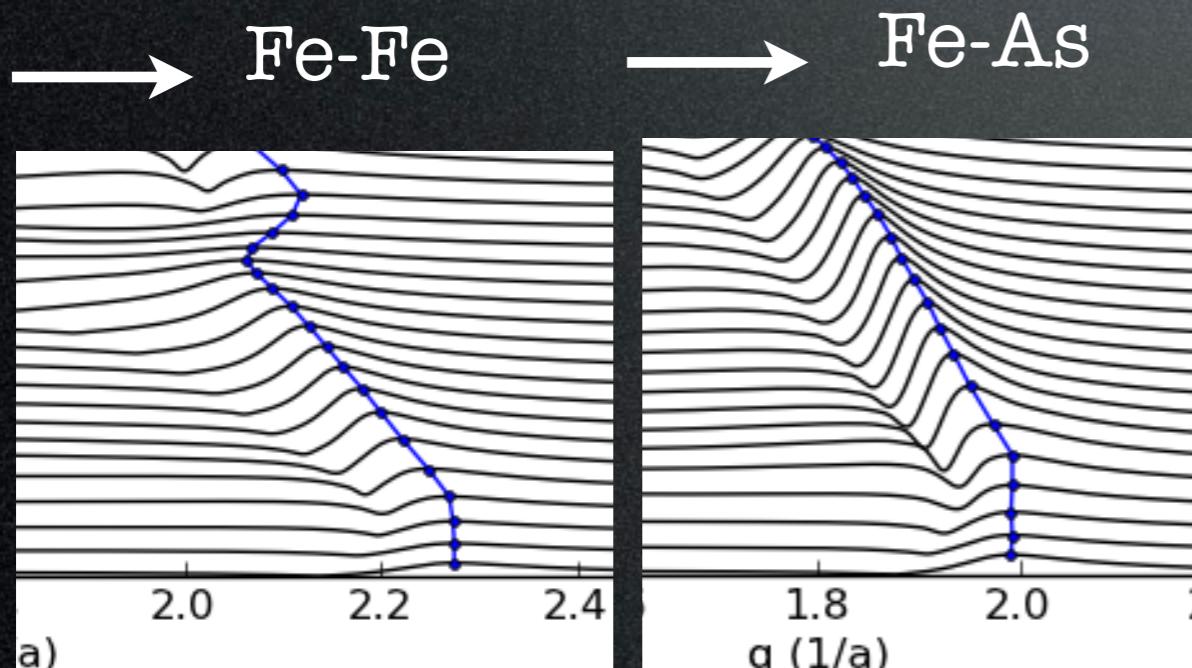
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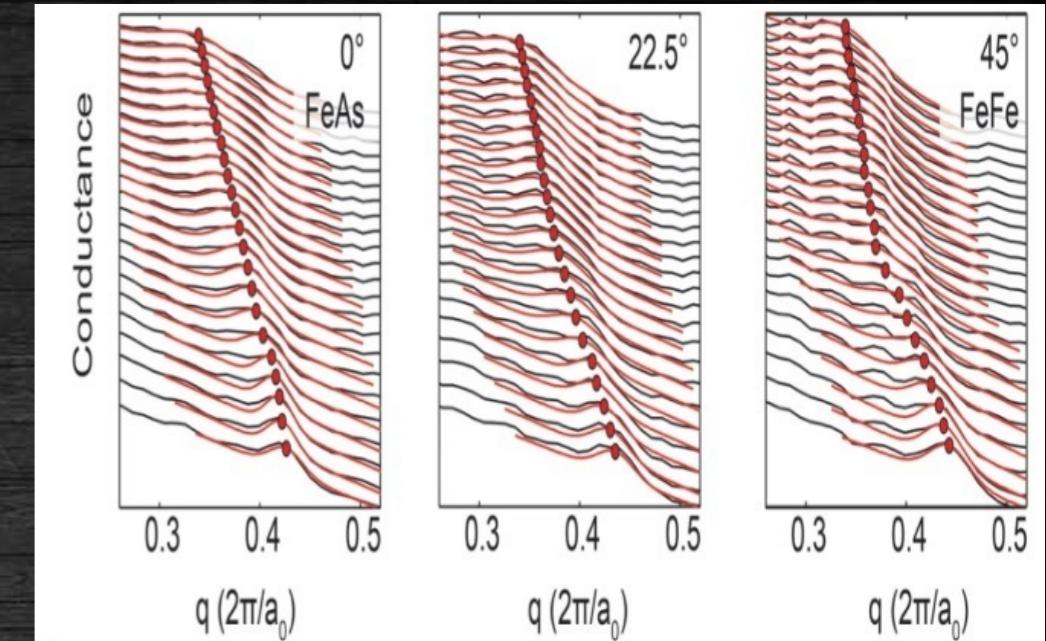


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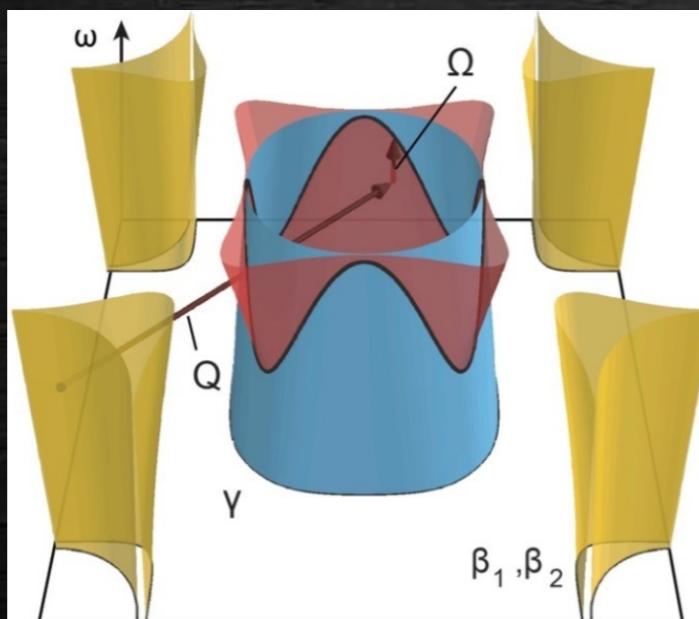
Allan, Lee et al, arXiv:1402.3714, to appear in Nat. Phys.

- Fingerprint of electron-boson coupling in LiFeAs :energy selective anisotropic self-energy
- Mode at finite $Q \rightarrow$ anisotropic self energy

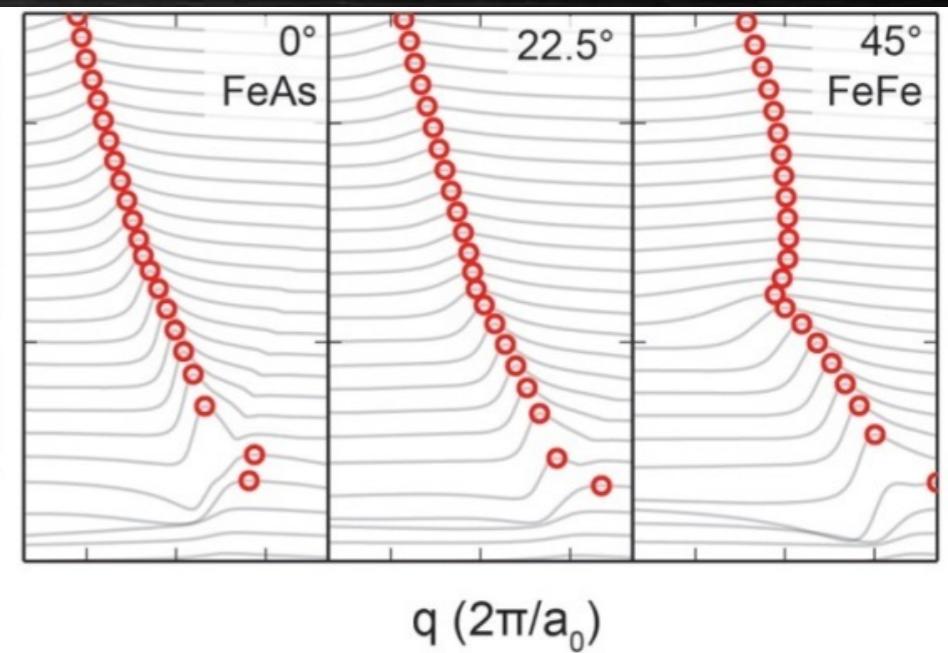
STS



AFSF



Norm. Conductance



Collaborators

Experimentalists

J.C. Davis (Cornell, BNL)
H. Eisaki (AIST)
K. Fujita (Cornell)
ChungKoo Kim (Cornell)
Y. Kohsaka (RIKEN)
Jihnhwan Lee (KAIST)
K. Shen (Cornell)
A. Schmit (Berkeley)
S. Uchida (U-Tokyo)

Theorists

M. Lawler (SUNY Binghamton)
A. Mesaros (Cornell, Leiden)
J. Sethna (Cornell)
S. Sachdev (Harvard)
J. Zaanen (Leiden)
Kyungmin Lee (Cornell)
Mark Fischer (Cornell)
Arun Paramekanti (U Toronto)

References

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Lawler, Fujita, et. al., Nature **466**, 347 (2010)
Mesaros, Fujita, et. al, Science **333**, 426 (2011)
Fischer and Kim, PRB **84**, 144502 (2011)
Fujita, et. al., Science (2014)
Allan, Lee et. al., to appear in Nature Physics (2014)
Fischer, et. al., to appear in NJP (2014)